

Electron delocalisation and weak interactions: Implications to chemistry, material sciences and physics

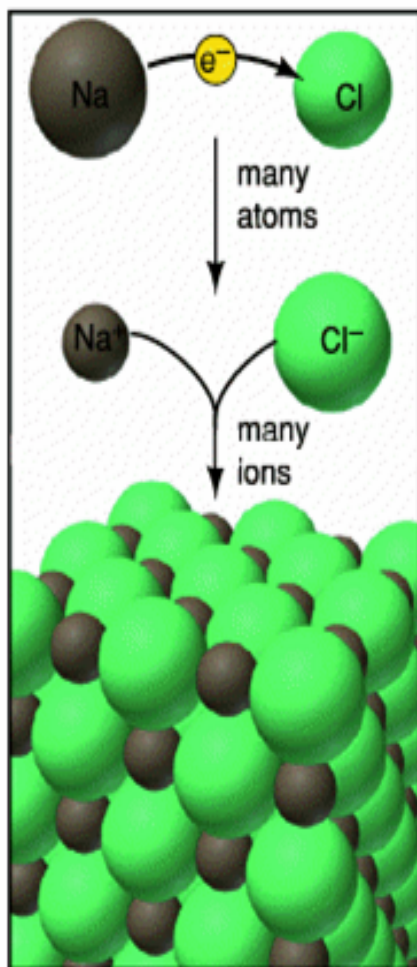
Thomas Heine

Email: thomas.heine@chemie.tu-dresden.de



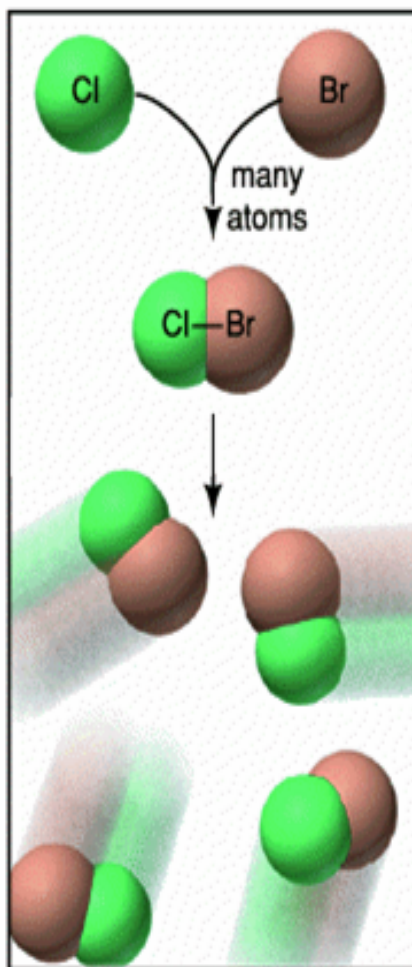


Bonding types in chemistry



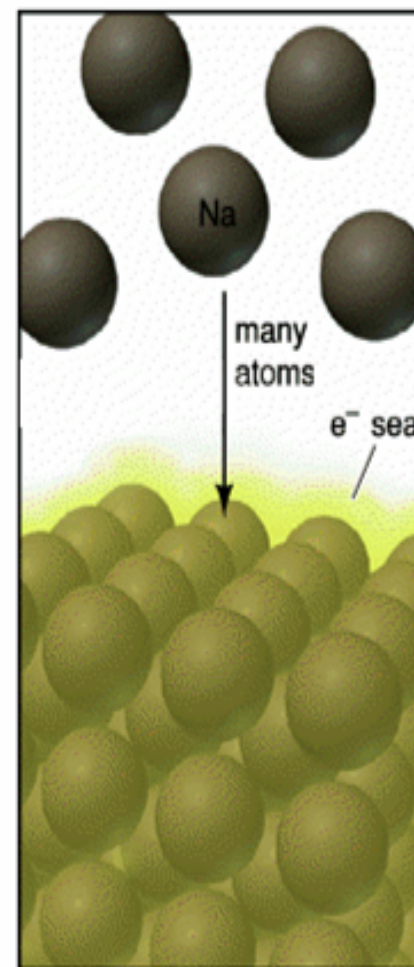
A Ionic bonding

displaced electrons



B Covalent bonding

localised electrons



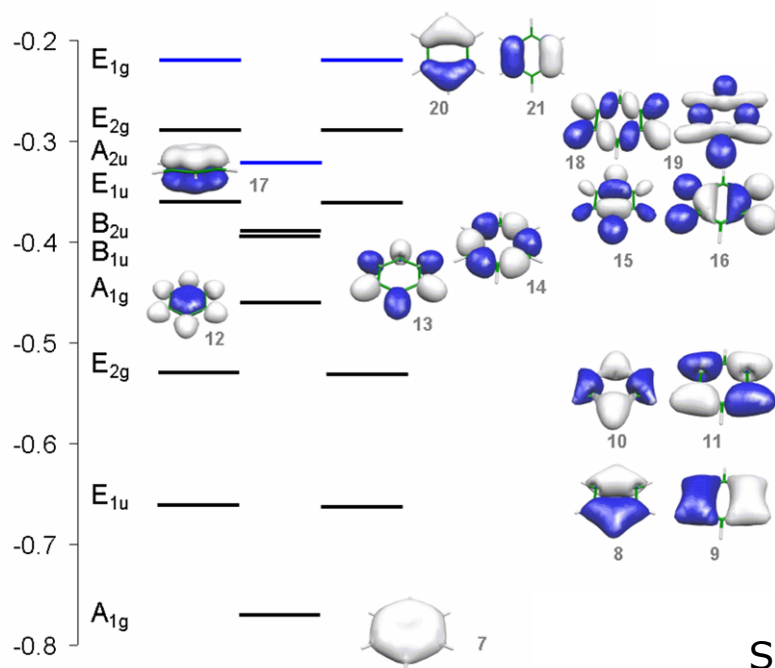
C Metallic bonding

delocalised electrons

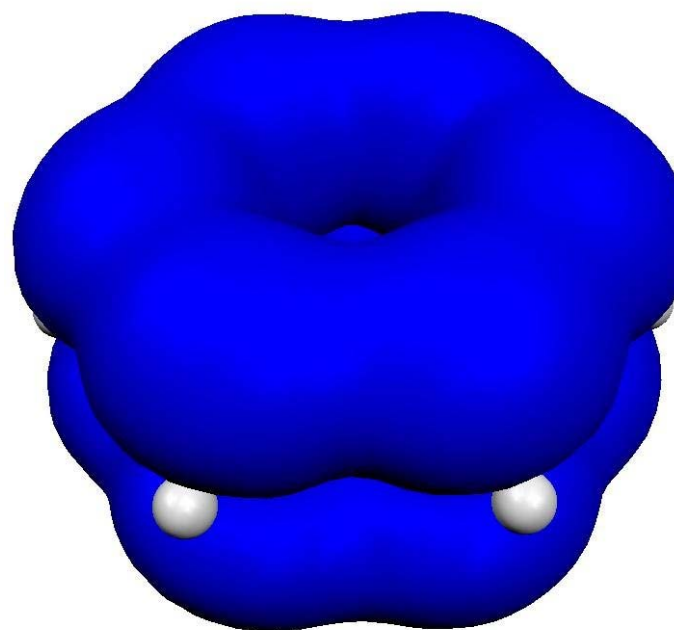


What about aromatic molecules

Molecular Orbitals of benzene



The ELF clearly shows delocalised clouds of π electrons



Santos, J. C.; Tiznado, W.; Contreras, R.; Fuentealba, P. J. Chem. Phys. 2004, 120, 1670.

For Review:

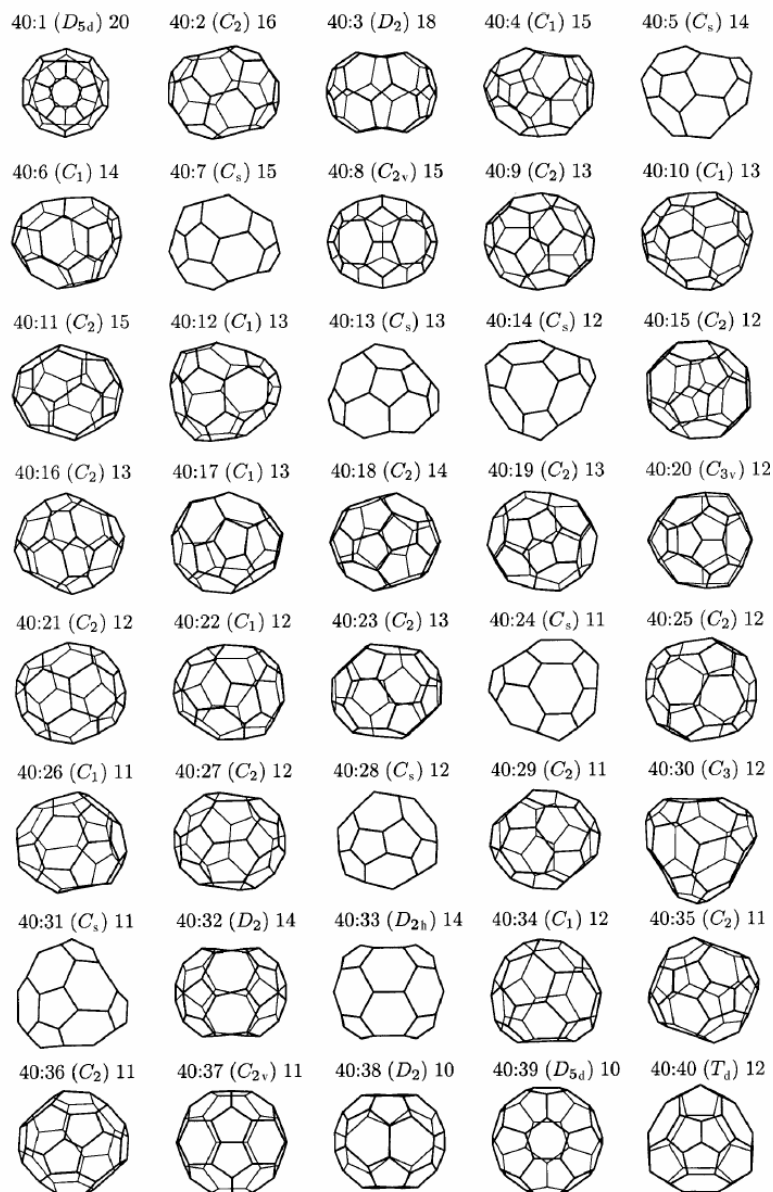
Chem. Rev. 2005, 105, 3889-3910

Chem. Rev. 2005, 105, 3812-3841

Email: thomas.heine@chemie.tu-dresden.de



Pi system determines stability of sp^2 carbon structures



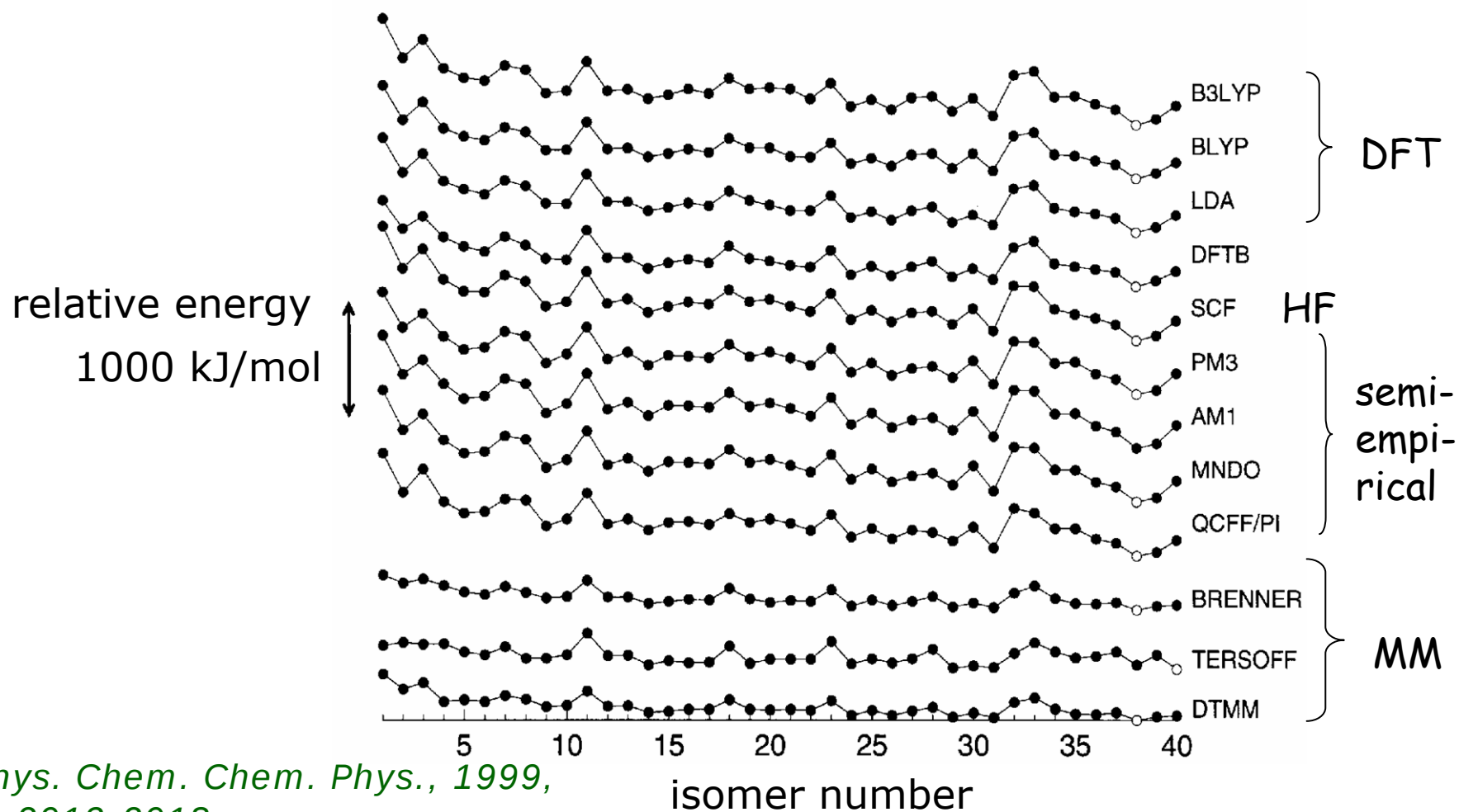
Fullerene isomers of C_{40}

- Contain 10-20 fused pentagons
- Nomenclature, (point group), number of pentagon adjacencies

Phys. Chem. Chem. Phys., 1999, 1, 2913-2918



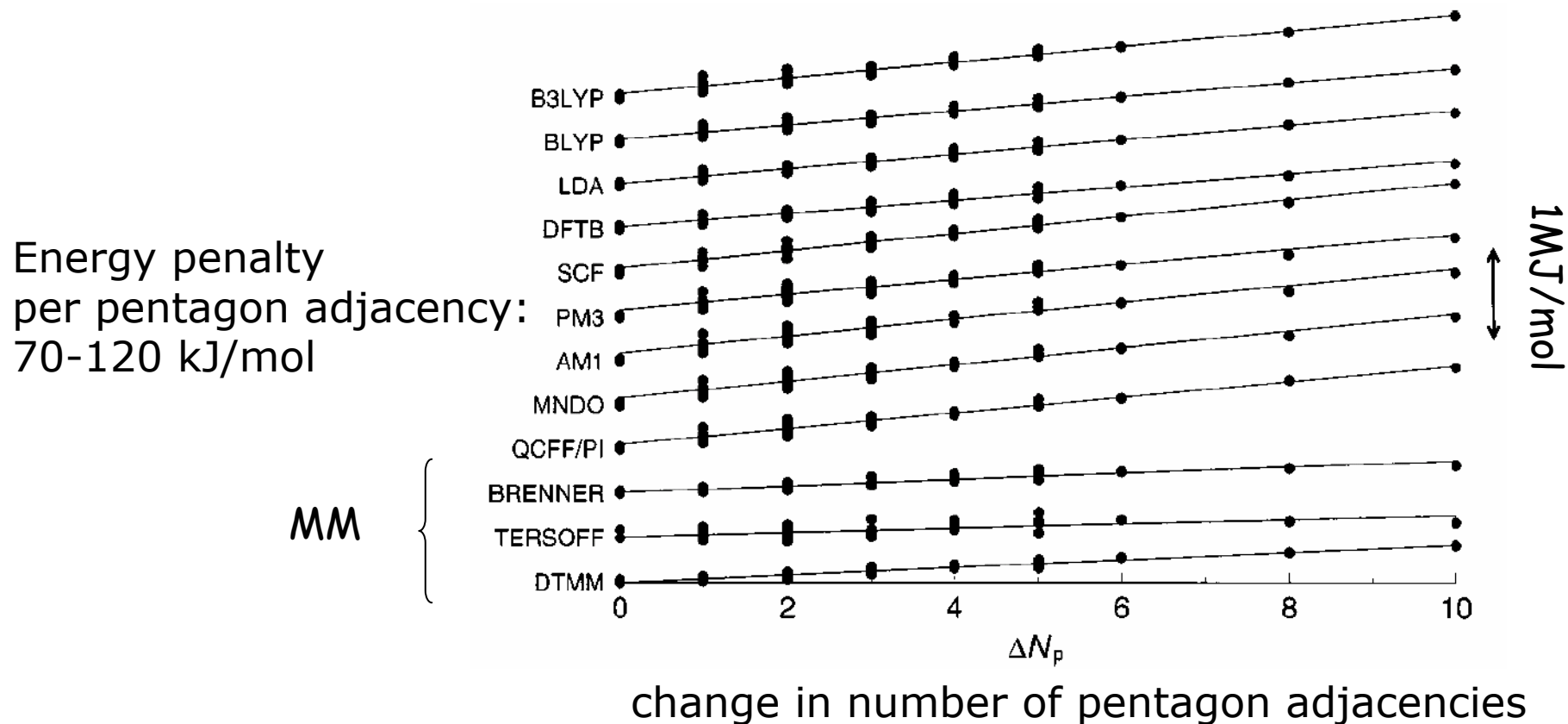
Relative energies of C₄₀



Phys. Chem. Chem. Phys., 1999,
1, 2913-2918



Rule of minimal number of pentagon adjacencies



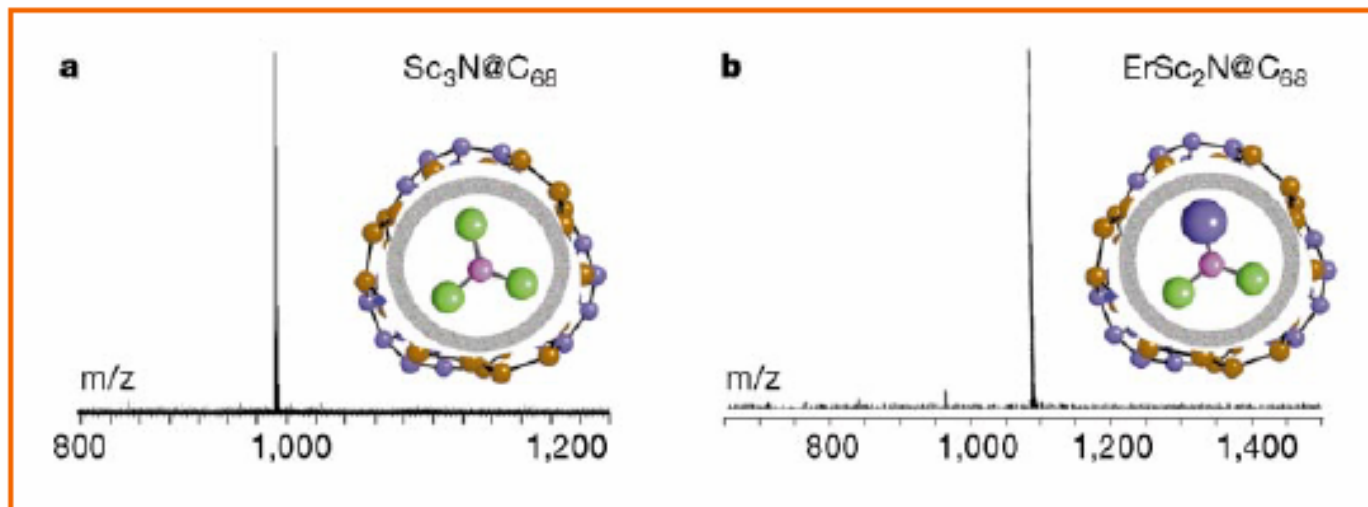
Phys. Chem. Chem. Phys.,
1999, 1, 2913-2918

Pi system determines stability!



