

Magnetic N@C₆₀ single-molecule transistors

Towards modeling of real devices

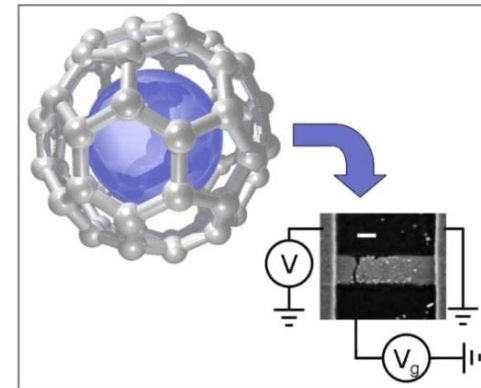
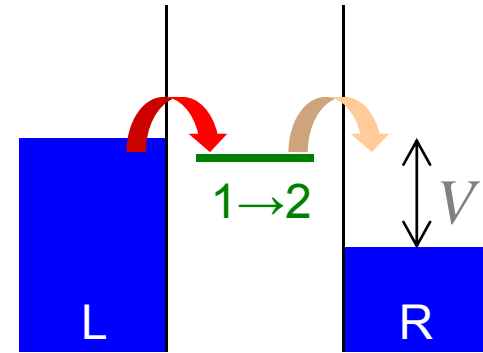
Carsten Timm



Max Bergmann Symposium 2008

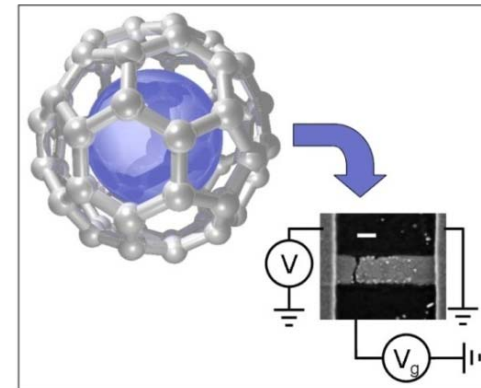
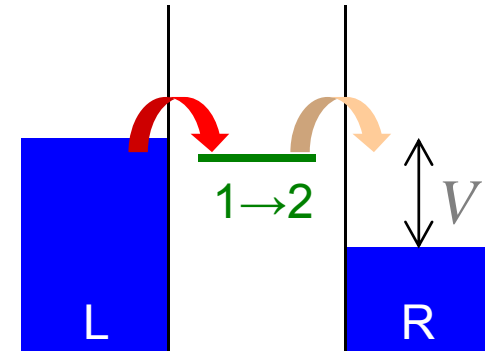
Overview

- Master equation formalism
- Endohedral $N@C_{60}$
- $N@C_{60}$ transistors

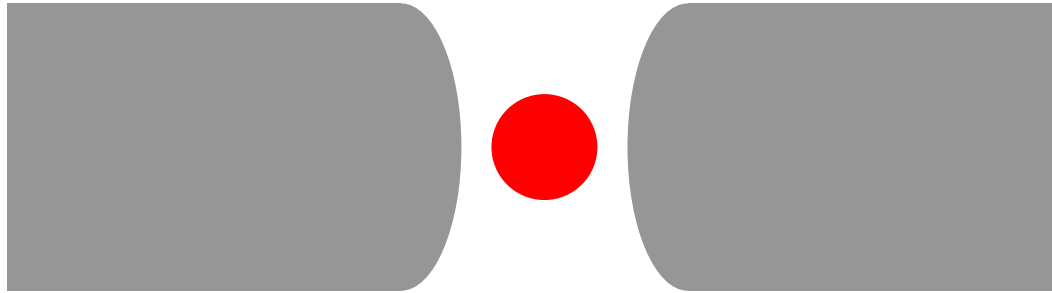


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Small system coupled to large reservoirs



Here: quantum dot / molecule coupled to bulk leads

$$\overline{A_{\text{dot}}}(t) = \text{?}$$



dot observable

$$\overline{I}(t) = \text{?}$$



current

$$\overline{A_{\text{dot}}}(t) = \text{Tr } \rho(t) A_{\text{dot}} \quad \text{with the density operator} \quad \rho(t) \cong \rho_{\text{dot}}(t) \otimes \rho_{\text{leads}}^0$$

Cannot solve this because H is complicated!

Now what?

A_{dot} only depends on the dot: $\overline{A_{\text{dot}}}(t) = \text{Tr } \rho_{\text{dot}}(t) A_{\text{dot}}$

with **reduced density operator** (in “small” dot Hilbert space)

$$\rho_{\text{dot}} \equiv \sum_i \langle\langle i | \rho | i \rangle\rangle \equiv \text{tr}_{\text{leads}} \rho$$

 basis of **lead** (reservoir) states only


Big question: What is the equation of motion of $\rho_{\text{dot}}(t)$?

The Master Equation!

