

The growth mechanism of carbon nanotubes within the "cluster volume to surface area" model

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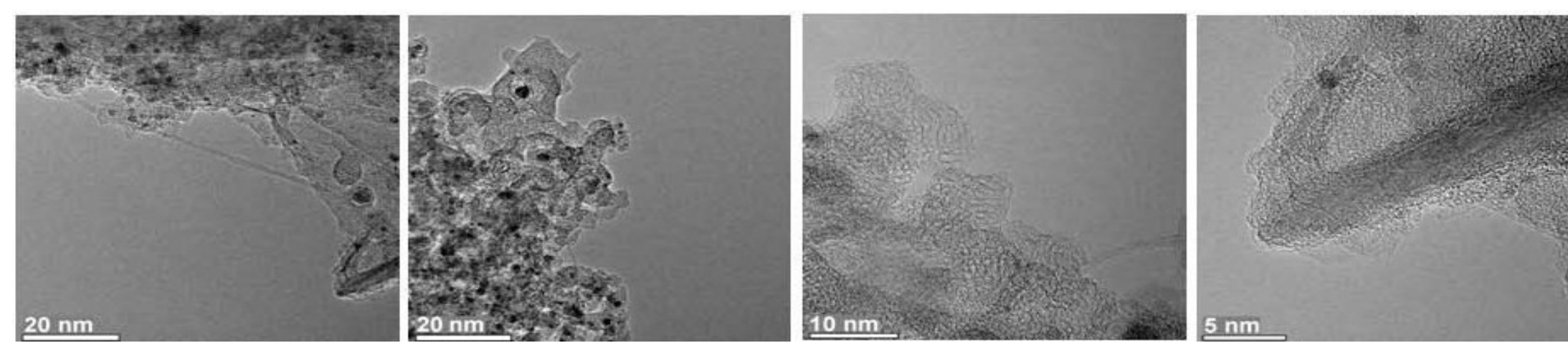
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Abstract

The influence of mixed catalysts for the high yield production of carbon nanotubes (CNTs) has been studied systematically. Based on extensive experimental data a "Catalyst Volume to Surface Area" (CVSA) model was developed to understand the influence of the process parameters on the yield and CNT diameter distribution [1,2]. In our study, we present a refined version of the CVSA model developed by combining experiments and simulations.