$\text{Sc}_3\text{N}@C_{68}$: The first fullerene with adjacent pentagons

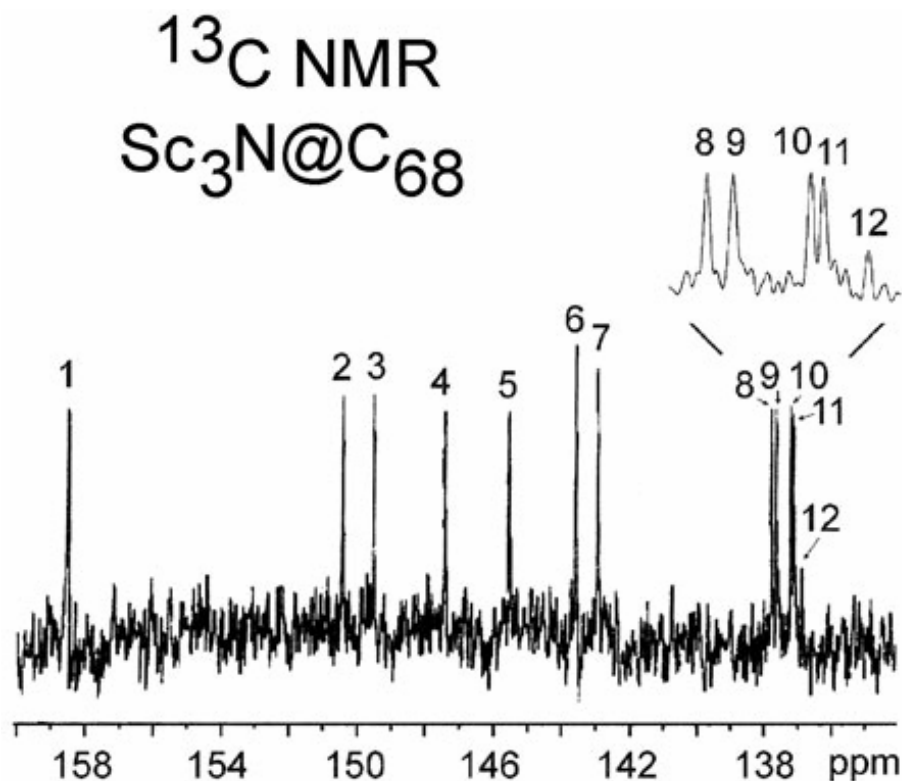
- mass spectrum: $\text{Sc}_3\text{N}@C_{68}$
- graph theory: C_{68} must have adjacent pentagons
- earlier calculations: adjacent pentagons energetically unfavoured
- assumption: stabilisation by endohedral Sc_3N molecule



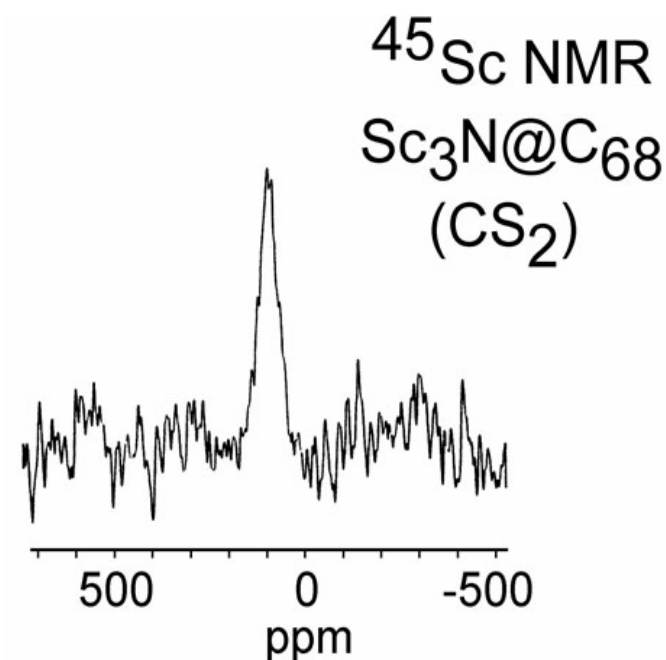
Nature 408 (2000) 427-428



^{13}C and ^{45}Sc NMR gives information on symmetry



Nature 408 (2000) 427-428



Graph theory: **11 isomers**
(point groups D_3 and S_6) out
of 6332 are compatible with
one ^{45}Sc and 11+1 ^{13}C signals

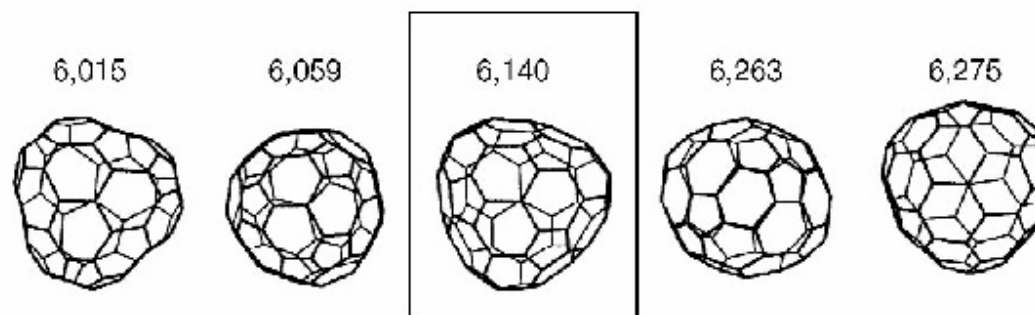
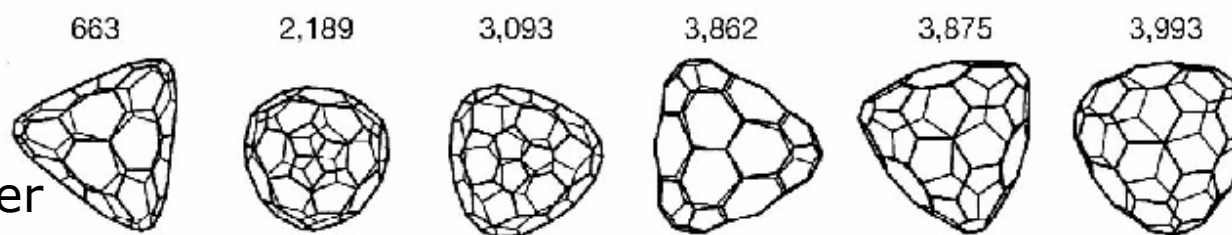


Which $\text{Sc}_3\text{N}@C_{68}$ isomer has been found?

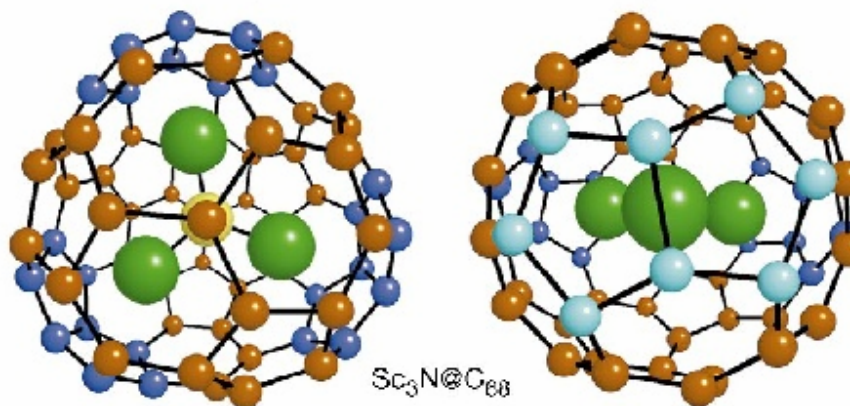
- minimum number of pentagon adjacencies: 6140 and 6275.

- 6140 is 120 kJ/mol more stable than all other isomers.

- Added excess electrons (2, 4, 6) to simulate charge transfer increase the energy gap

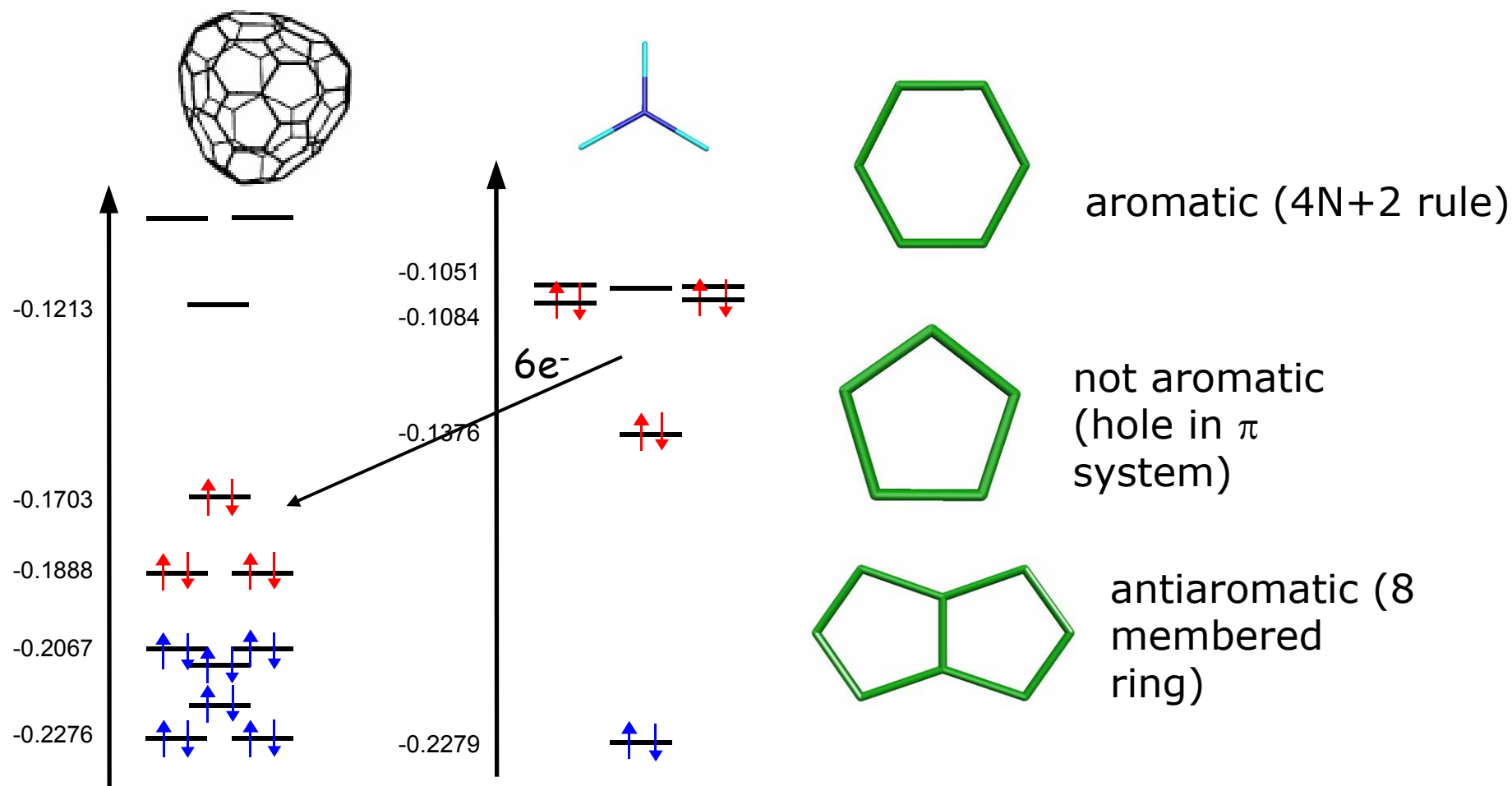


*Nature 408 (2000)
427-428*





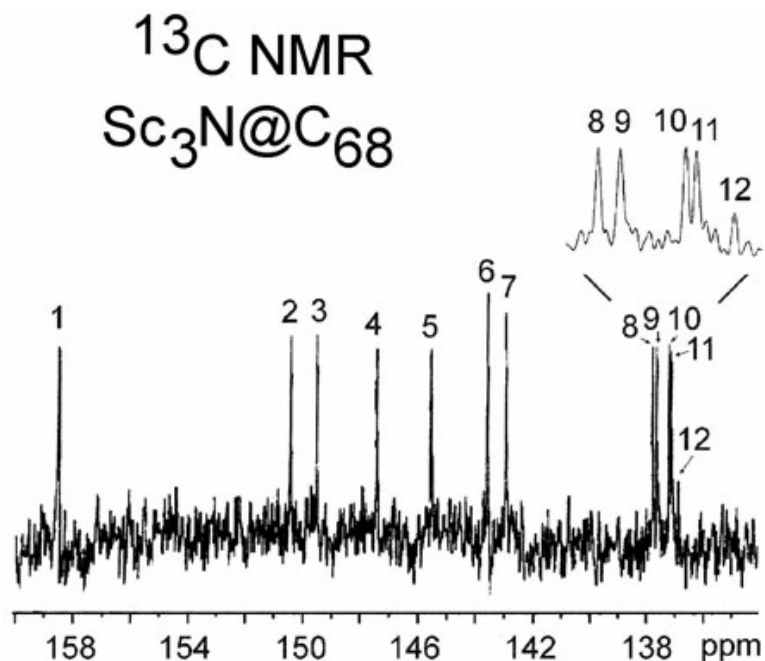
Simple explanation using Hückel and MO theory



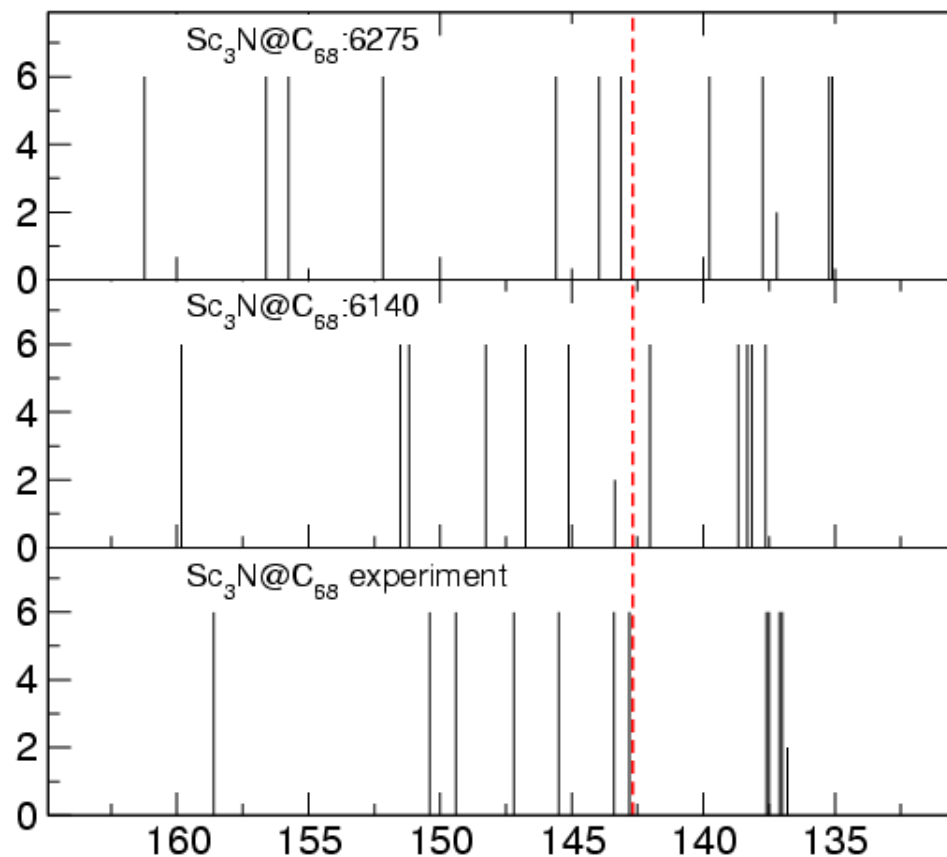
- $\text{Sc}_3\text{N}@C_{68}$: 3 adjacent pentagons connected to Sc
- ~ 2 electrons per adjacent pentagon $\rightarrow$
- **isoelectronic with 10 membered ring (aromatic)**



Confirmation by ^{13}C NMR fingerprint



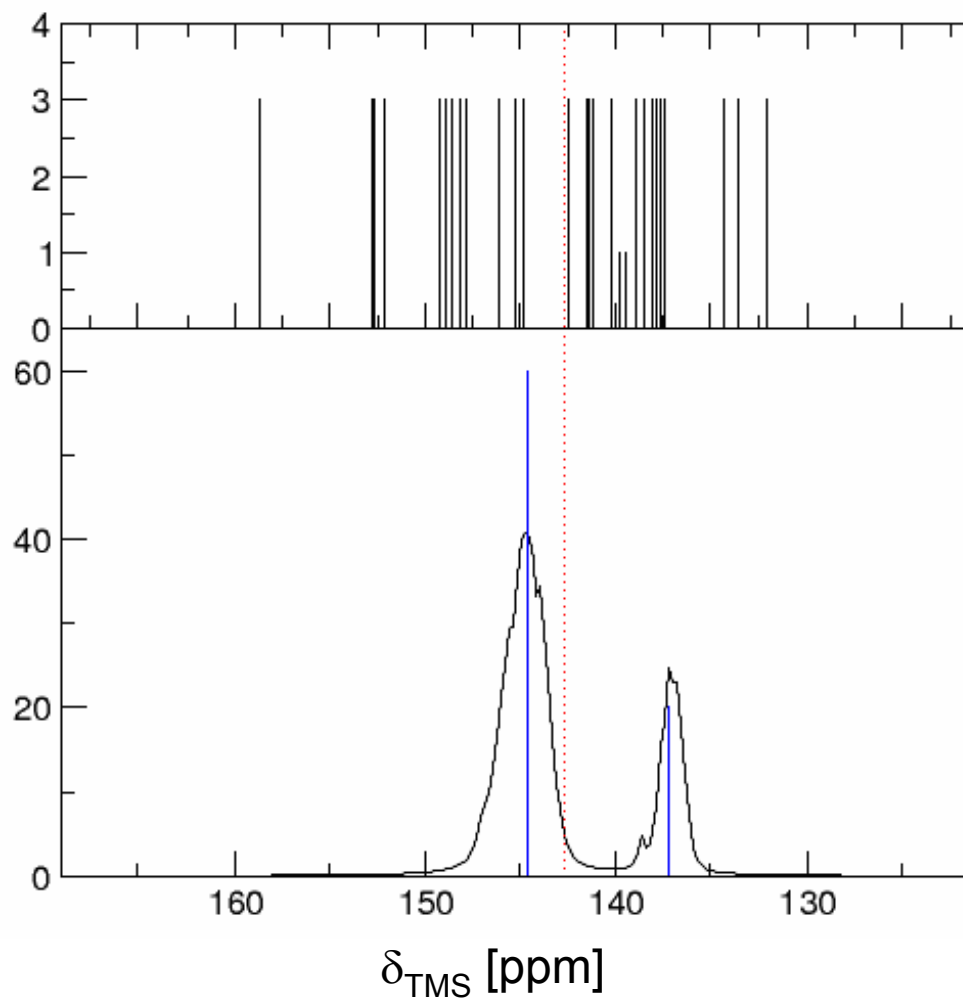
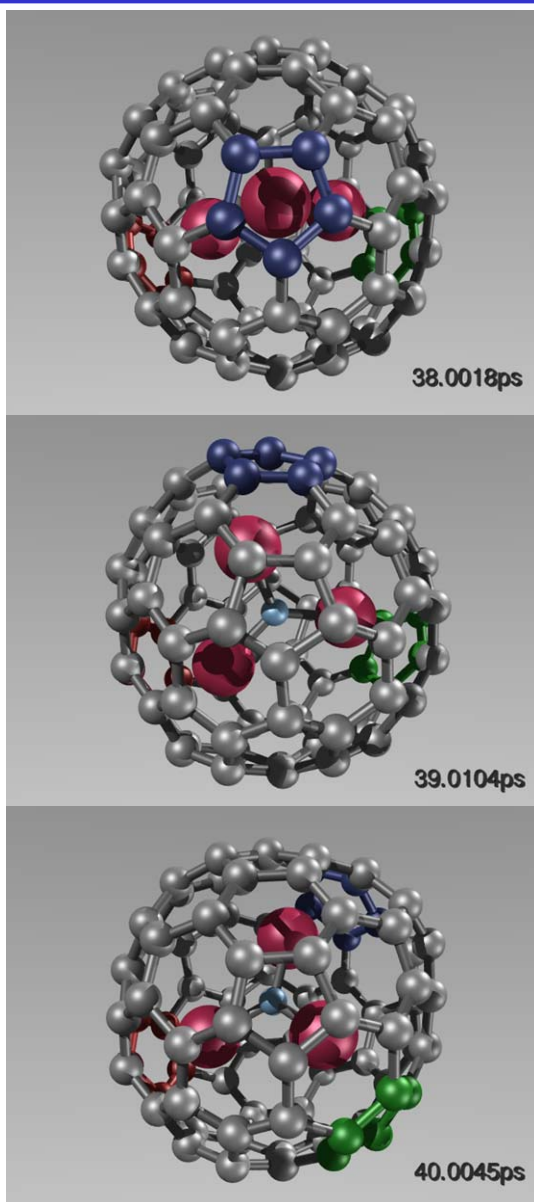
Nature 408 (2000) 427-428