Many different approaches; all start from the von Neumann equation:

$$\frac{d\rho}{dt} = -i [H, \rho] \quad \Longrightarrow \quad \frac{d}{dt} \rho_{\text{dot}} = -i \text{tr}_{\text{leads}} [H, \rho(t)]$$

Wangsness-Bloch-Redfield master equation

Hamiltonian $H = H_{\text{dot}} + H_{\text{leads}} + H_{\text{hop}}$  here: electron hopping between dot and leads

- iterate von Neumann equation to expand to second order in H_{hop}
- assume **product state** with leads in equilibrium at time t : $\rho(t) \cong \rho_{\text{dot}}(t) \otimes \rho_{\text{leads}}^0$
means that dot and leads are uncorrelated (**strong** but superfluous assumption)

$$\frac{d}{dt} \rho_{\text{dot}} \cong -i [H_{\text{dot}}, \rho_{\text{dot}}(t)] - \int_{-\infty}^t dt' \text{tr}_{\text{leads}} \left[H_{\text{hop}}, \left[e^{-i(H_{\text{dot}} + H_{\text{leads}})(t-t')} H_{\text{hop}} e^{i(H_{\text{dot}} + H_{\text{leads}})(t-t')}, \rho_{\text{dot}}(t) \otimes \rho_{\text{leads}}^0 \right] \right]$$

Wangsness-Bloch-Redfield master equation

not of the form $\frac{d\rho_{\text{dot}}}{dt} = -i [\tilde{H}, \rho_{\text{dot}}]$

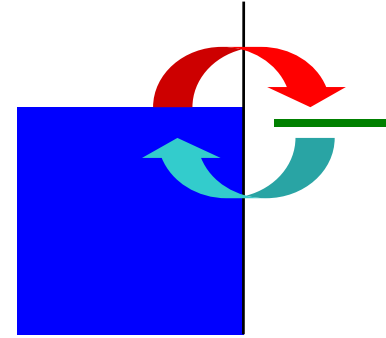
see C.T. , PRB **77**,
195416 (2008)

→ time evolution **not unitary**, includes **relaxation**

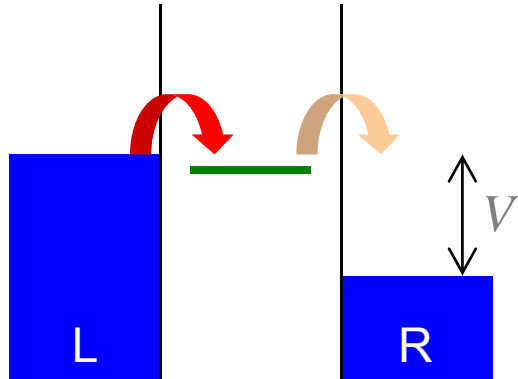
Case 1: single reservoir (particle & energy bath)

dot approaches equilibrium for $t \rightarrow \infty$:

$$\rho_{\text{dot}} \propto e^{-\beta(H_{\text{dot}} - \mu N_{\text{dot}})}$$



Case 2: two leads in *separate* equilibrium—e.g. different chemical potential



Have a **bias voltage** V

Keeps dot out of equilibrium
but approaches a steady state

Rate equations

Unperturbed dot many-particle eigenstates: $H_{\text{dot}} |m\rangle = E_m |m\rangle$

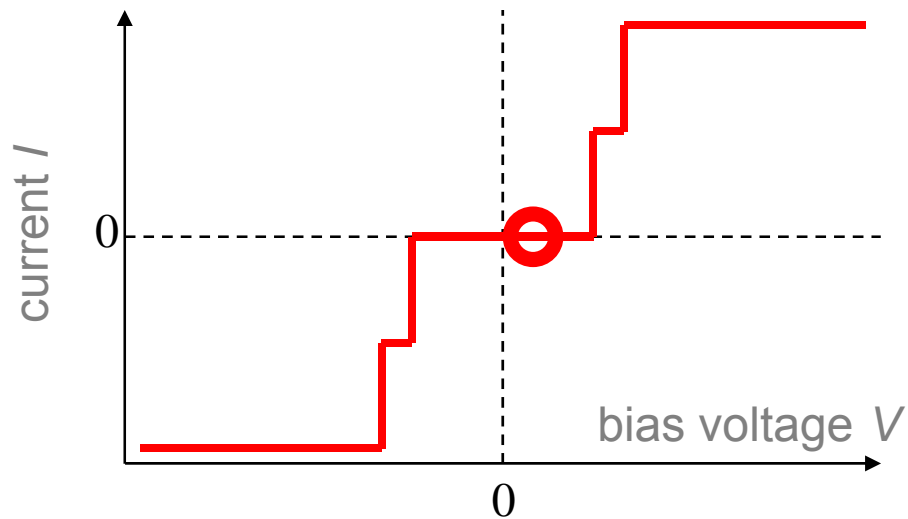
If off-diagonal components of ρ_{dot} in basis $\{|m\rangle\}$ relax rapidly (**rapid dephasing**):
sufficient to keep only diagonal components

$P_m \equiv (m | \rho_{\text{dot}} | m)$ **probabilities** of dot states $|m\rangle$

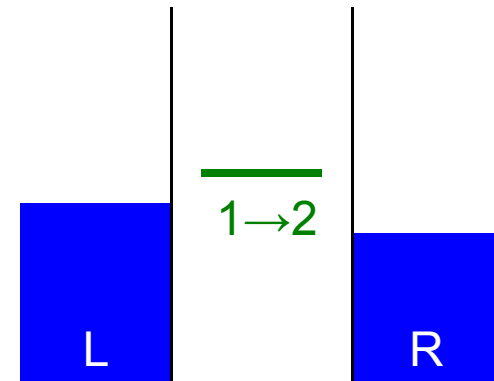
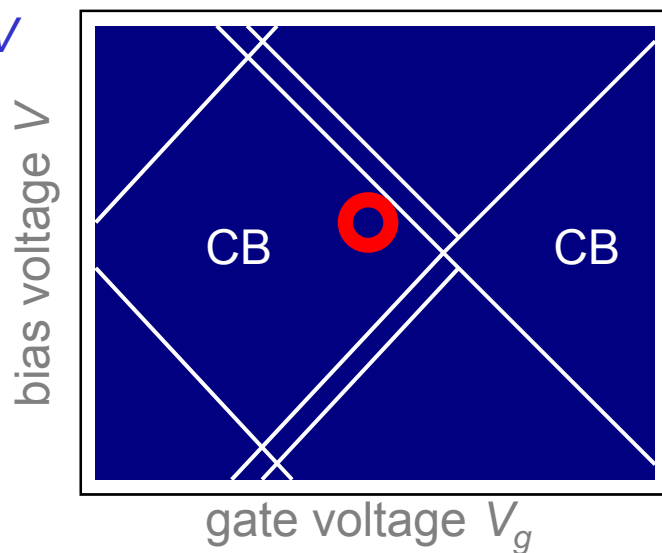
obtain rate equations
$$\frac{dP_m}{dt} = \sum_n \left(\underset{\text{in}}{R_{n \rightarrow m} P_n} - \underset{\text{out}}{R_{m \rightarrow n} P_m} \right)$$