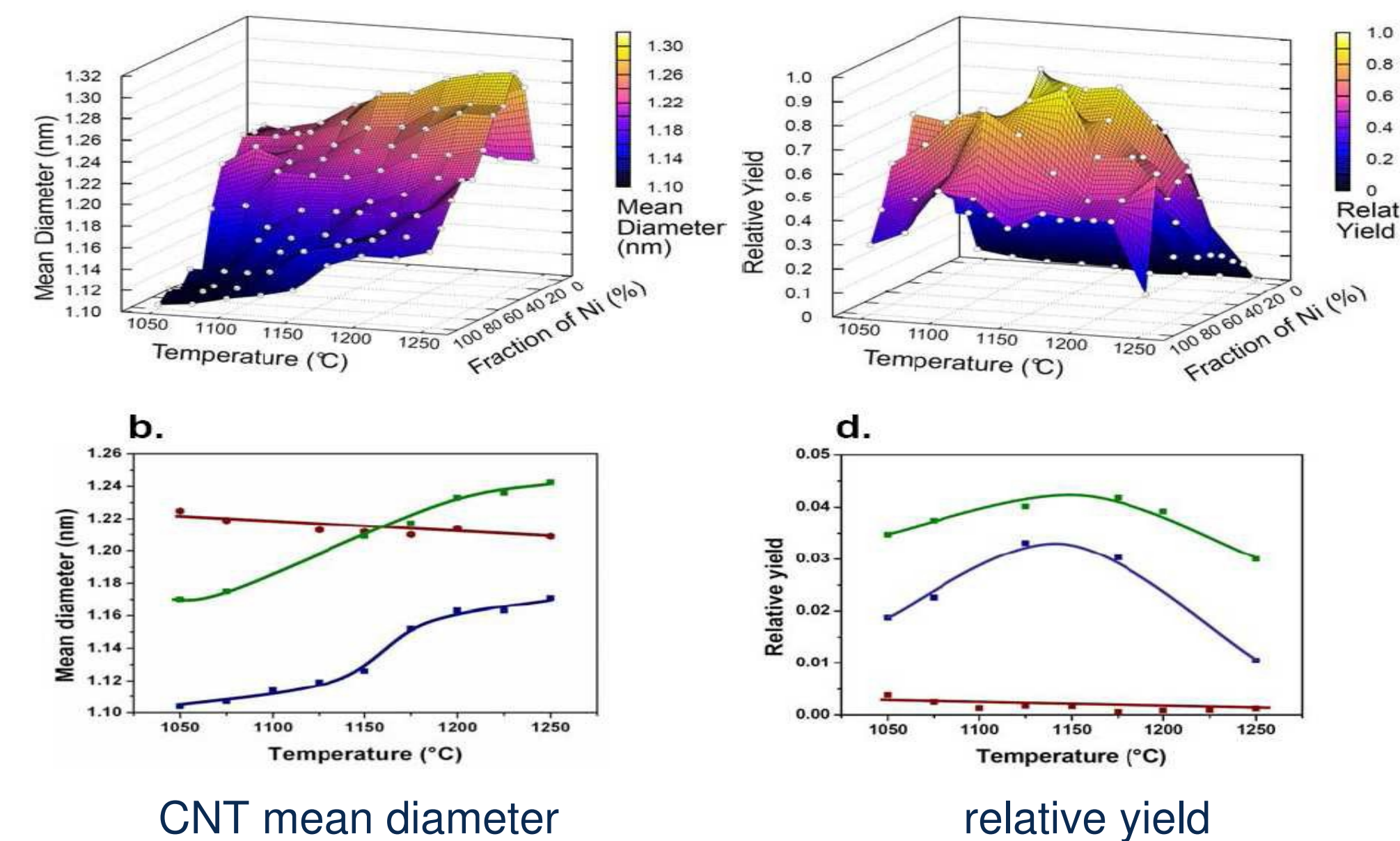
Experiments

- synthesis of carbon nanotubes (CNTs) by laser ablation with mixed catalysts



TEM images

- characterization of CNTs by optical absorption spectroscopy (OAS) [1]



CNT mean diameter

relative yield

Motivation

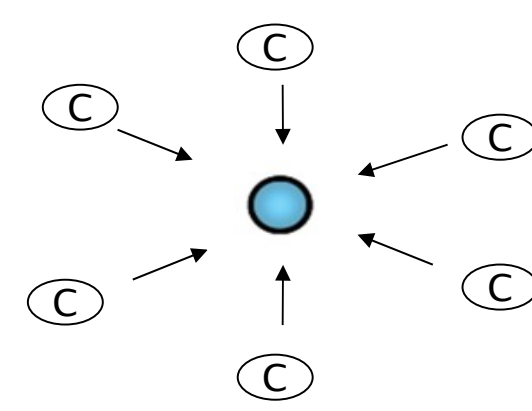
Want to understand the growth mechanism.