J. Phys. Chem. A 2005, 109, 7068-7072



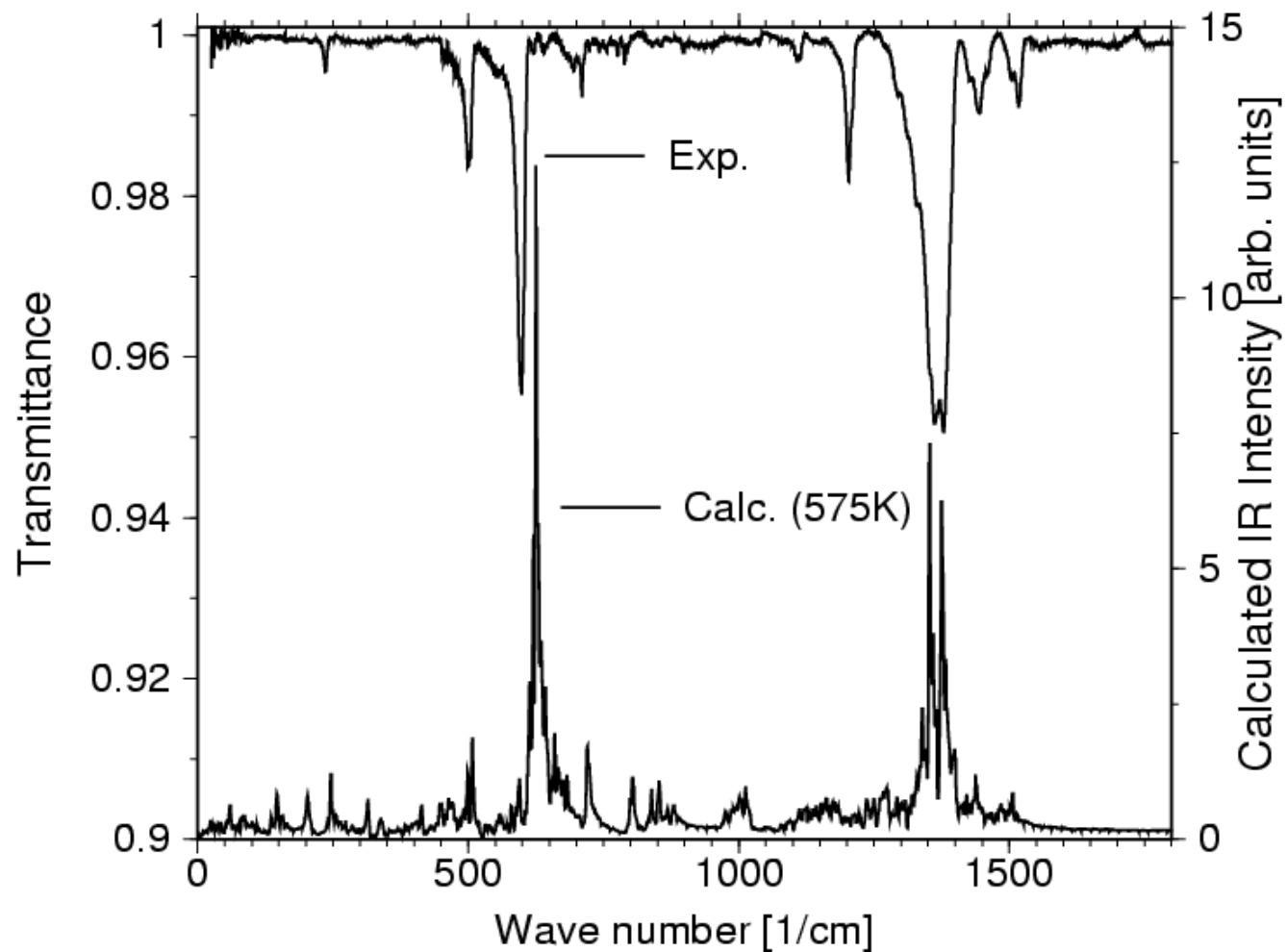
^{13}C NMR in $\text{Sc}_3\text{N}@C_{80}$



Magn. Res. Chem. 2004, 42,199



IR spectrum of $\text{Sc}_3\text{N@C}_{80}$



unpublished

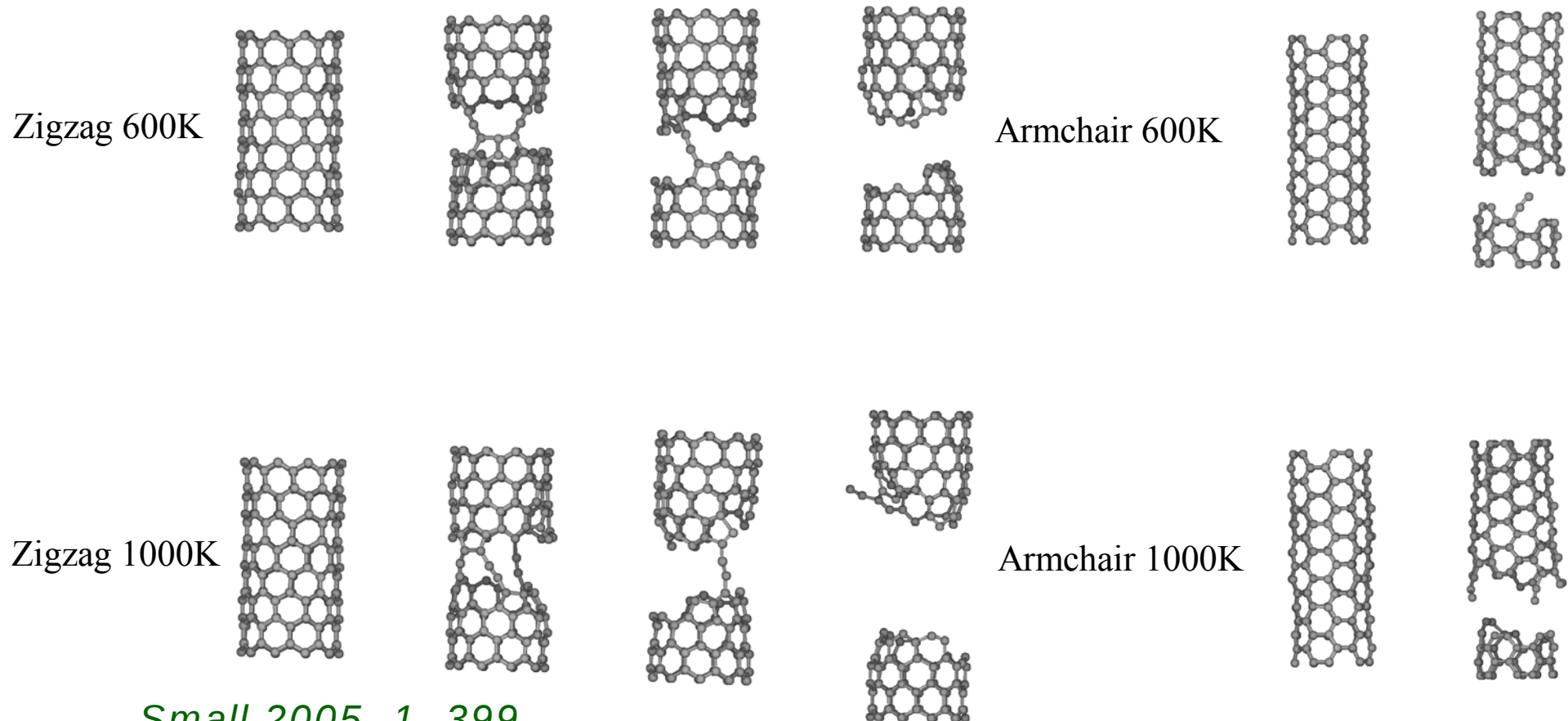


Mechanical and electromechanical properties of carbon and inorganic nanotubes



Electromechanical properties of single-walled carbon nanotubes

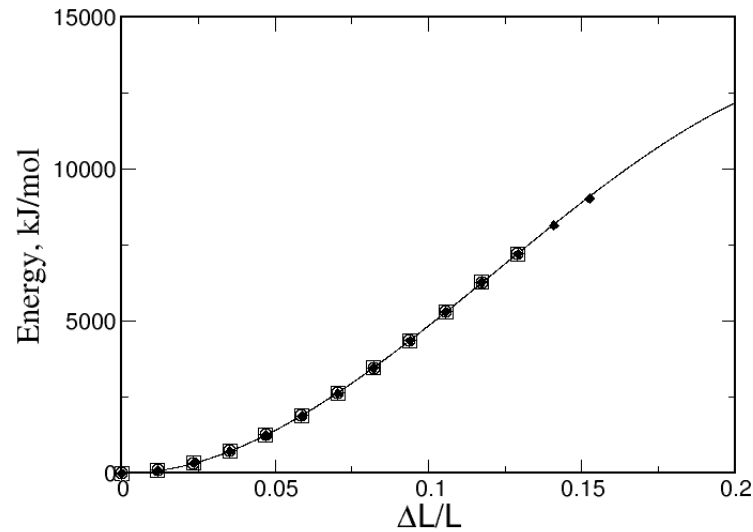
Rupture of CNTs at different temperatures: DFTB-based Born-Oppenheimer MD with successive iterations of pulling the tubes until rupture



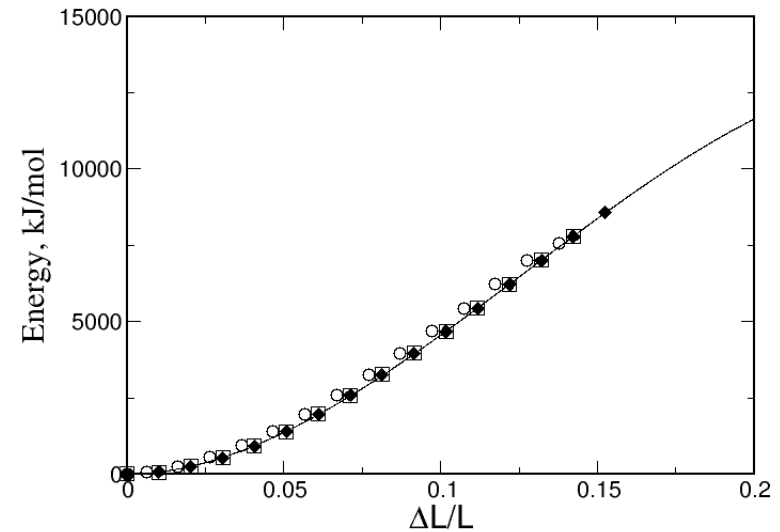
Small 2005, 1, 399



Elastic properties of SWCNT's



zigzag



armchair

300K: full circles
600K: squares
1000K: empty circles

- Independent on temperature
- Rupture at $\Delta L/L \approx 0.15$
- Hooke-like behaviour up to $\Delta L/L \approx 0.1$

Small 2005, 1, 399



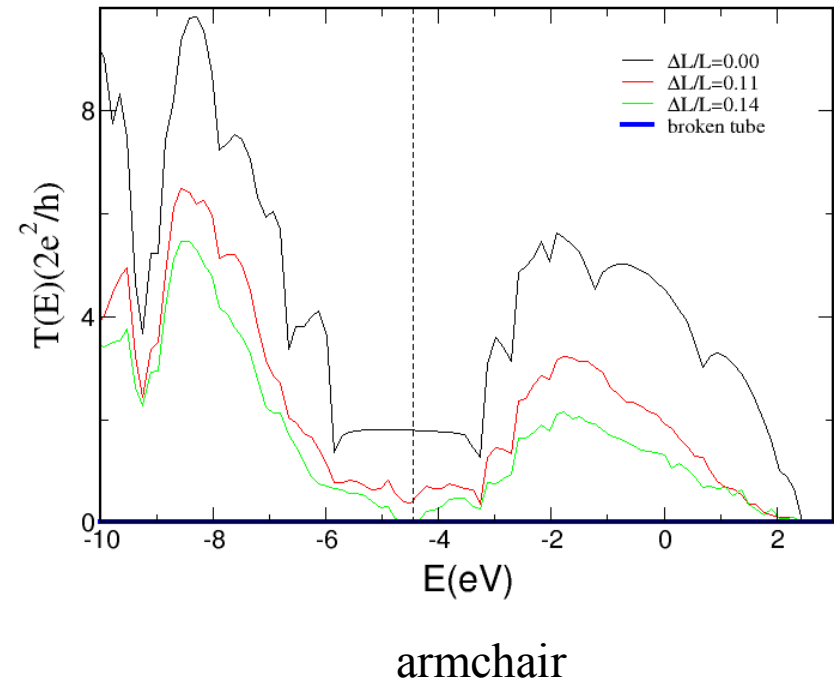
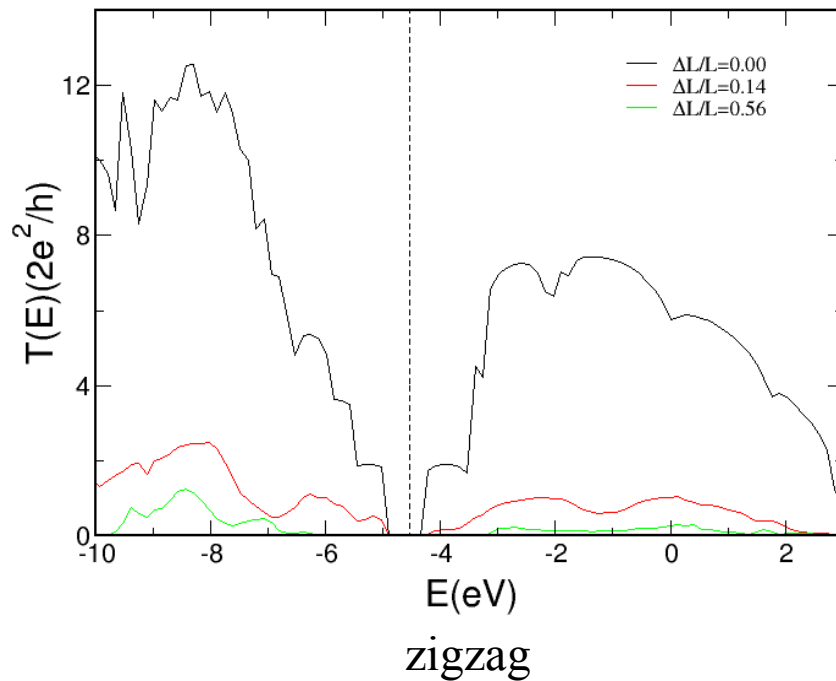
Mechanical properties of nanotubes



Thanks to Sibylle Gemming



Electromechanical properties of CNTs



Electronic transmission probability $T(E)$ depends strongly on $\Delta L/L$!