 $P_m(t)$  observables, e.g. $I(t) \equiv \bar{I}(t)$

Generic behavior described by rate equations



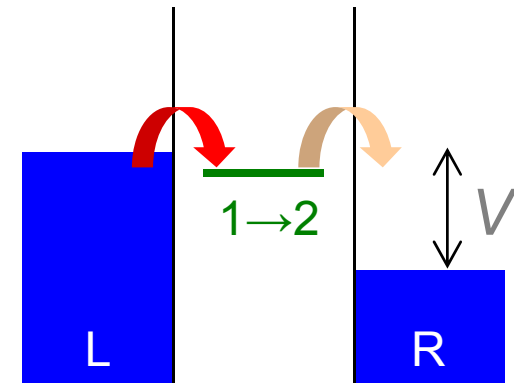
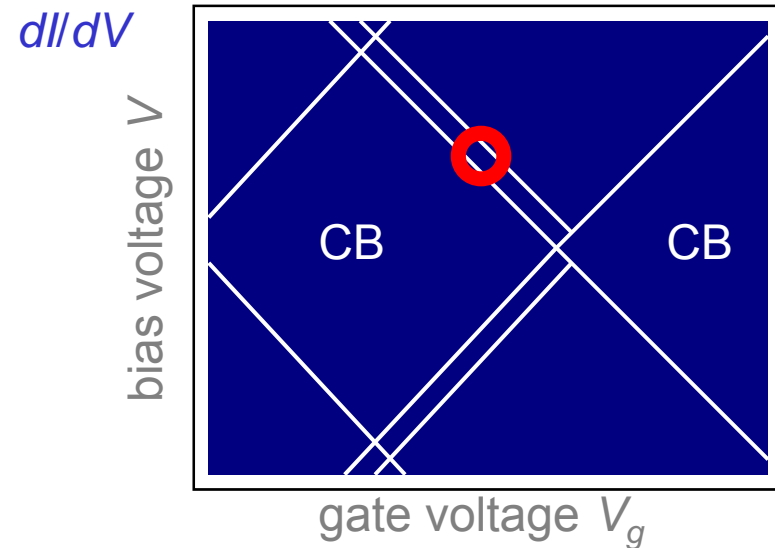
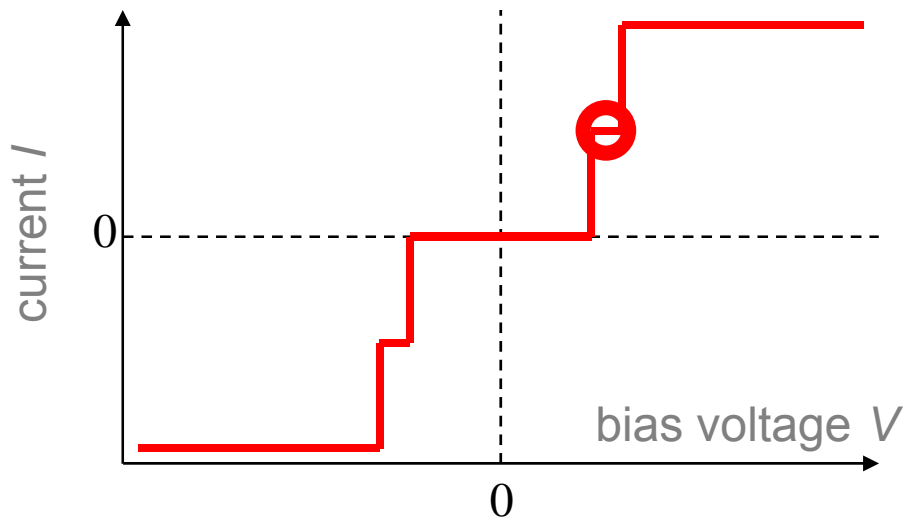
dI/dV



very small current:

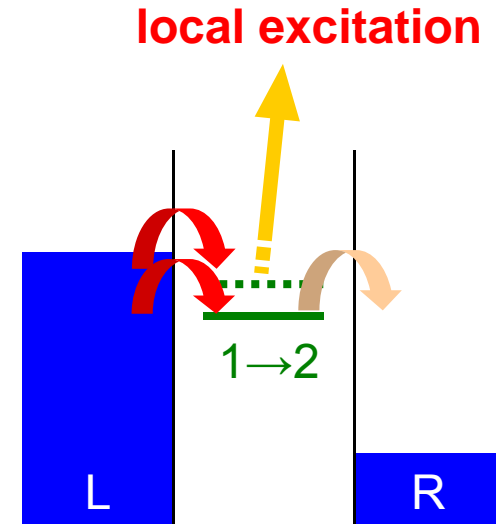
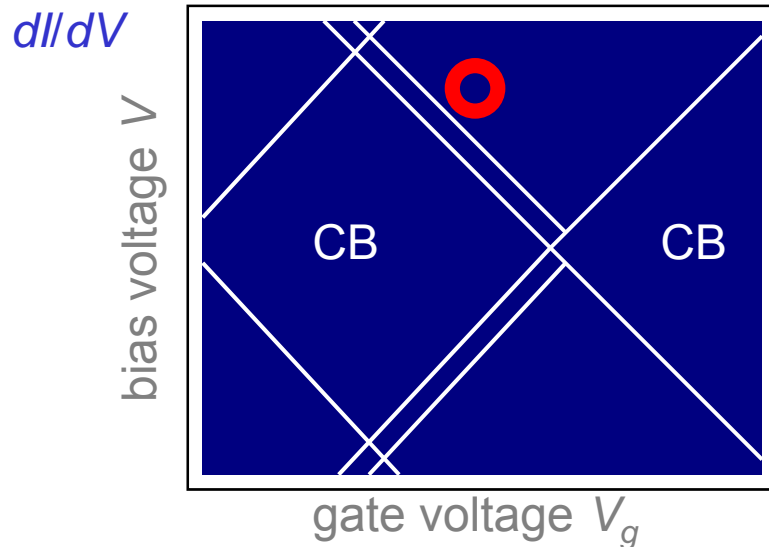
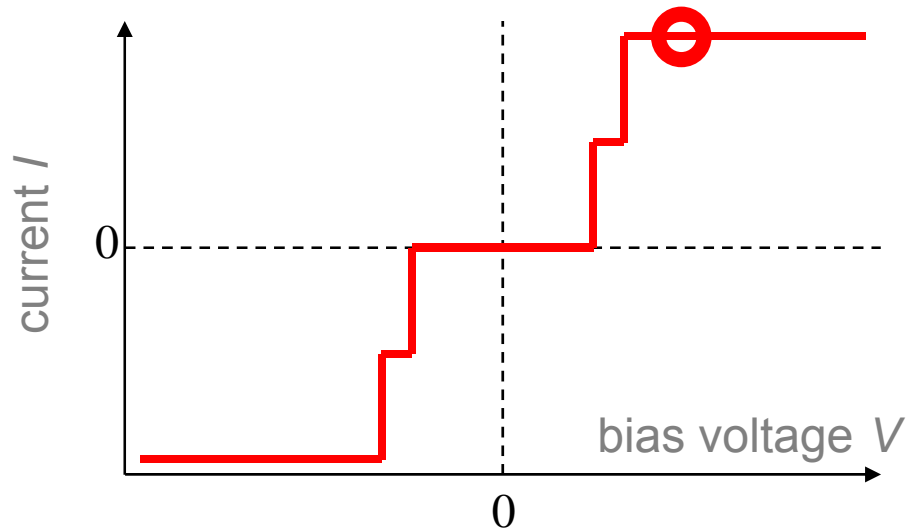
Coulomb blockade

Generic behavior described by rate equations



tunneling

Generic behavior described by rate equations

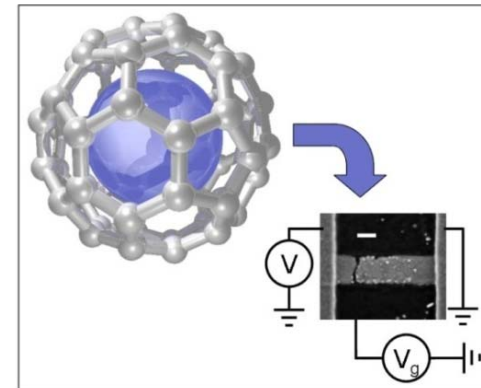
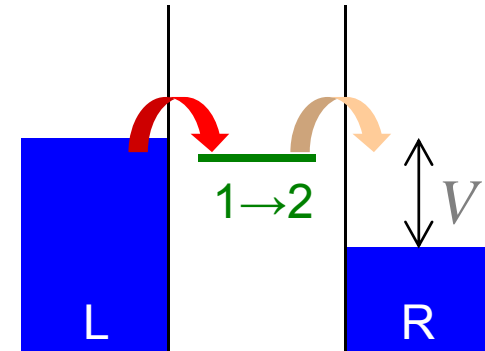


inelastic tunneling
 (vibration, spin flip)

characteristic for
 molecules

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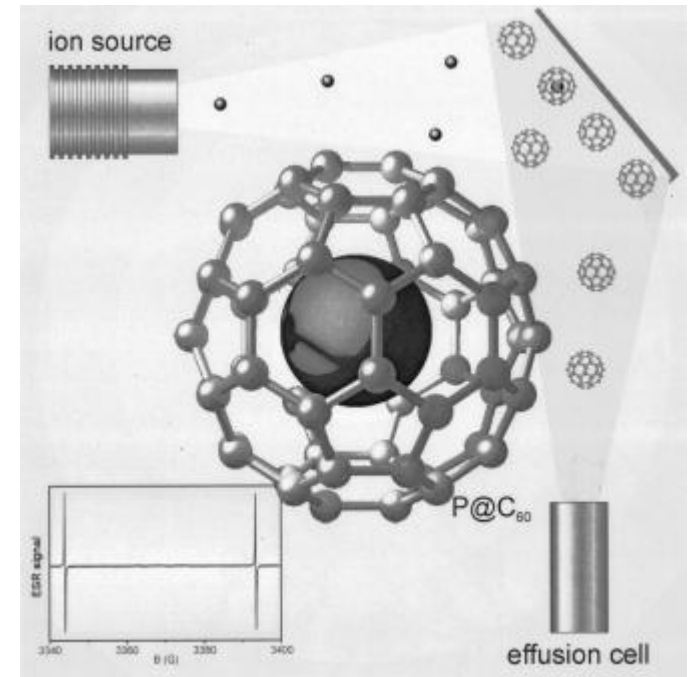