Strategy

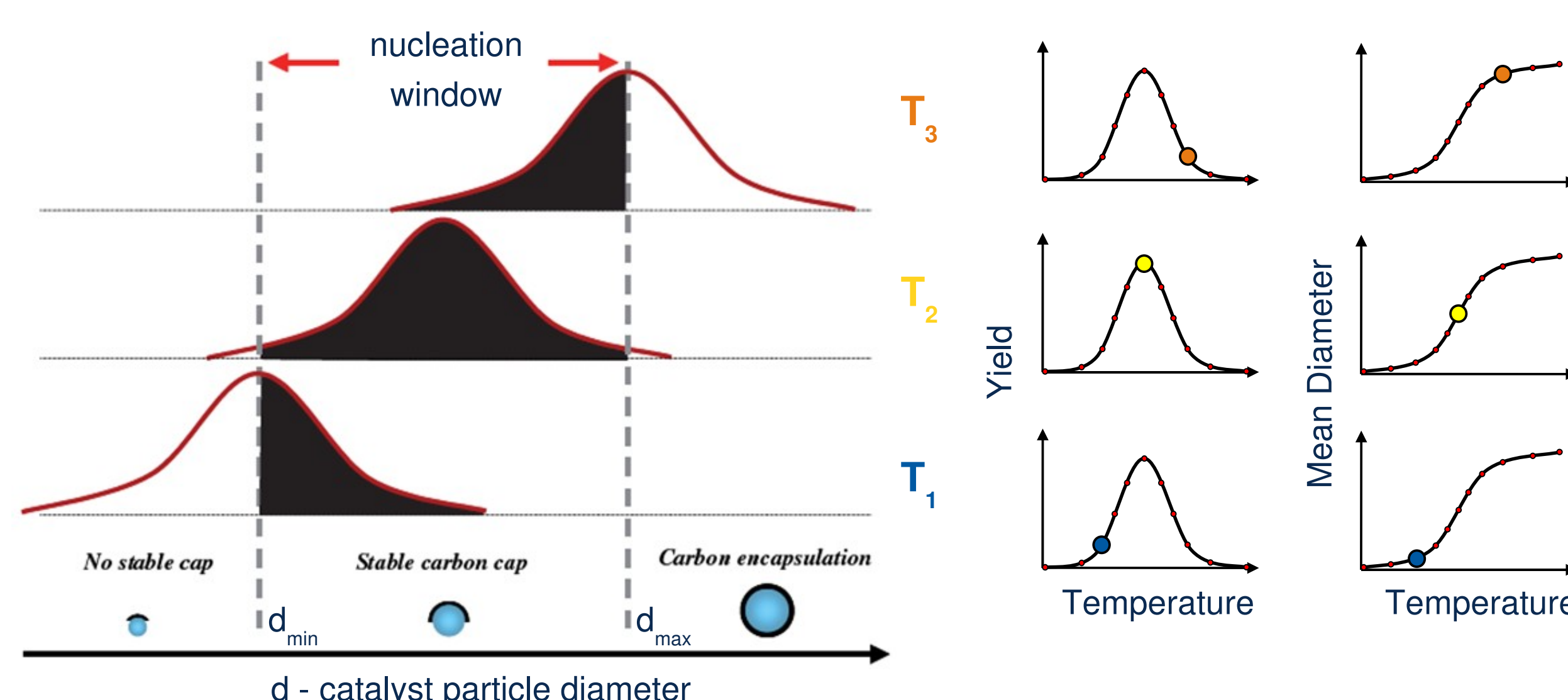
- use "cluster volume to surface area" (CVSA) growth model [1,2]
- formulate the model mathematically
- fit measured data to the model and determine the model parameters
- interpret the model parameters in terms of microscopic quantities

Growth Mechanism of Carbon Nanotubes (CVSA)

- after laser evaporation carbon dissolves into the catalyst particle and a liquid metal-carbide is formed
- the bigger the particles the more carbon is inside
- during the condensation carbon precipitates via the surface
- for CNT nucleation, formation of hemispherical cap is necessary
- the catalyst particle size increases with furnace temperature. Why?

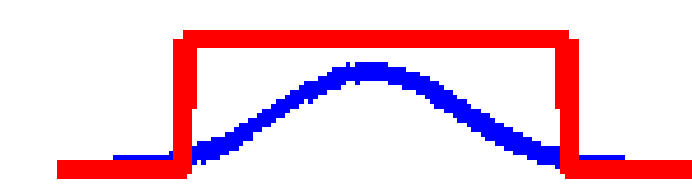


- during cooling the catalyst particles condensate
- the higher the temperature the longer is the cooling time



Results: Mathematical Formulation of the CVSA model

- $n(d)$: nucleation window = rectangular function
- $s(d)$: catalyst particle diameter distribution = Gaussian distribution
- $g(d) = n(d) \cdot s(d)$: growth function