Small 2005, 1, 399

Email: thomas.heine@chemie.tu-dresden.de

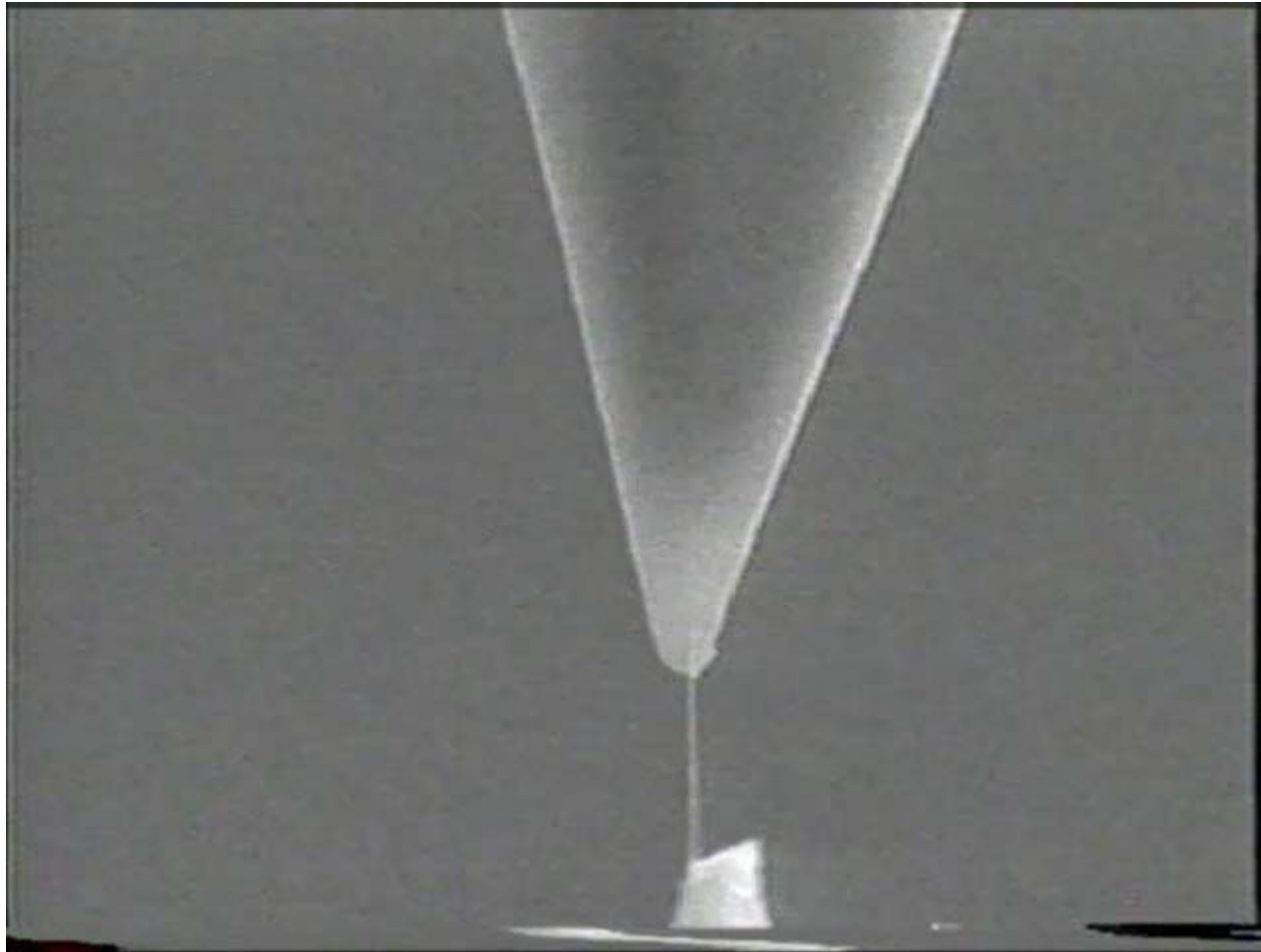


Axial tension of WS_2 and MoS_2 nanotubes

- In standard materials: mechanical properties are determined by defects (Griffith theory)
- Nanotubes: almost defect free $\rightarrow$ mechanical properties of almost ideal structure can be studied, and superior mechanical properties can be achieved
- Special structure of WS_2/MoS_2 particularly interesting regarding the axial tension



Mechanical properties of MoS₂ nanotubes - experiment



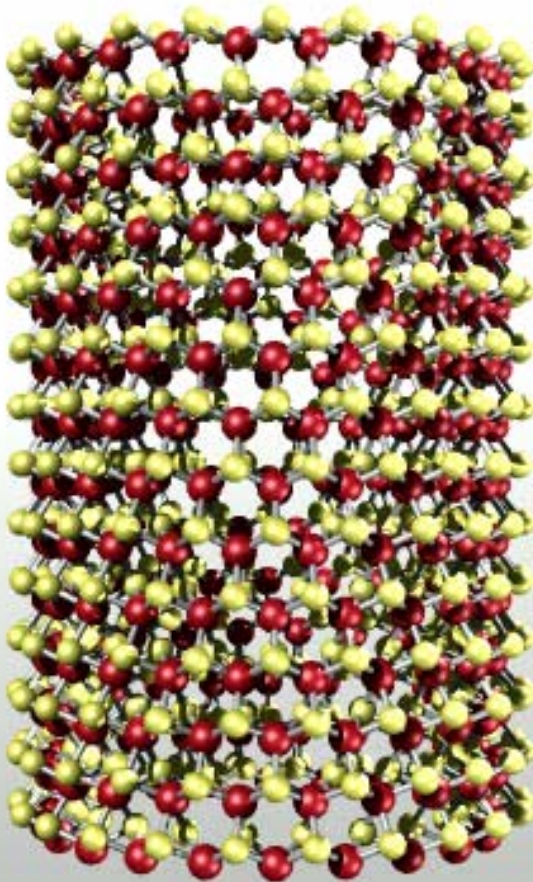
Breaking a WS₂ nanotube with an AFM, in-situ SEM

Proc. Natl. Acad. Sci. USA 2006, 103, 523.

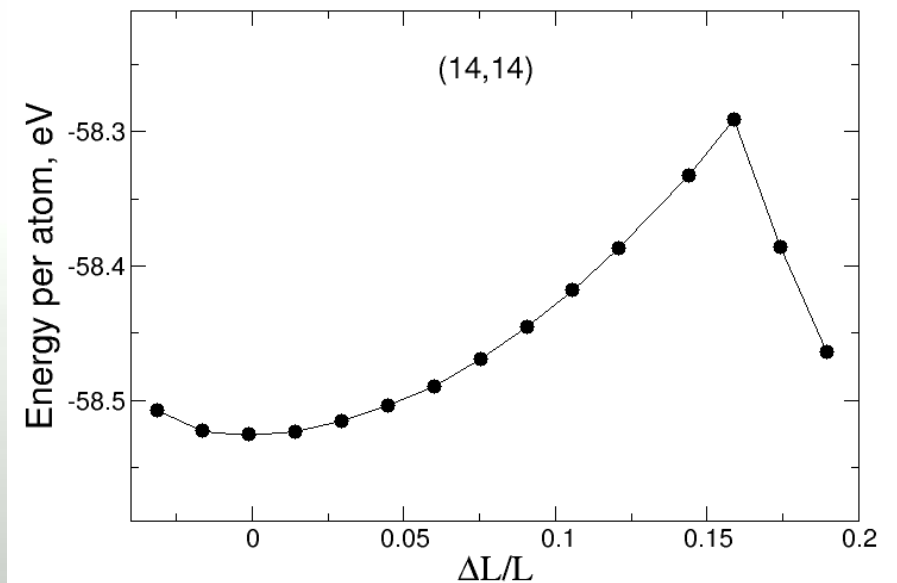
Email: thomas.heine@chemie.tu-dresden.de



Mechanical properties of MoS₂ nanotubes - simulation



Breaking a MoS₂ nanotube with an AFM

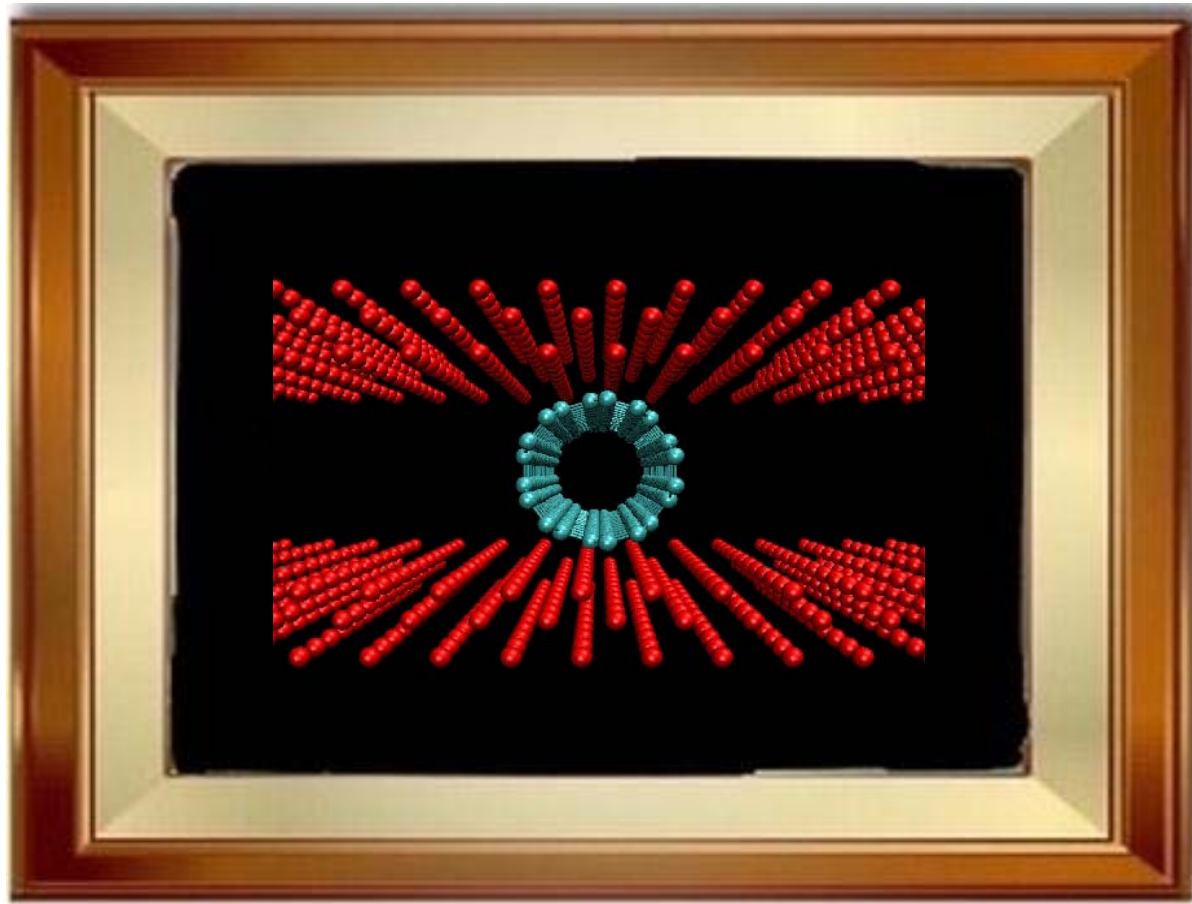


Almost harmonic behaviour until rupture!

Proc. Natl. Acad. Sci. USA 2006, 103, 523.



Squeezing nanotubes



*Molybdenum grips, MM,
fixed positions, van-der-
Waals forces to the NT*

*Nanotubes/Fullerenes:
DFTB (QM)*

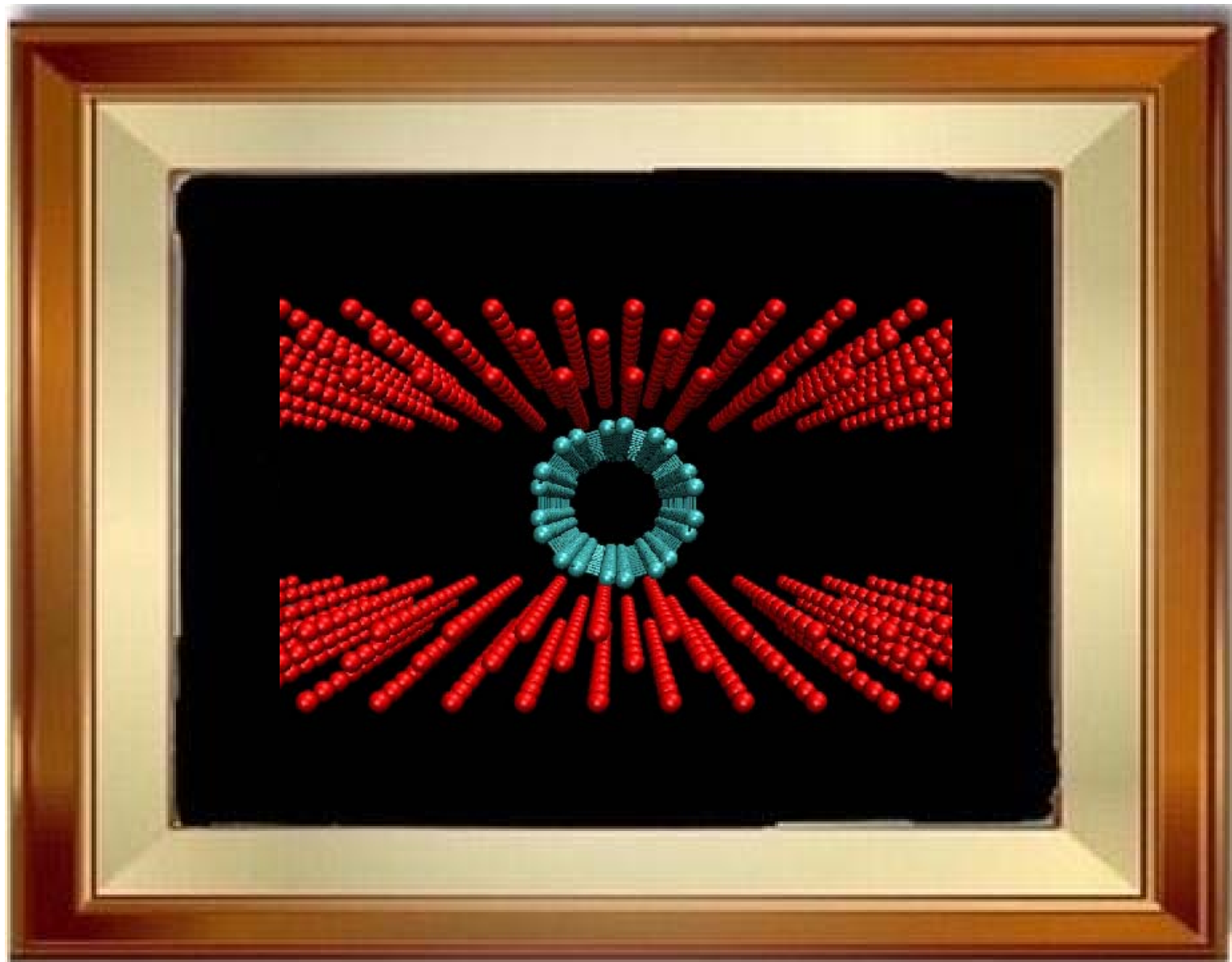
*Periodic boundary
conditions*

*Milen St. Stefanov Dobrev, Andrey Enyashin, G. Seifert, T. Heine,
to be published*

Email: thomas.heine@chemie.tu-dresden.de

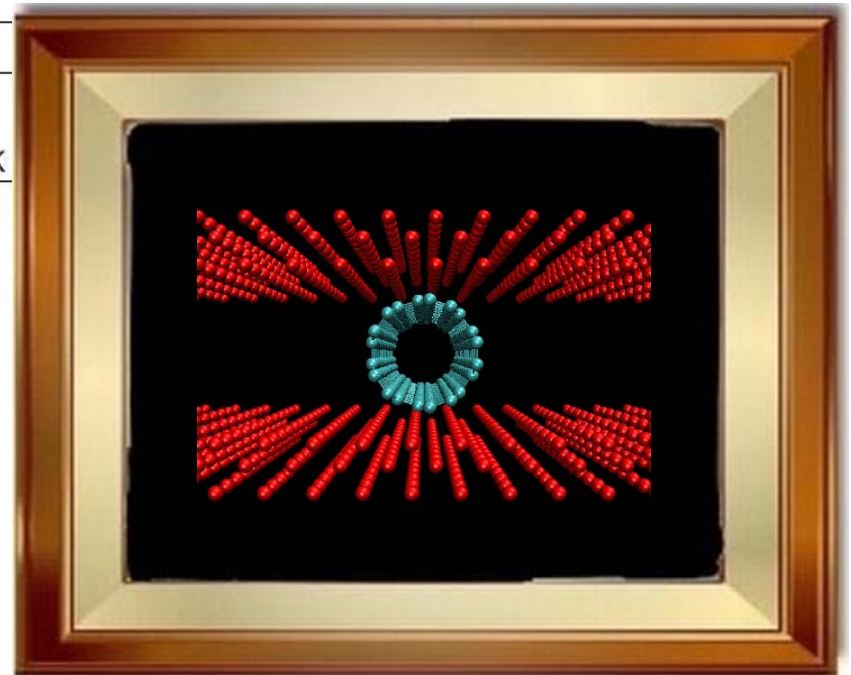
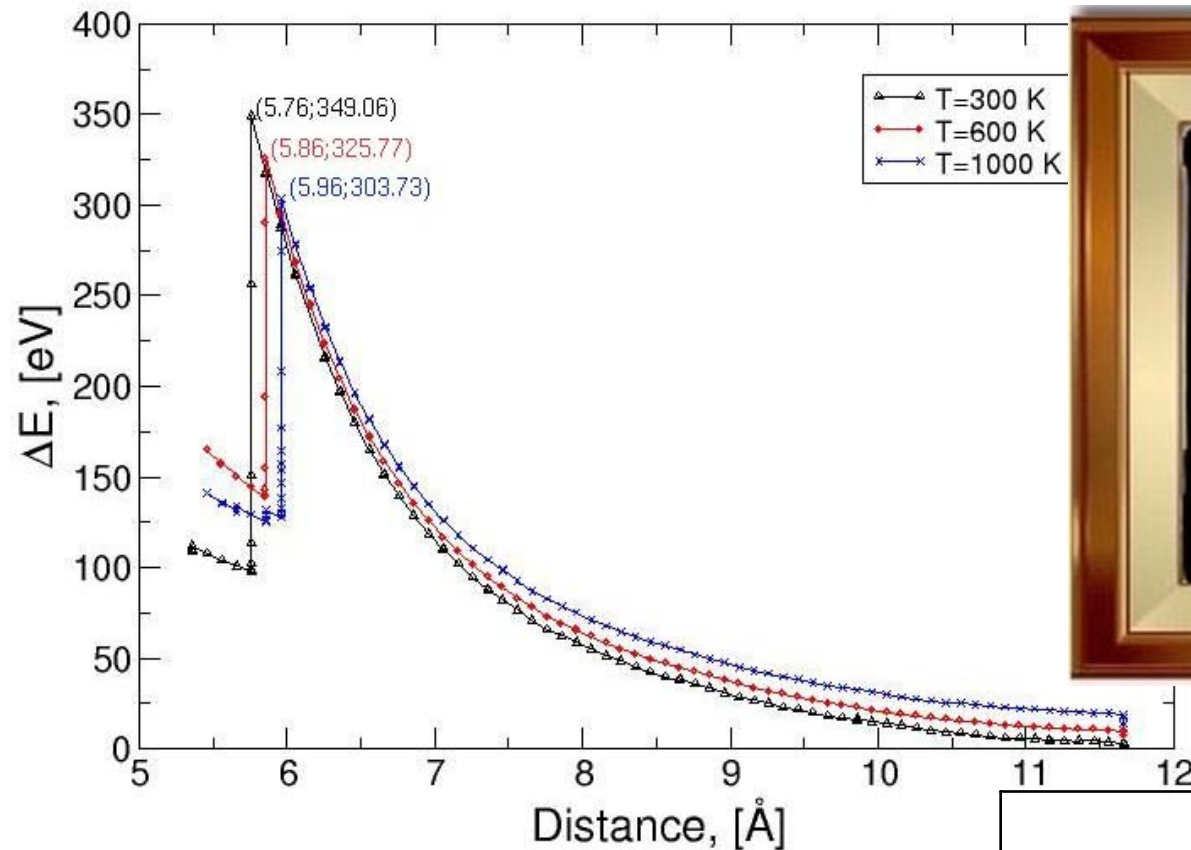