Endohedral $N@C_{60}$

- nitrogen atom located at center of C_{60}
- nitrogen retains **spin $S_N = 3/2$** (Hund's 1st rule)

production by Harneit group (FU Berlin) using

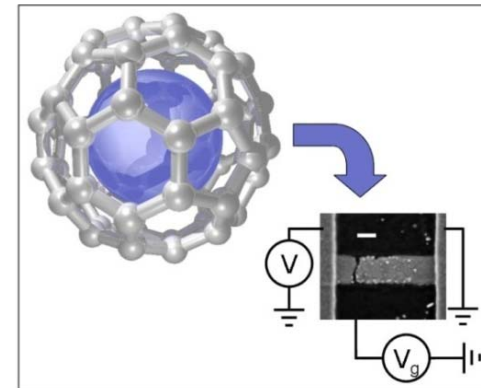
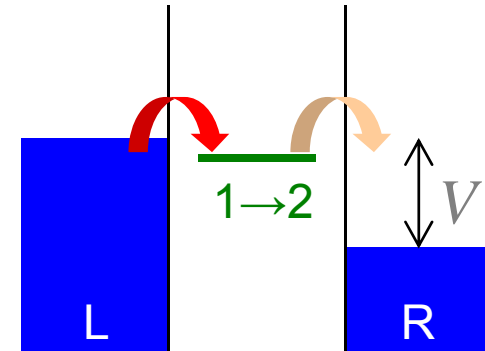
- ion implantation
- enrichment / mass separation



Larsson *et al.*, J. Chem. Phys. **116**, 7849 (2002)
(shown for phosphorus)

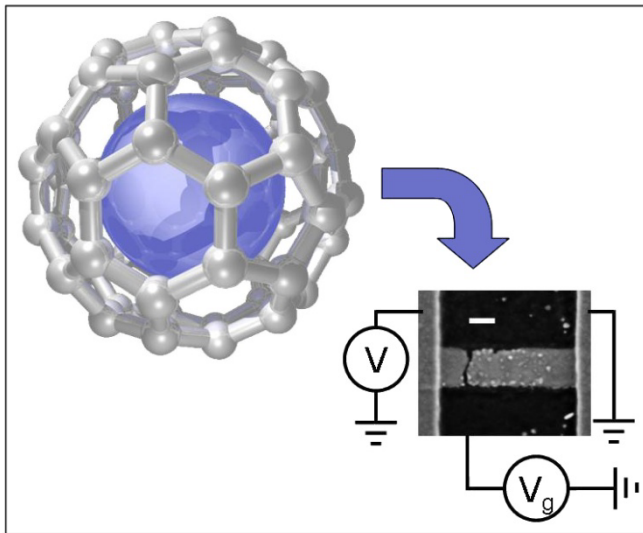
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Motivation: Hope to observe **inelastic tunneling due to coupling to molecular spin**

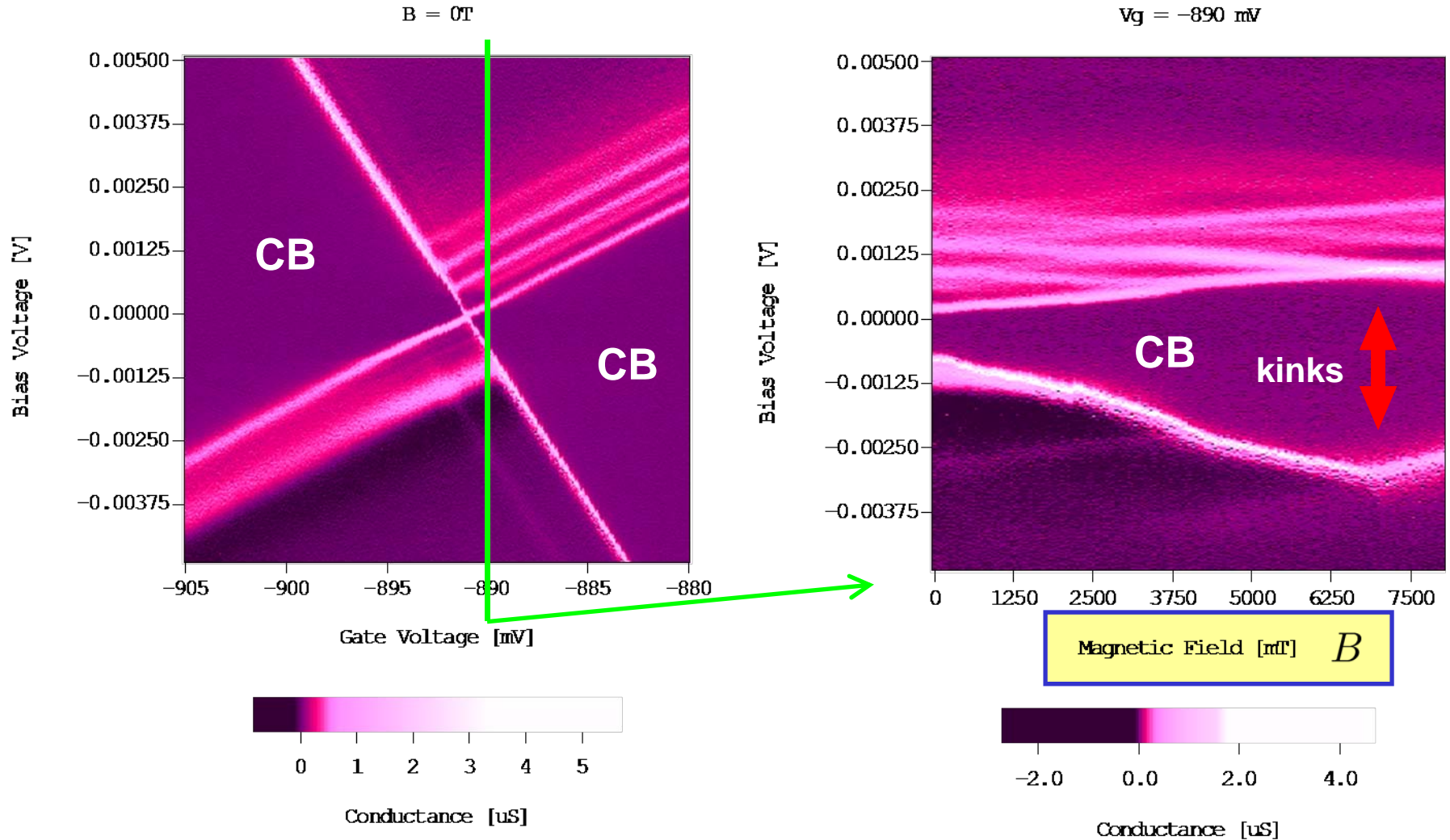
earlier calculations by F. Elste and C.T., PRB **71**, 155403 (2005)