T = temperature

C = composition of catalysts

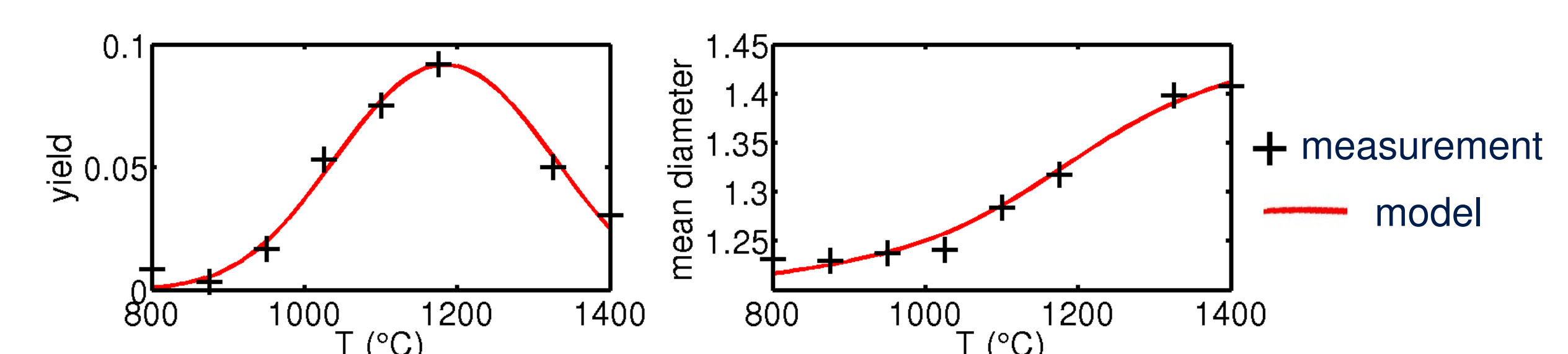
$$\text{yield: } N_{CNT}(T, C) = \int_{-\infty}^{\infty} g(d^{CNT}, T, C) \delta d^{CNT}$$

$$\text{mean diameter: } d_0^{CNT}(T, C) = \frac{1}{N_{CNT}} \int_{-\infty}^{\infty} d^{CNT} g(d^{CNT}, T, C) \delta d^{CNT}$$

- assumptions: $d^{CNT} = d^{CP}$: catalyst particle diameter = CNT diameter
 $d_0^s(T) = a + bT$: position of $s(d)$ shifts linearly with T
- model parameters: σ^s = spread (standard deviation) of $s(d)$
 N^{CP} = area below $s(d)$ = number of catalyst particles
 d_{min}, d_{max} = boundaries of $n(d)$
 a, b = parameters of $d_0^s(T) = a + bT$