Squeezing Carbon Nanotubes





Elastic properties side-squeezed Nanotubes

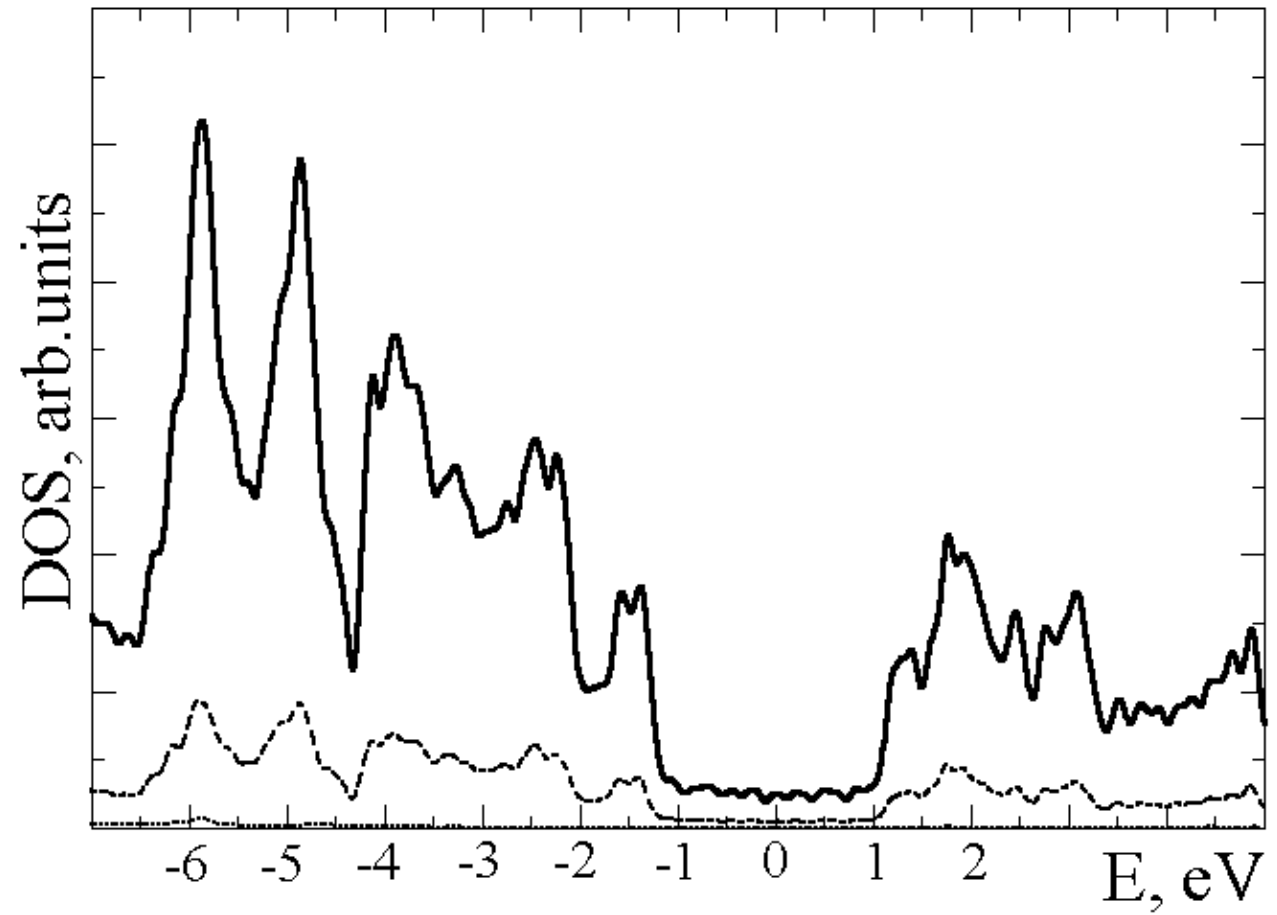
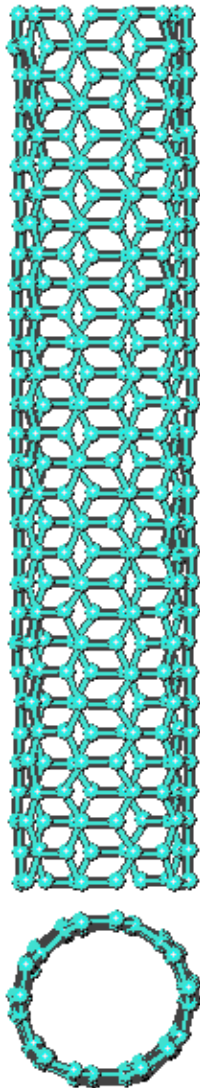


(5,5) CNT

	D_c , $\text{\AA}$	p_c , GPa	k , $\text{eV/\AA}^2$ ($\times 10^{-3}$)
300K	5.76	47.62	2.89
600K	5.86	46.38	3.23
1000K	5.96	38.61	3.47

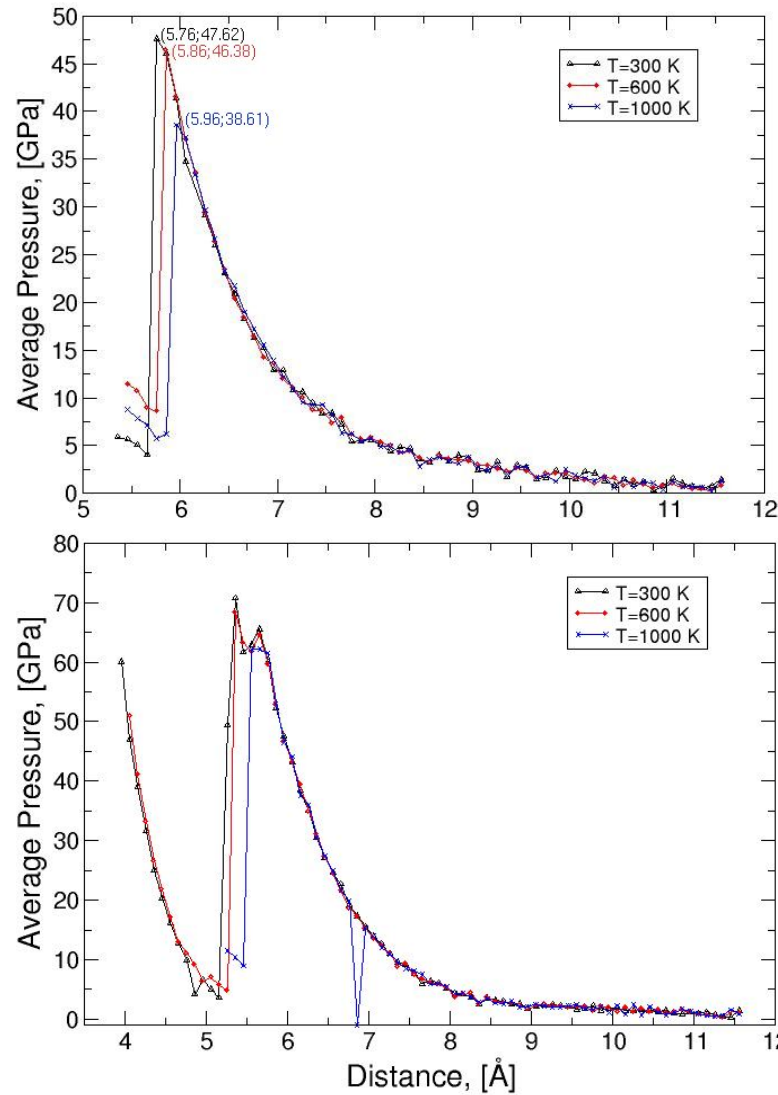


Influence on electronic properties of (5,5) CNT

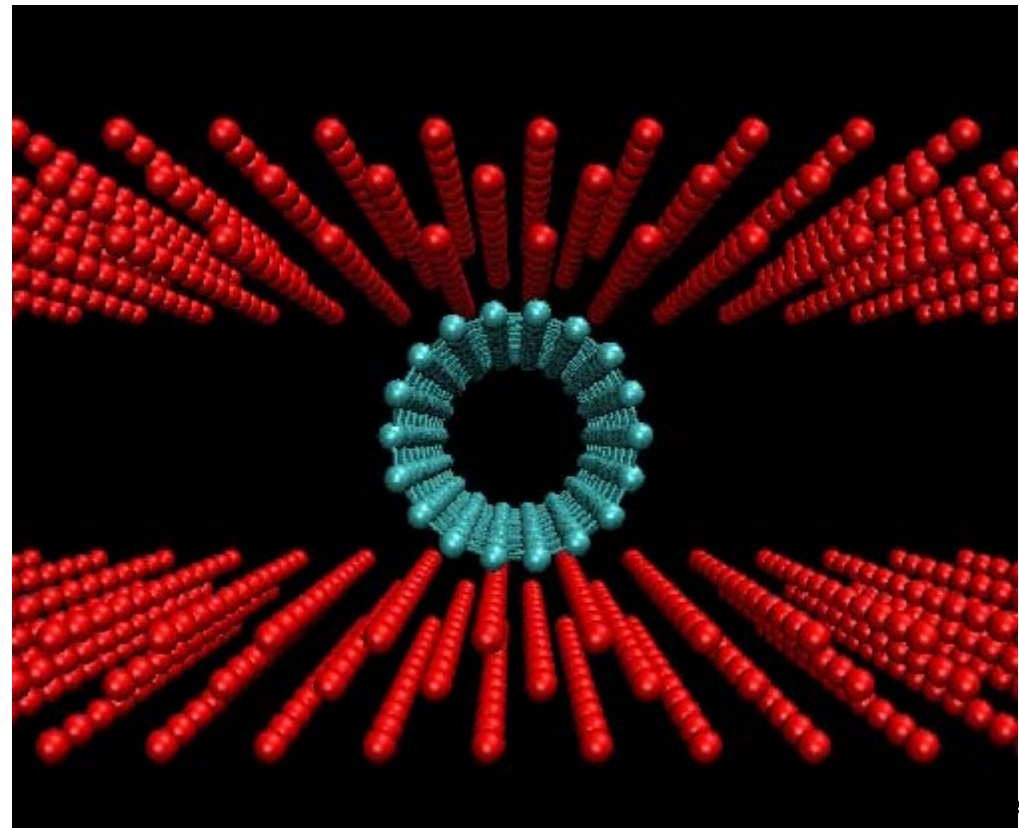




The (9,0) CNT is more stable than the (5,5) CNT

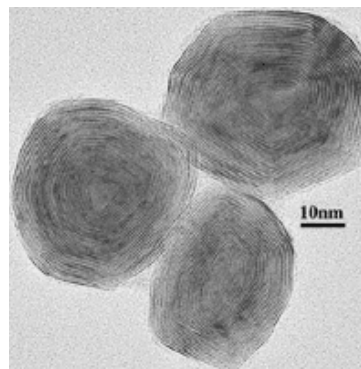
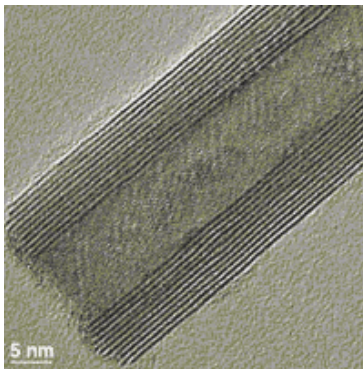
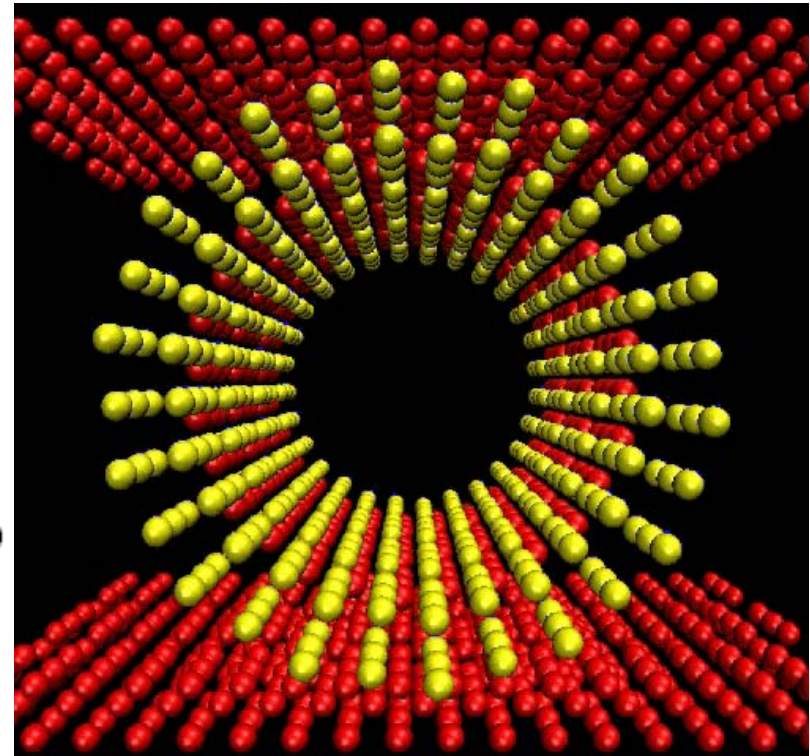
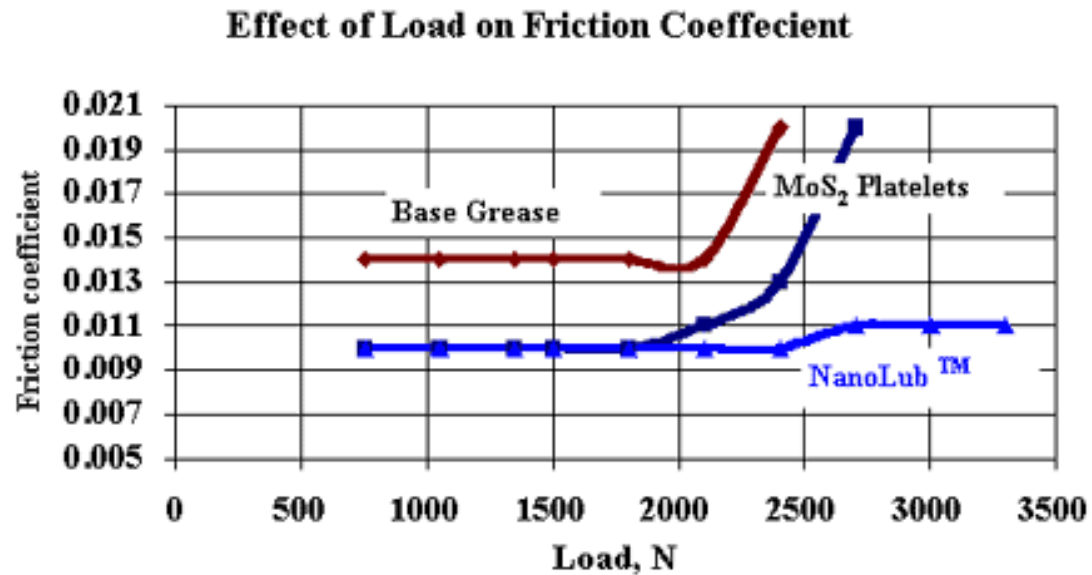


	$D_c, \text{\AA}$ 9,0 (5,5)	p_c, GPa 9,0 (5,5)	$k, \text{eV/\AA}^2 (\times 10^{-3})$ 9,0 (5,5)
300K	5.36 (5.76)	70.71 (47.62)	2.22 (2.89)
600K	5.36 (5.86)	68.28 (46.38)	2.05 (3.23)
1000K	5.56 (5.96)	62.15 (38.61)	2.11 (3.47)





Applications of inorganic nanotubes – New insights





Hydrogen storage by physisorption in aromatic carbon nanostructures



Energy sources for mobile applications

One possible design of the car of the future

HydroGen3 liquid



- Fuel: 4.6 kg LH₂
- Range (EDC): 400 km

HydroGen3 compressed 700



- Fuel: 3.1 kg CH₂
at 700 bar (10,000 psi)
- Range (EDC): 270 km

Technology: H₂ tank → fuel cells → electric engines



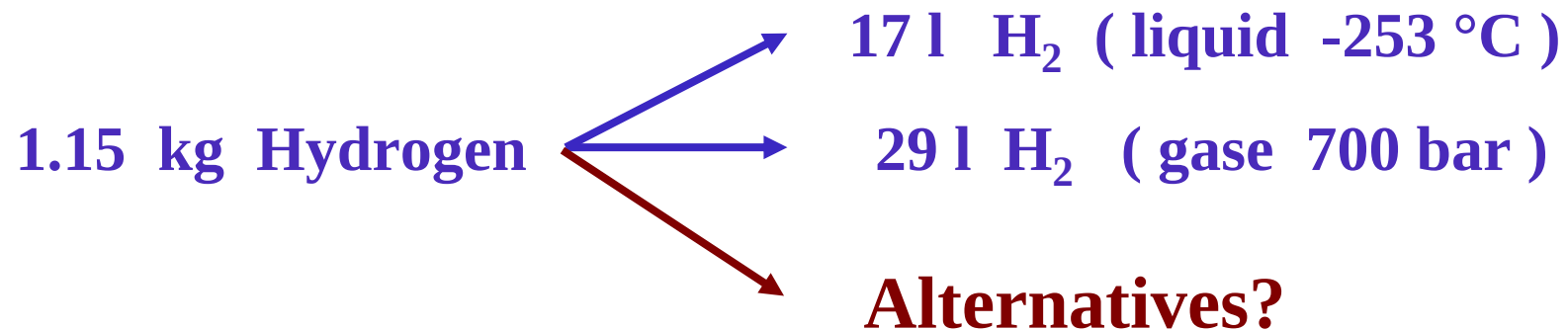
Problem: Storage of H₂

1 liter n-Octan	:	36.2 MJ
1 liter Hydrogen (NPT)	:	10.7 kJ

this is three order of magnitude lower than required for practical use !

European Driving Cycle EDC – Hydrogen Consumption

1.15 kg Hydrogen for 100 km (for that particular car)





London dispersion

- No overlapping densities
- Interaction of two polarisable objects

$$E_{\text{London}} = -\frac{2}{3} \frac{I_1 I_2}{I_1 + I_2} \alpha_1 \alpha_2 \frac{1}{r^6}$$

London, F.; Z. Physik 1930, 63, 245.

Well-known application: Lennard-Jones potential:

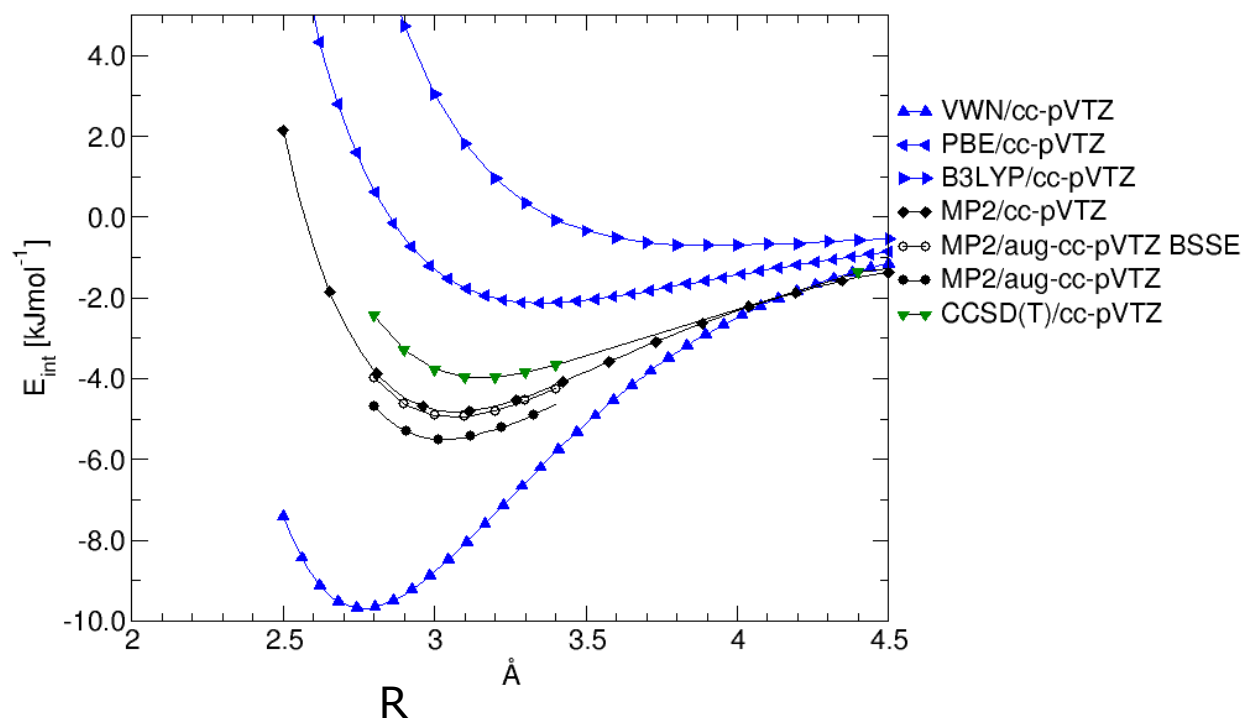
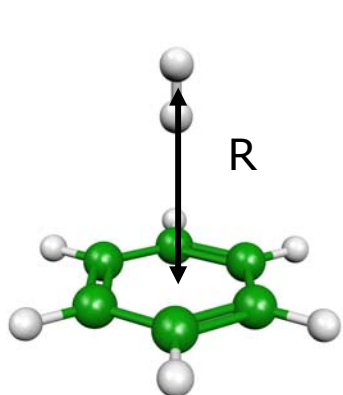
$$E_{\text{Lennard-Jones}} = \frac{C_{12}}{r^{12}} - \frac{C_6}{r^6}$$

short-range repulsion long-range attraction



Weak interactions and DFT?