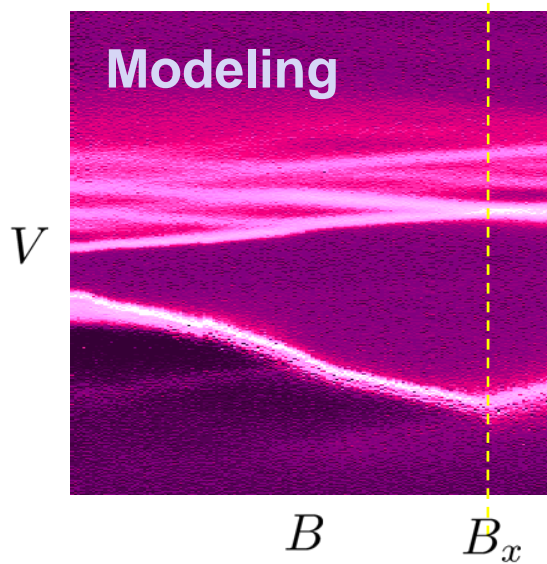


N@C₆₀ in Pt break junctions
(Ralph group, Cornell university)

J. E. Grose, E. Tam, C.T., M. Scheloske, B. Ulgut, J. J. Parks, H. D. Abruña, W. Harneit, and D. C. Ralph, Nature Materials **7**, 884 (2008)

Differential conductance: experiment



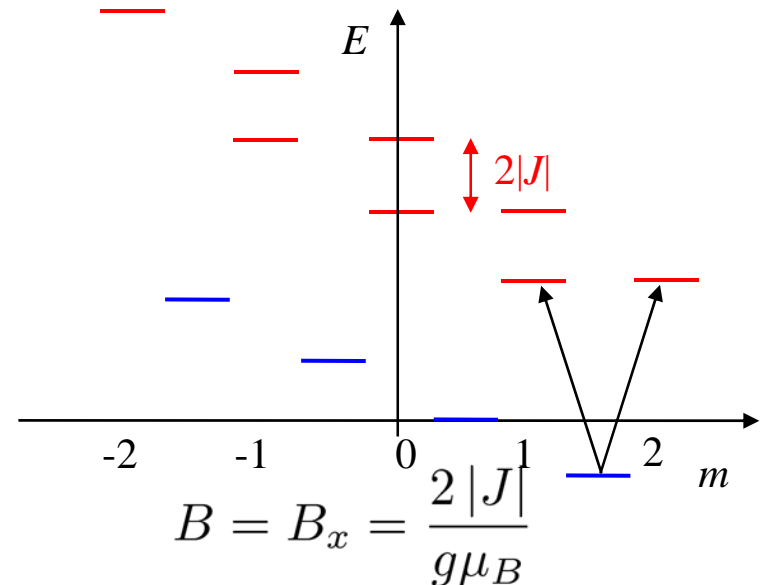
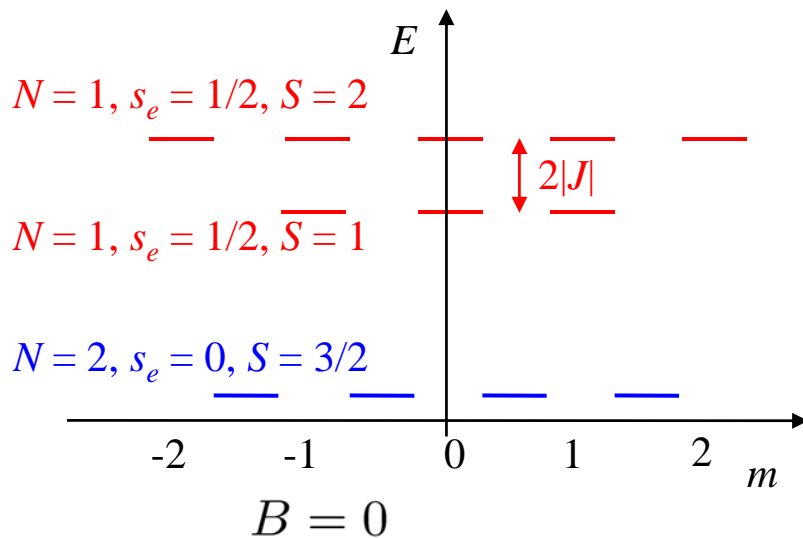