Results: Fit of the CVSA Model to Measured Data

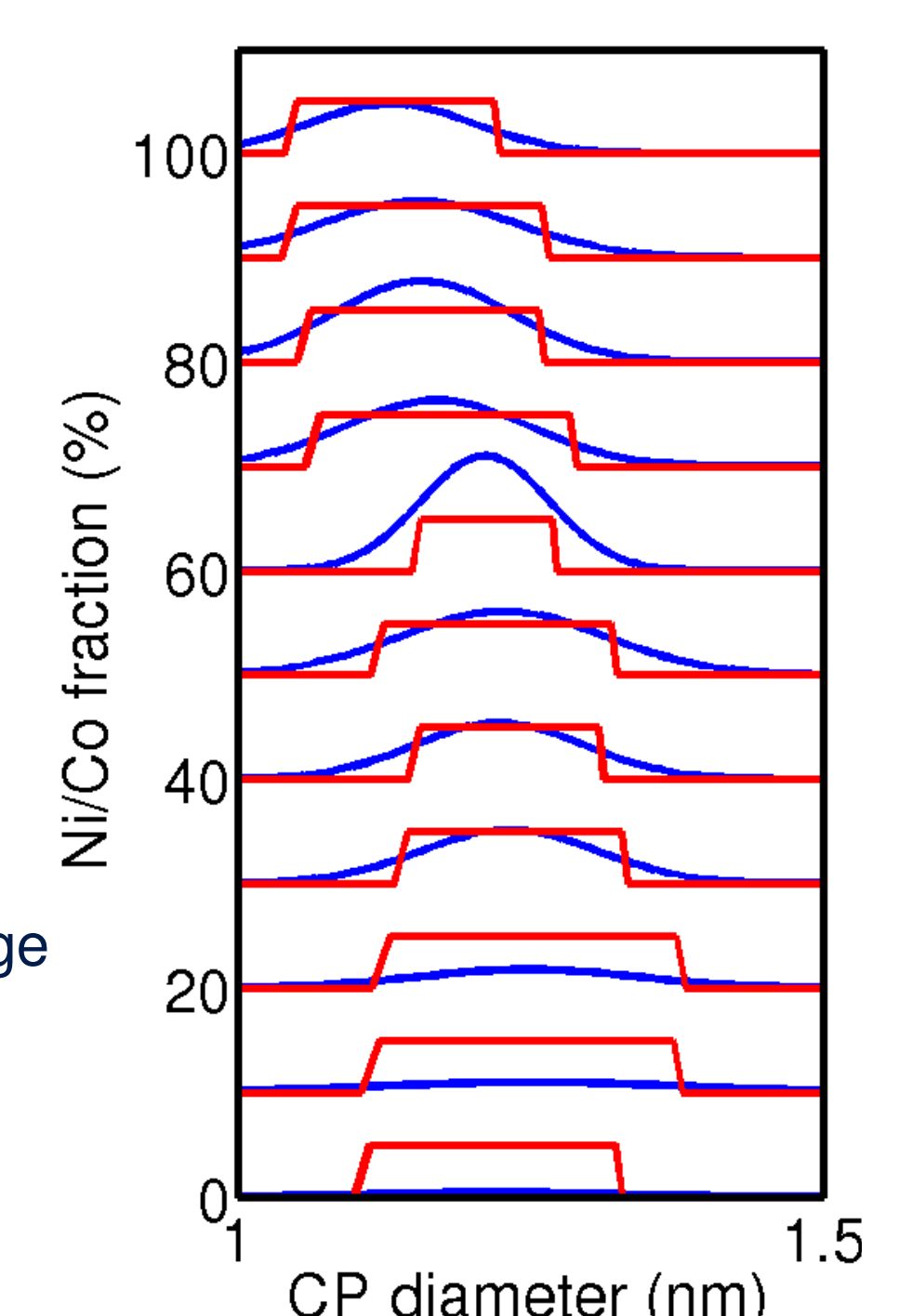
High yield catalyst mix Ni:Co:Mo = 5:4:1



model parameters: $\sigma^s = 0.100 \text{ nm} \pm 13.6\%$
 $N^{CP} = 0.108 \text{ a.u.} \pm 11.9\%$
 $d_{min} = 1.18 \text{ nm} \pm 1.3\%$, $d_{max} = 1.47 \text{ nm} \pm 1.3\%$
 $a = 0.143 \text{ nm} \pm 9.4\%$, $b = 0.001 \text{ nm/}^\circ\text{C}$ (fixed)

Catalyst mix with different Ni:Co fractions [1]:

- Results: with increasing Ni:Co fraction
 - the position of $n(d)$ shifts towards smaller diameters
 - the spread of $s(d)$, σ^s , changes very little
 - the number of catalyst particles, N^{CP} , changes strongly
- Problems:
 - fitting procedure needs to have the maximum of the yield in the measured range
 - some model parameters are correlated
 - measurements at low yields are very noisy = very hard to fit



Outlook

- more measurements are necessary to improve the data density
- unbiased data processing for OAS spectra needed
- improve the model and the fitting procedure (resolve correlated parameters and maximum yield problem)
- test reliability of model parameters to allow for a physical interpretation
- interplay of model and measurements to improve our understanding of the CNT growth mechanism

References

- [1] S. Tetali *et al.*, "Unravelling the Mechanisms Behind Mixed Catalysts for the High Yield Production of Single-Walled Carbon Nanotubes", ACS Nano **3**, 3839 (2009).
- [2] M. H. Rummeli *et al.*, "Catalyst Volume to Surface Area Constraints for Nucleating Carbon Nanotubes", J. Phys. Chem. B **111**, 8234 (2007).