(Available) Density-Functional theory for London dispersion interaction

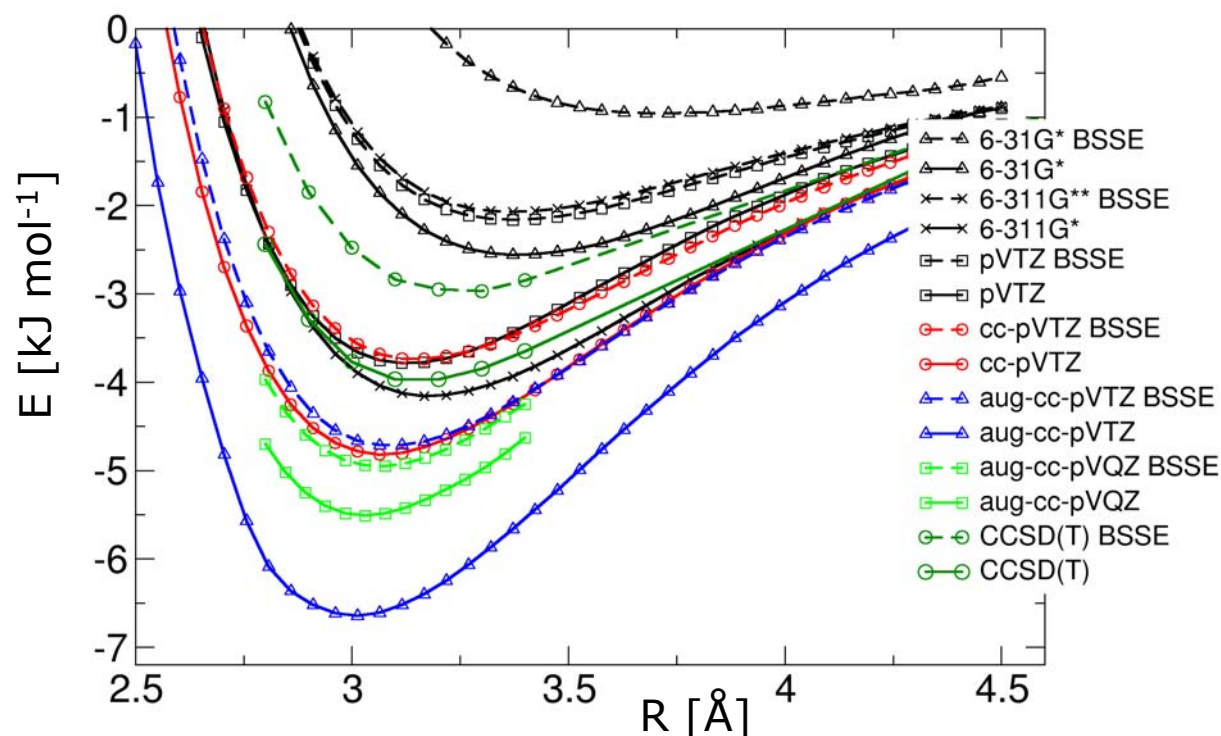
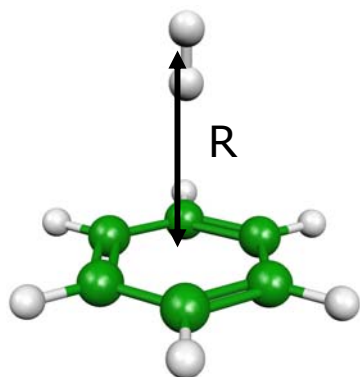


DFT is not appropriate for long-range dispersion



Weak interactions and ab initio theory?

Dispersion is a correlation phenomenon and extremely basis-set dependent. Ab initio theory (MP2, CCSD(T)) can account for it, but at a price we don't want to pay



Phys. Chem. Chem. Phys. 6 (2004) 980

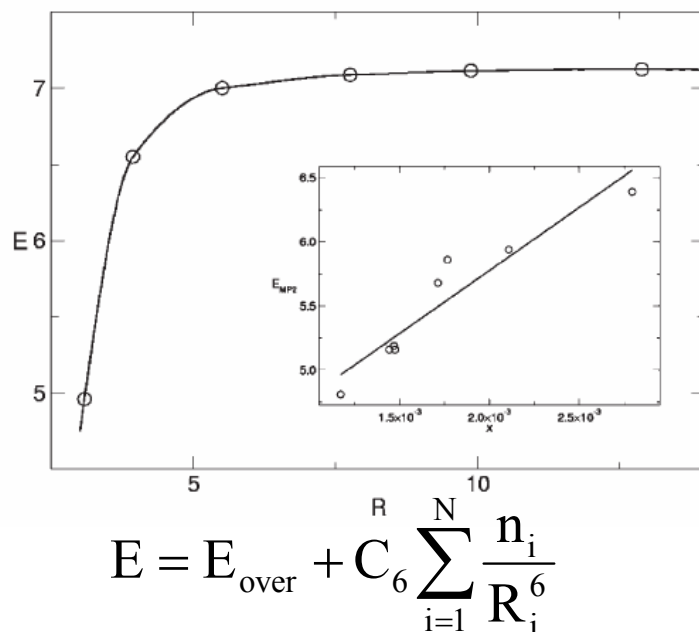


Alternatives

DFT gives wrong results
Decent ab initio is prohibitively expensive

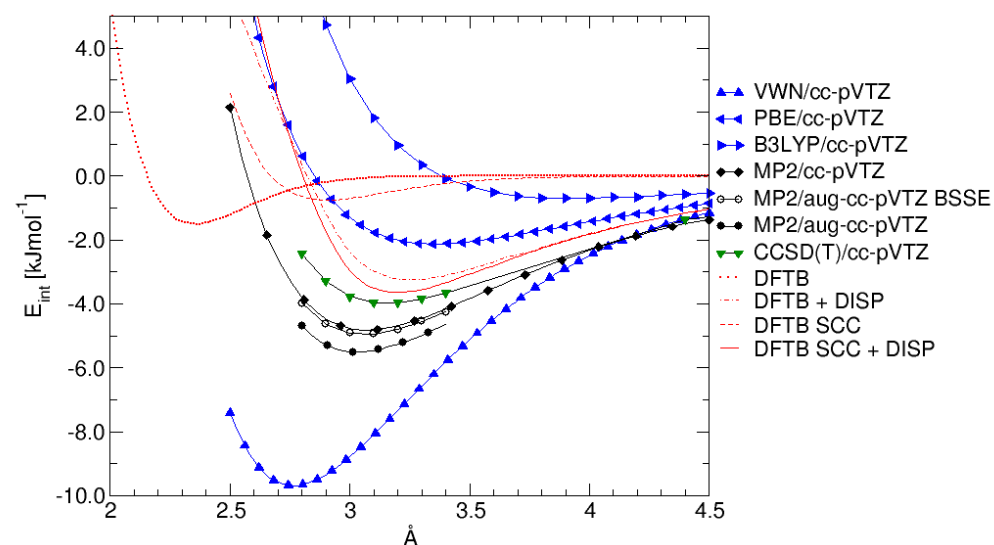
Find a reasonable model for the application

H₂-graphene interaction by extrapolation



Use a pragmatic method

Add a C₆ term to a method which excludes dispersion as approximate DFT (DFTB)



JCTC 1, 2005, 841

Email: thomas.heine@chemie.tu-dresden.de

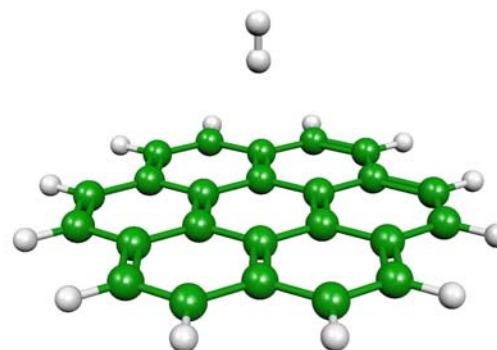
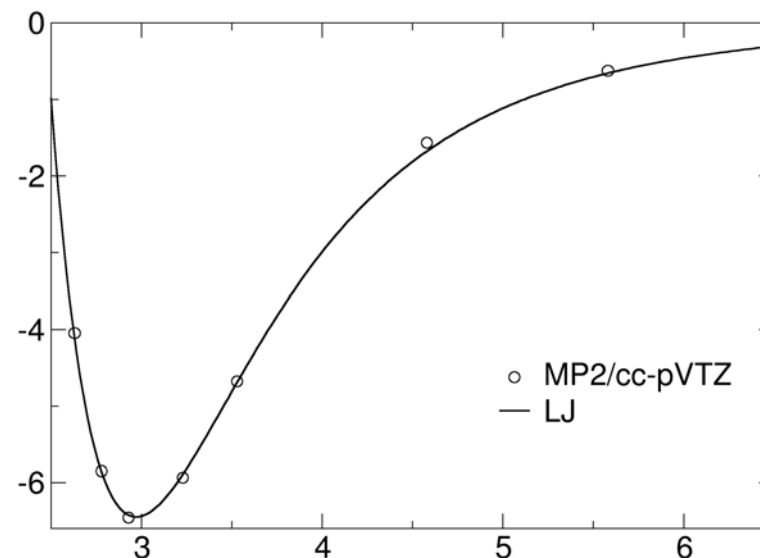
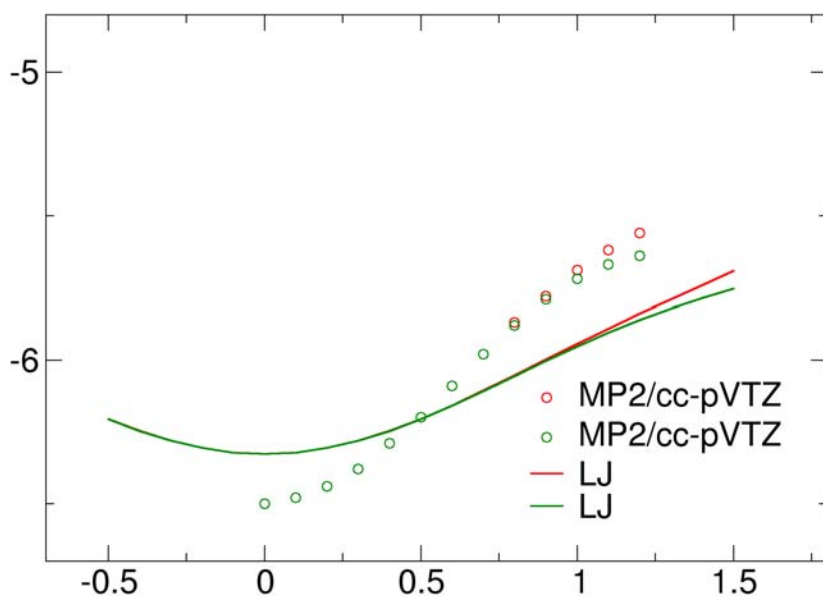


Create H₂-carbon interaction potential

Fitting ab initio results to
empirical potential

$$V(\mathbf{r}) = \sum_i A e^{-\alpha r_i} + C_6 r_i^{-6}$$
$$r_i = |\vec{r} - \vec{R}_i|$$

Movement of H₂ normal to PAH →



← lateral movement

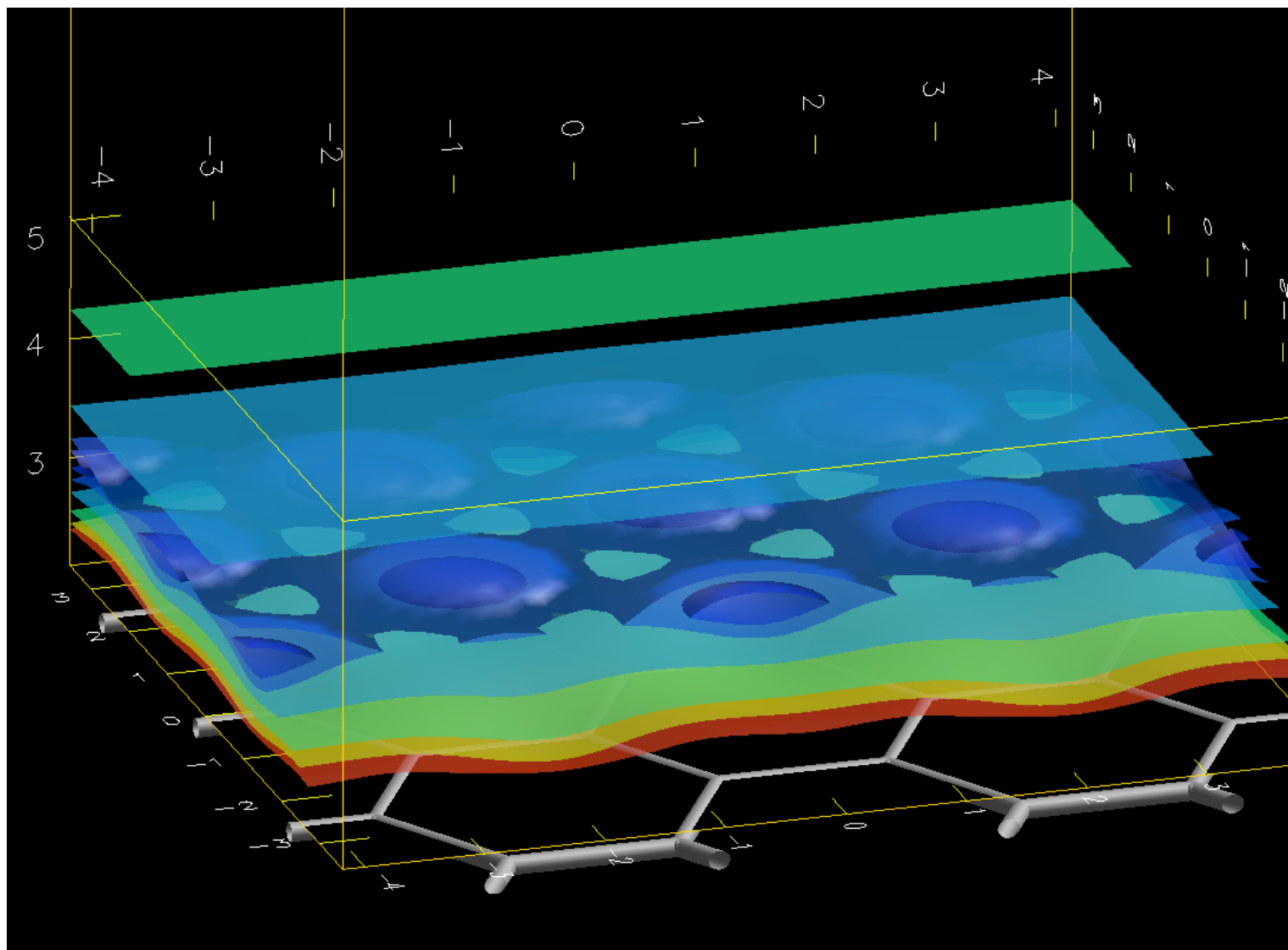


Computation of free energy

- *Quantum-mechanical treatment for computation of free energy* as
 - H_2 is light-weighted $\rightarrow$ zero point vibrations are large
 - H_2 -host potential is very soft $\rightarrow$ motion even at 0K
 - H_2 -host potential is strongly anharmonic $\rightarrow$ popular approximations fail
- *Computational strategy:*
 - solve stationary Schrödinger equation of one shapeless particle with mass of H_2 in the external potential of the frozen host structure
 - Compute the relative free energy ΔF with respect to free H_2 (gas state) within the same approximation (counterpoise correction)
- *Note:*
 - Classical simulation possible (e.g. Monte Carlo), but many simulations necessary to obtain statistically relevant number



Potential of graphite in the box



V [kJ/mol] =
-7.35 (deep
blue), -7.13
(blue), -6.0
(teal), -3.0
(green), 0.0
(yellow), and
3.0 kJ/mol
(red)

*PNAS 2005,
102, 10439*



Computation of adsorption free energy ΔF

- compute eigenstates ε_i of the two systems (in host potential and reference free particle)
- Compute partition function

$$q = \sum_i \exp\left(\frac{-\varepsilon_i}{kT}\right)$$

- Compute relative free energy

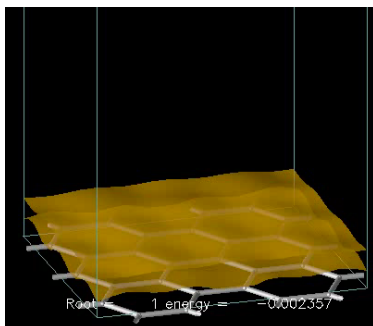
$$\Delta F = -RT \ln\left(\frac{q}{q_r}\right)$$

- Compute equilibrium constant

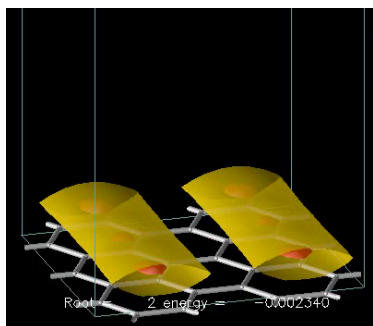
$$K_{eq} = \exp\left(-\frac{\Delta F}{RT}\right)$$



Probability densities of H₂ on graphene

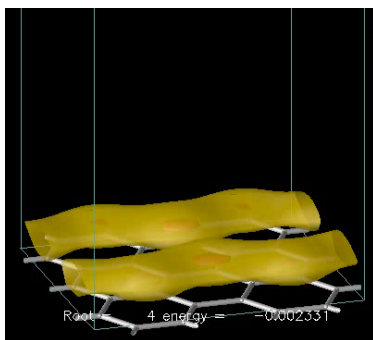


1st, 2nd, and 4th eigenstates for the single-layer graphene structure.



$$\begin{aligned}\Delta F(0K) &= -6.2 \text{ kJ/mol} \\ \Delta F(300K) &= -1.2 \text{ kJ/mol} \\ K_{eq}(300K) &= 1.6\end{aligned}$$