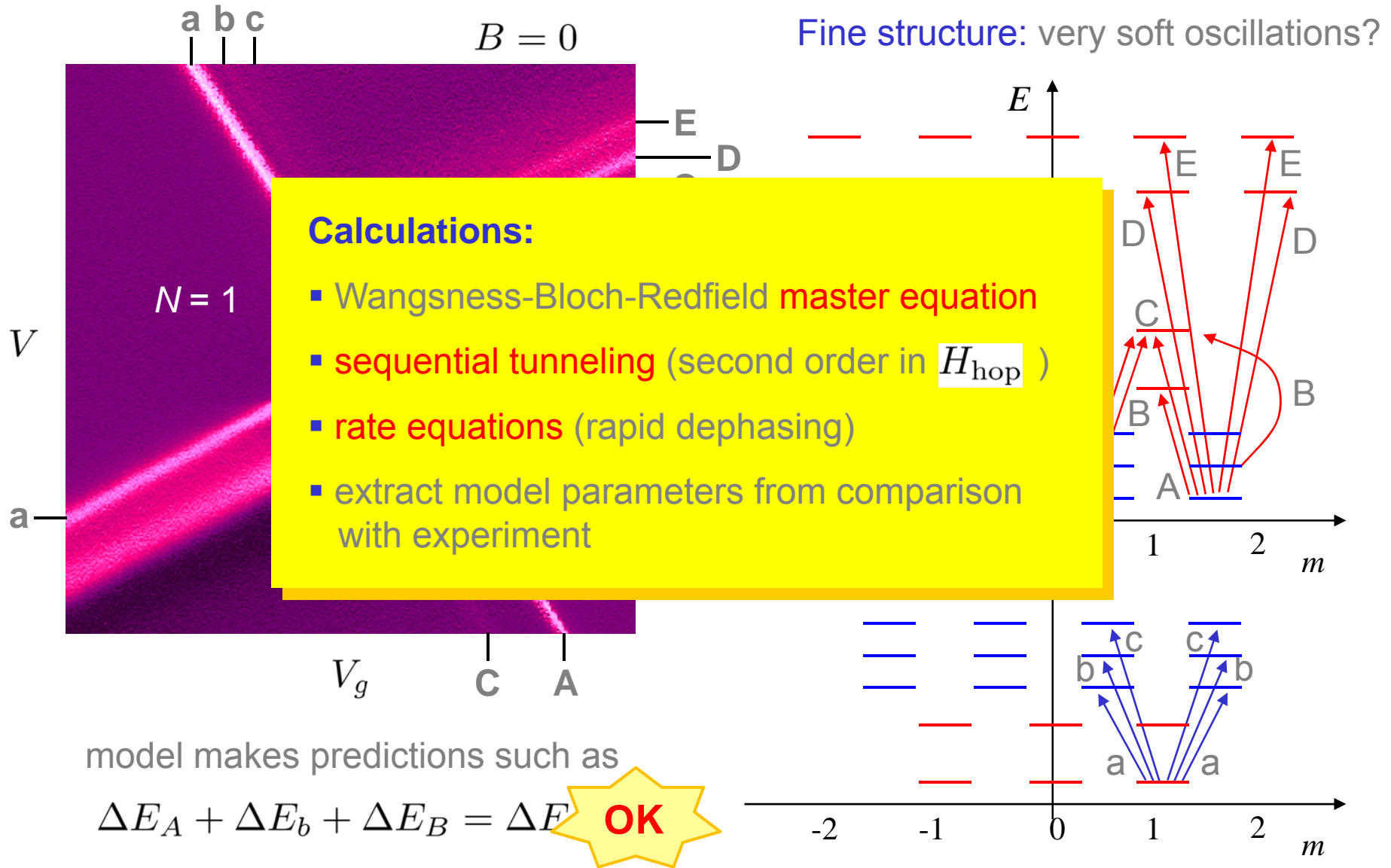
$$H_{\text{dot, el}} = (\epsilon - eV_g^*) \sum_{\sigma} a_{\sigma}^{\dagger} a_{\sigma} + U a_{\uparrow}^{\dagger} a_{\uparrow} a_{\downarrow}^{\dagger} a_{\downarrow} - J \mathbf{s}_e \cdot \mathbf{S}_N - g\mu_B B (s_e^z + S_N^z)$$

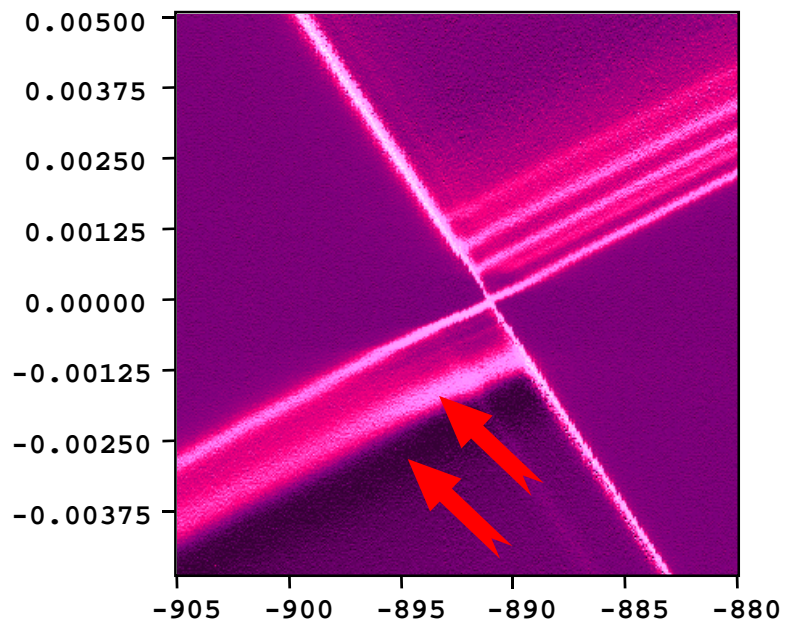
$V_g^* = \alpha V_g + \beta_L V$: local potential (asym. coupling)