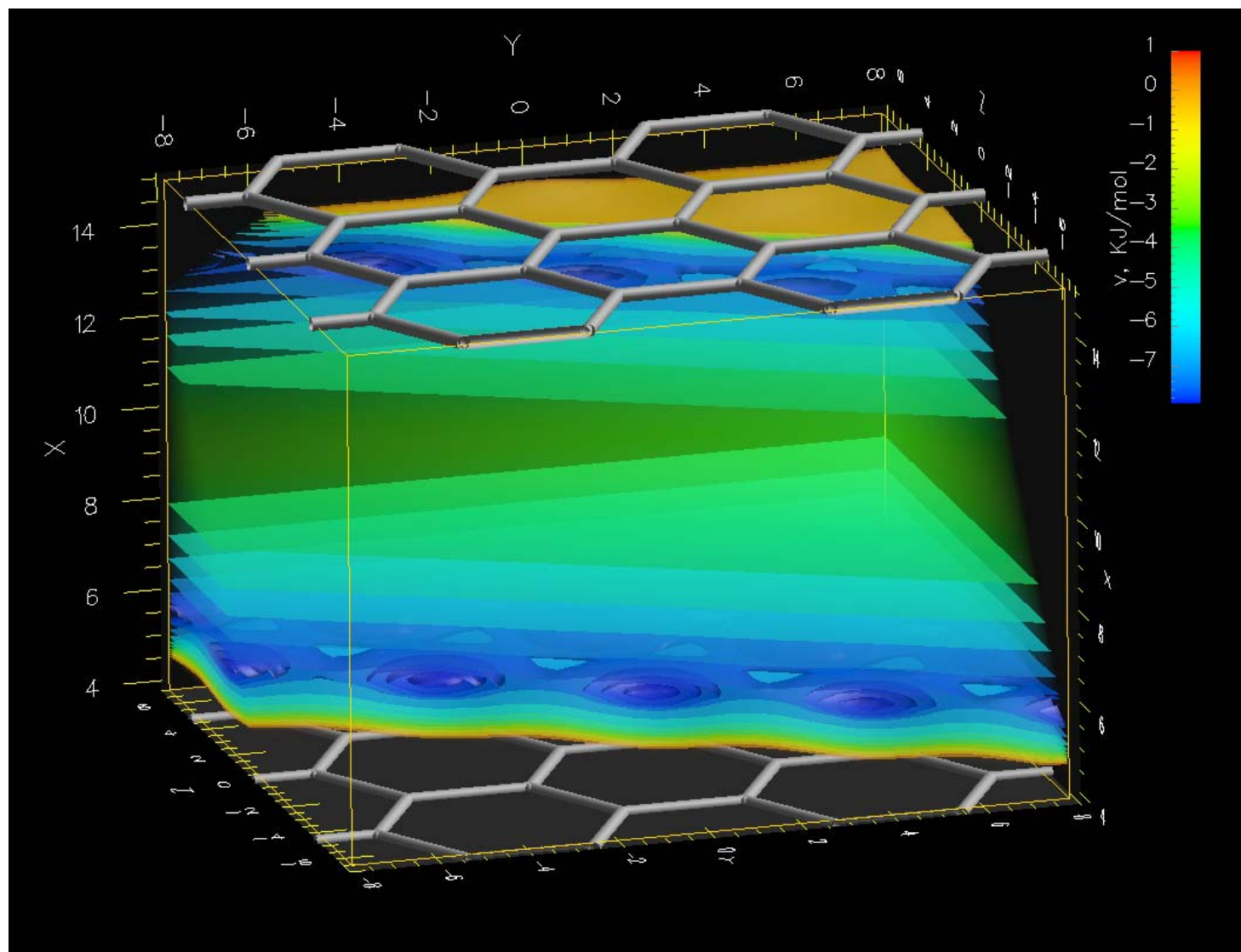
**→ Graphite surfaces are lousy
H₂ storage materials!**



*S. Patchkovskii, J. Tse, S. Yurchenko,
L. Zhechkov, G. Seifert, T. Heine,
PNAS 2005, 102, 10439*



Potential of graphite in the box

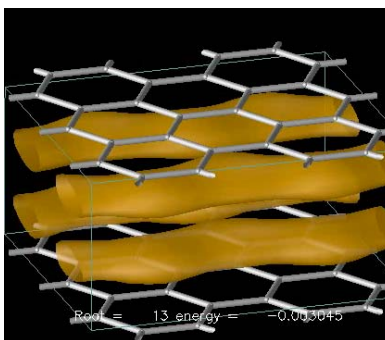
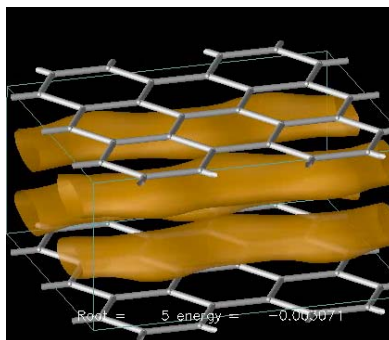
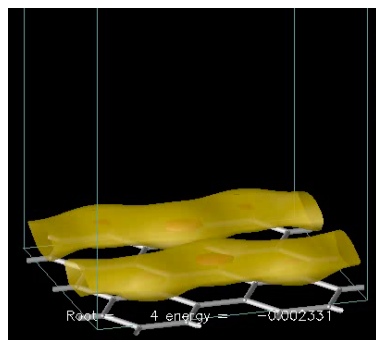
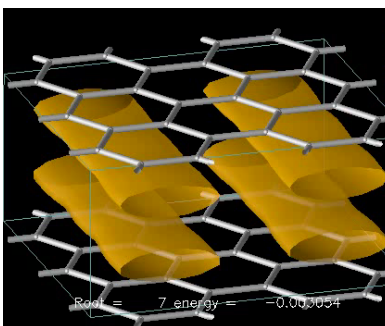
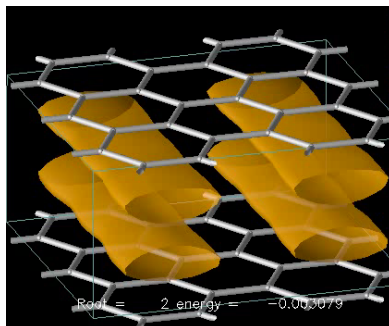
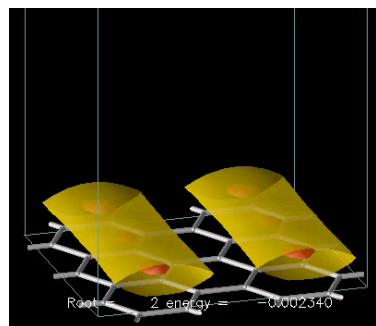
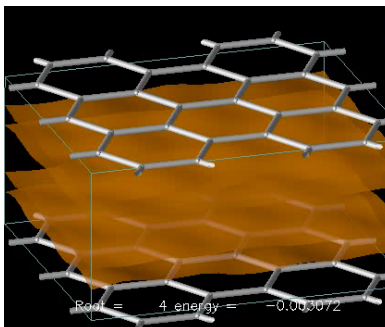
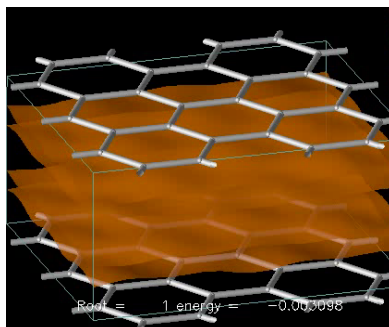
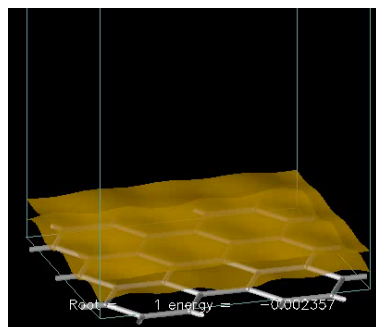


V [kJ/mol] =
-7.35 (deep blue), -7.13 (blue), -6.0 (teal), -3.0 (green), 0.0 (yellow), and 3.0 kJ/mol (red)

*PNAS 2005,
102, 10439*



Probability densities of H_2



A

B

C

A: 1st, 2nd, and 4th eigenstates for the single-layer graphene structure. B, C: Corresponding in-phase (B: 1st, 2nd, and 5th) and out-of-phase (C: 4th, 7th, 13th) eigenstates for the double-layer structure (8Å interlayer separation).

*PNAS 2005,
102, 10439*



H₂ in a graphite bilayer of distance c

c, Å	$\Delta F(0K)$, kJ/mol	$\Delta F(300K)$, kJ/mol	K(300K)
∞^a	-6.2	-1.2	1.6
12	-6.4	-4.2	5.5
10	-6.7	-5.2	8.0
8	-8.1	-7.3	18.6
6	-13.0 ^a	-10.0 ^a	56.2 ^b

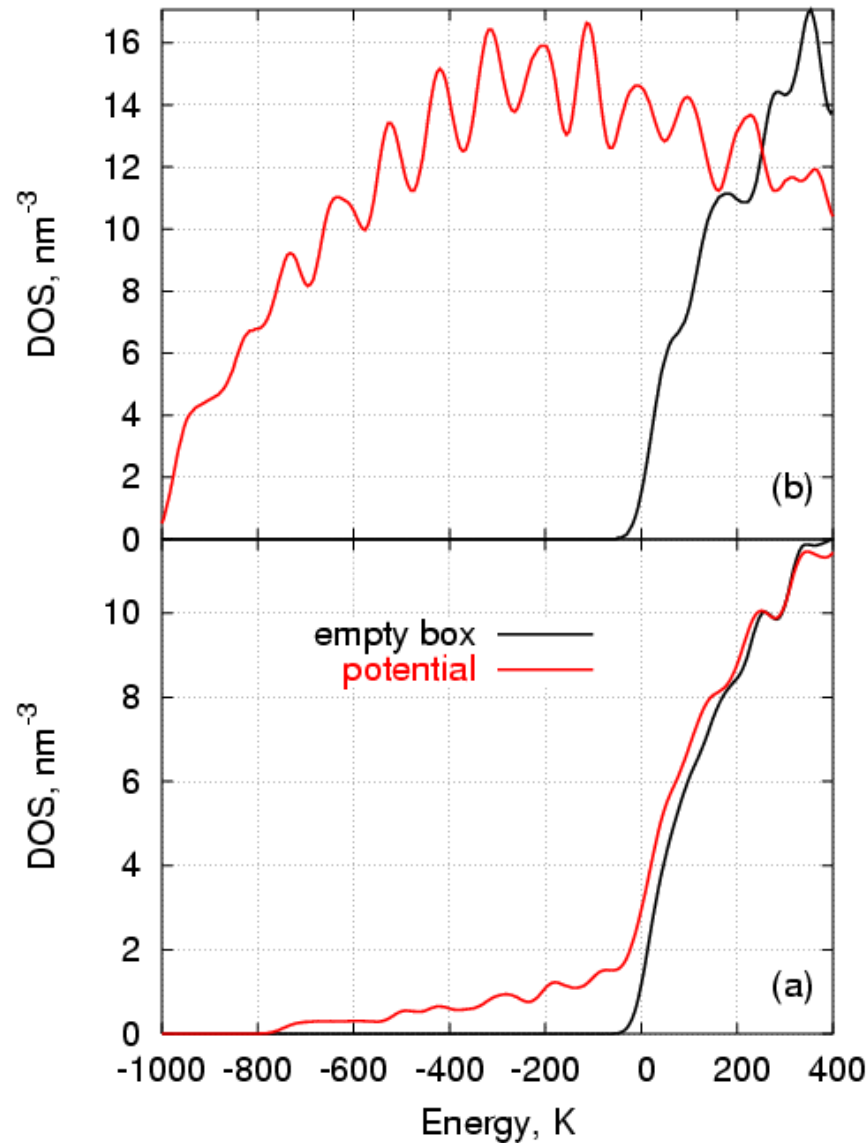
^aThe infinite distance is computed in a box with c=80 Å, but with only one monolayer contributing to the potential.

^bDue to inherent inaccuracies of our model these numbers are subject to larger error bars.

Result: graphene is a lousy H₂ storage material
But: Bilayer appears to be a good H₂ storage material



Density-of-states (DOS)



bilayer, $c=8\text{\AA}$

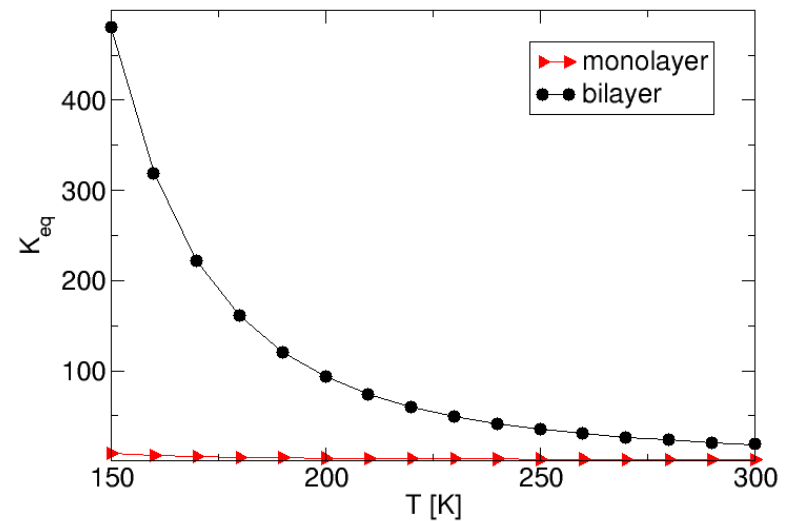
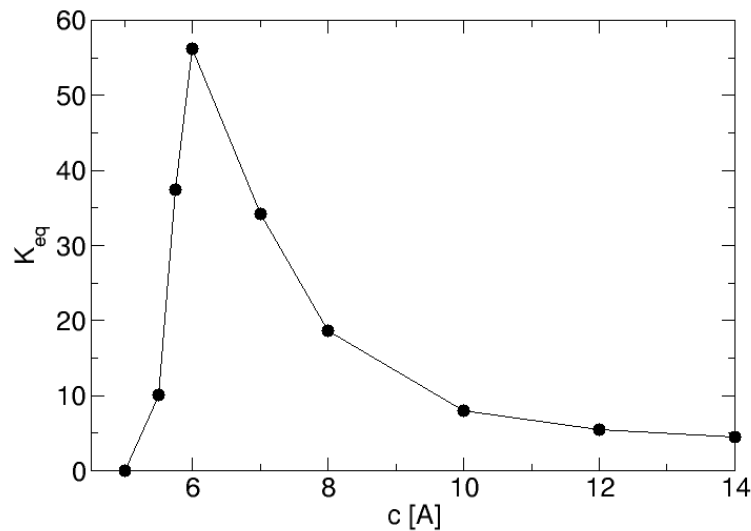
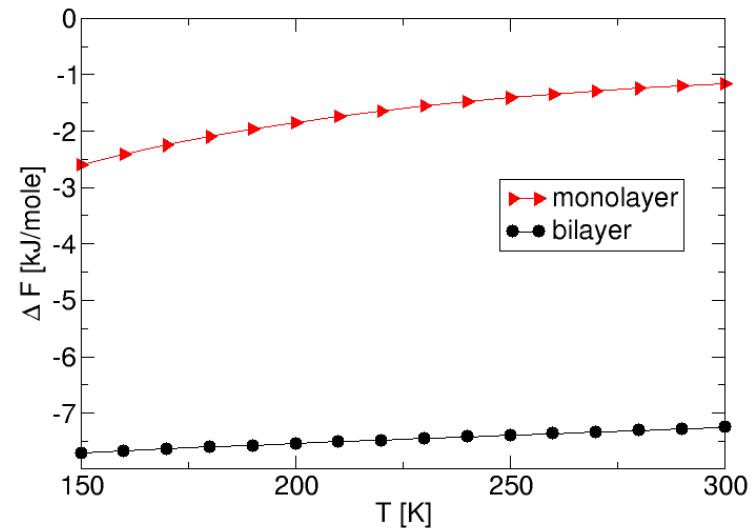
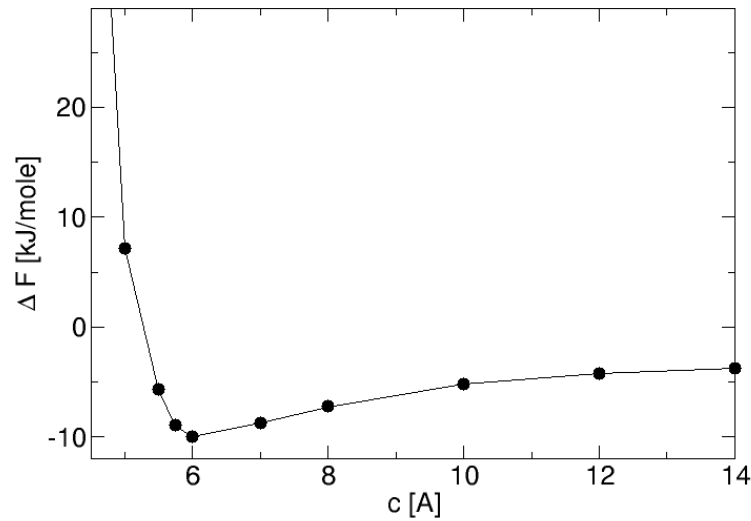
Note: H_2 is a boson, so states can be occupied with many particles

monolayer, $c=\infty$

PNAS 2005, 102, 10439

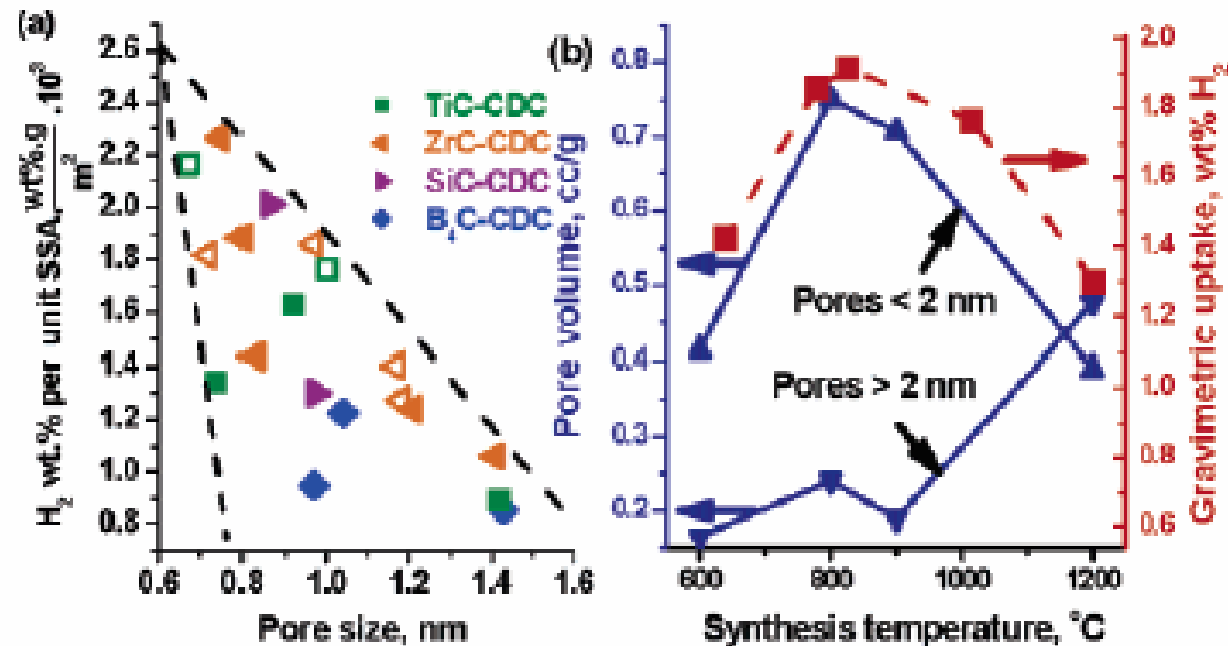


Influence on ΔF_{300} and K_{eq}





Experimental confirmation



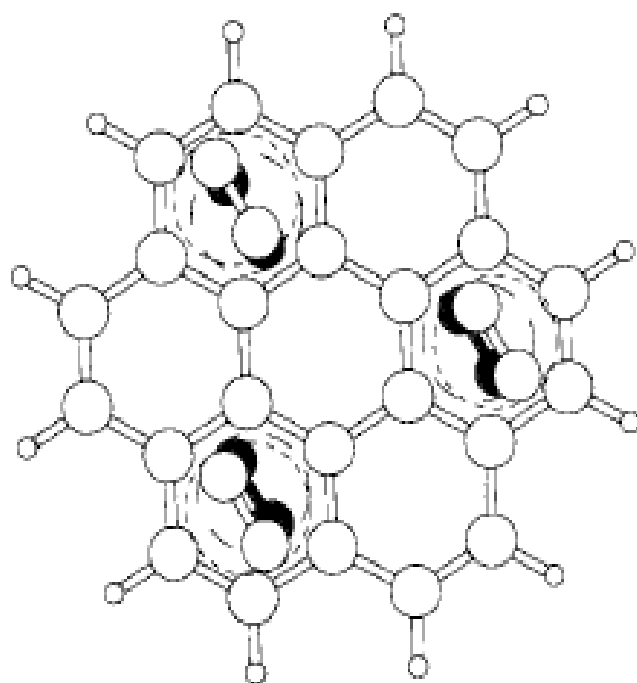
Y. Gogotsi, R. K. Dash, G. Yushin, T. Yildirim, G. Laudisio, J. E. Fischer, *J. Am. Chem. Soc.* 2005, 127, 16006.