U : Coulomb repulsion on C_{60}

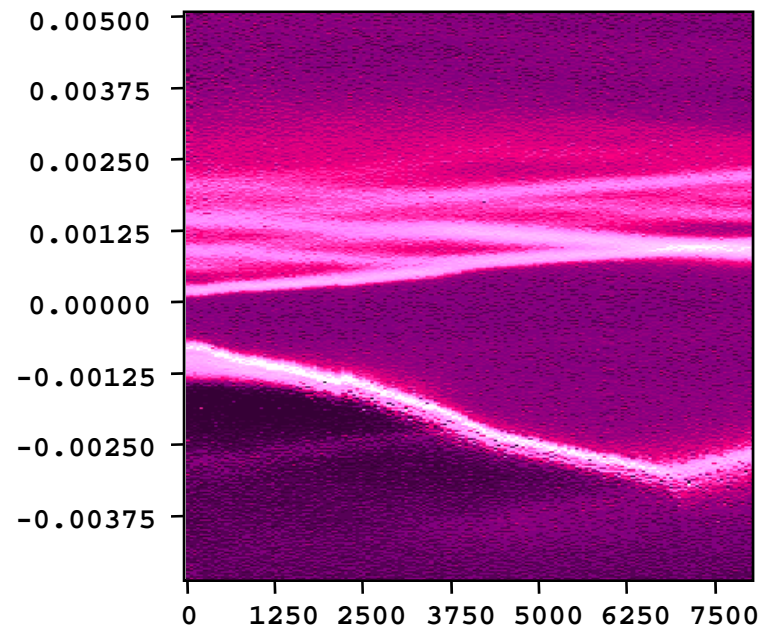
$J < 0$: exchange between electron and N spin



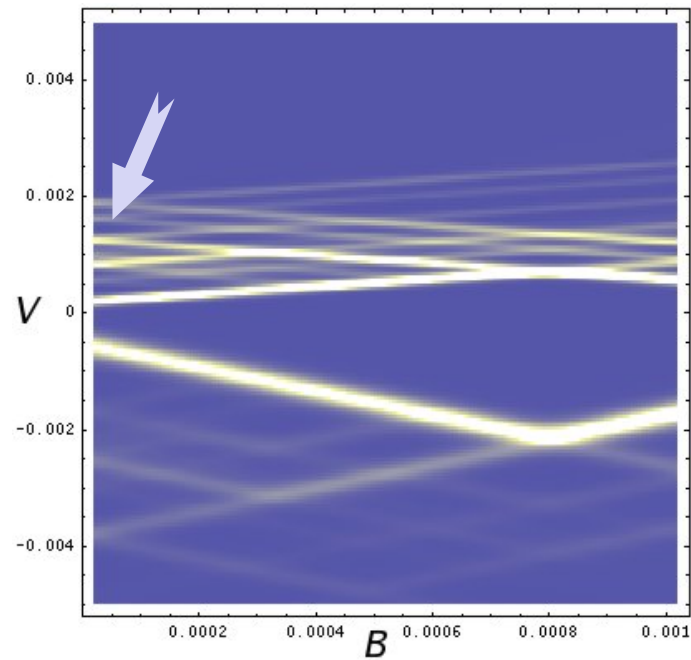
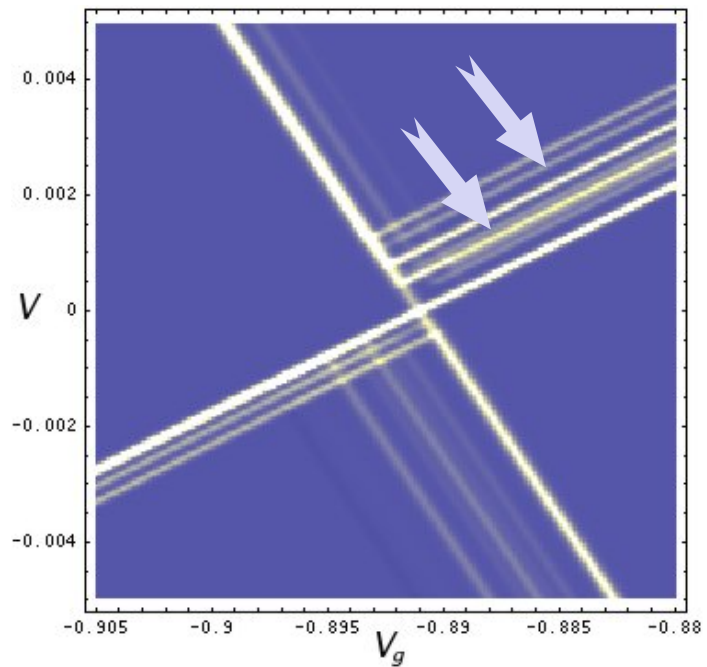




experiment



theory



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Acknowledgements

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