Figure 2. Effect of pore size on hydrogen sorption. (a) Hydrogen storage normalized to surface area plotted as a function of pore size for several CDCs. The general trend defined by the dashed line envelopes indicates that small pores are more efficient than large ones for a given SSA. Solid symbols stand for as-produced and empty for hydrogen-annealed CDC. (b) Pore volume for micropores (< 2 nm) and mesopores (> 2 nm) in comparison with the gravimetric hydrogen uptake as a function of chlorination temperature for B₄C–CDC.

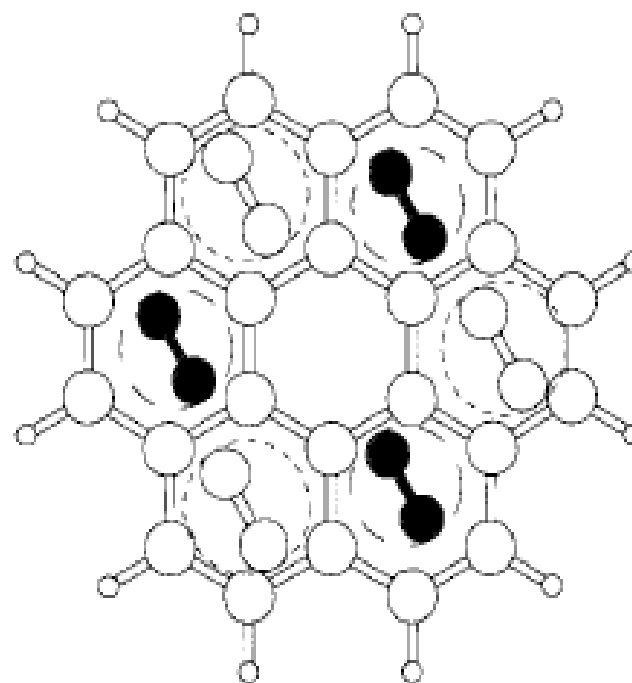


Second challenge for reproducible experimental results in the field of H₂ physisorption

Interaction of N₂ with PAHs is ~ 3 times stronger than that of H₂!



non-alternating occupation.

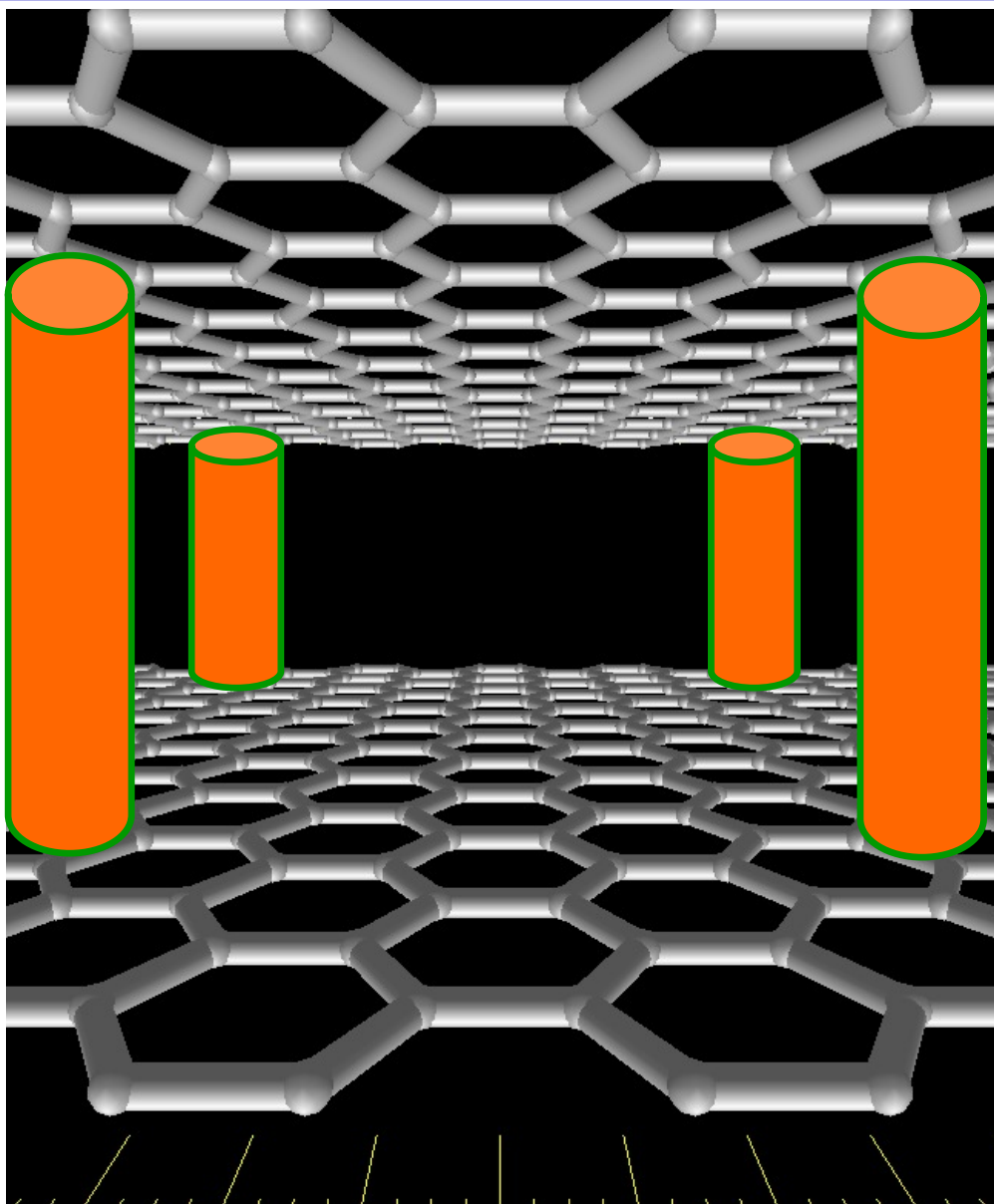


alternating occupation

L. Zhechkov, T. Heine, G. Seifert, Int. J. Quantum Chem. 106 (2006) 1375.



Message: Interlayer distance needs to be fixed!



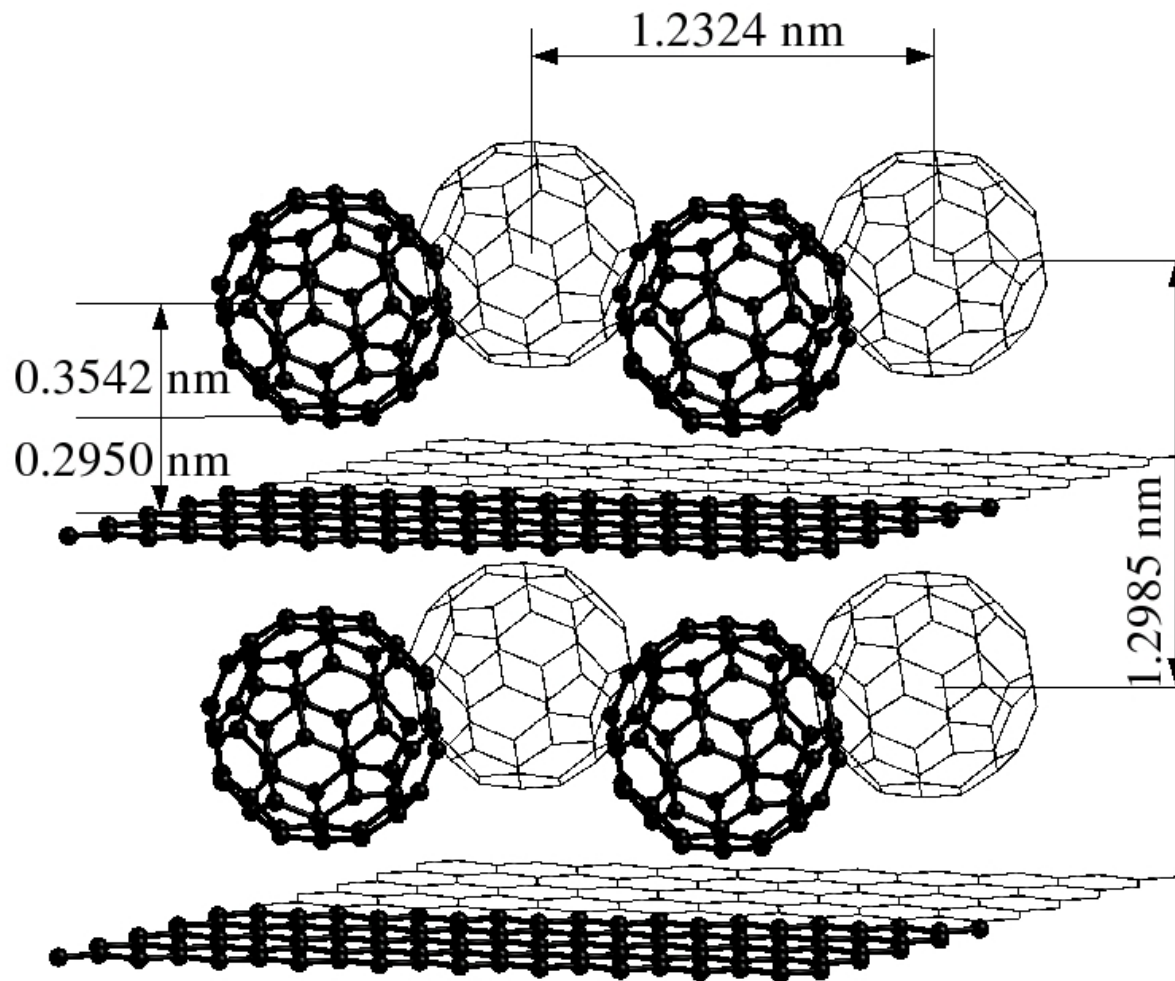
There are several ways to fix the interlayer distance (functionalisation, internal polymerisation, intercalation with cations or spacers...).

Our favourite: Introduction of spacer molecules → „nano combs“

Additional beneficial effect: nano combs can act as nano sieve and protect the carbon nanostructures from gas impurities.



Recent experiment: fullerenes as spacers in graphite, C_{60} -intercalated graphite (CIG)



C_{60} -intercalated graphite (CIG) has been synthesised and characterised.

*Gupta, V., Scharff, P.,
Risch, K., Romanus, H.,
Müller, R., Solid State
Comm. 2004, 131, 153.*



Stability of CIG

Calculated (DC-DFTB) cohesion energies per C-atom (E_{atom}), HOMO-LUMO-gaps (Δ) and mass densities (ρ) for several carbon allotropes. Experimental values are given in parenthesis.

structure	E_{atom} (eV/atom)	Δ (eV)	ρ (g/cm ³)
graphite	-9.09	0 (0) ¹	2.27 (2.266) ¹
graphene layer	-8.90	0 (0)	--
diamanond	-8.87	6.88 (6.01) ¹	3.54 (3.514) ¹
C ₆₀ (gas phase)	-8.51	1.78 (1.7)	--
C ₆₀ (solid state)	-8.54	1.67 (1.70) ²	1.73 (1.72) ²
CIG	-8.71	0	1.28

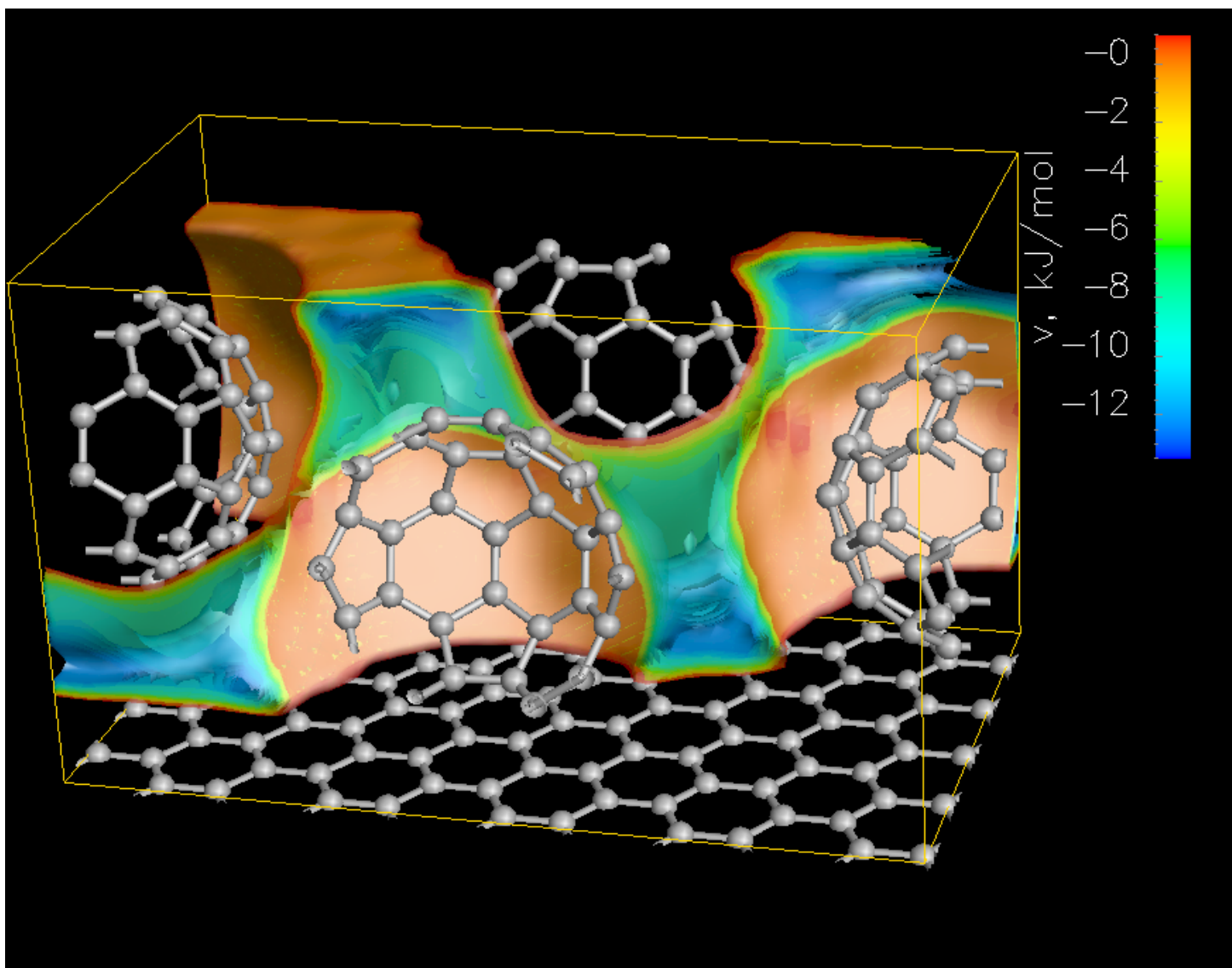
¹Greenwood, N. N.; Earnshaw, A., *Chemistry of the elements*. Elsevier: Amsterdam, 1997.

²Dresselhaus, M. S.; Dresselhaus, G., Fullerenes And Fullerene-Derived Solids As Electronic Materials. *Annual Review Of Materials Science* **1995**, 25, 487-523.

A. Kuc, L. Zhechkov, S. Patchkovskii, G. Seifert, T. Heine, Nano Letters, 7 (2007) 1.

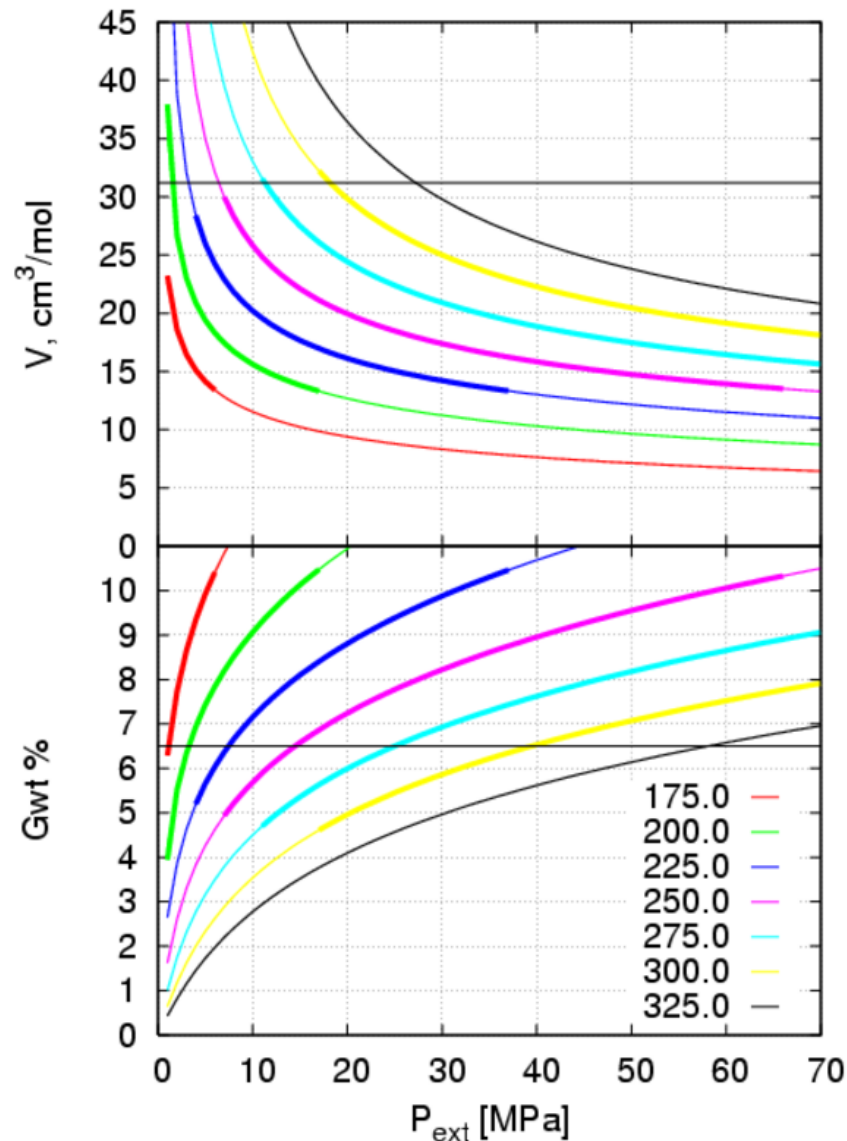


H₂-CIG interaction potential





H₂ storage capacity of CIG



Volumetric (top) and gravimetric H₂ storage capacity of CIG, calculated using the real gas equation as function of the external pressure. Isotherms for various temperatures (colour coded) are plotted. Our approximations hold for the bold parts of the isotherms.

A. Kuc, L. Zhechkov, S. Patchkovskii, G. Seifert, T. Heine, Nano Letters, 7 (2007) 1.



CIG as molecular sieve

- Diffusion constants, calculated through Einstein's relation, from a MD simulation of a CIG supercell containing ~ 2000 atoms over 1 ns.
 - H_2 : $8.5 \cdot 10^{-3} \text{ cm}^2/\text{s}$
 - N_2 : $3.8 \cdot 10^{-4} \text{ cm}^2/\text{s}$
 - C_{60} : $1.7 \cdot 10^{-4} \text{ cm}^2/\text{s}$
- Conclusion: The fullerene pockets are trapping N_2 . Therefore, CIG can separate H_2 from N_2 („Nano-HPCL“)

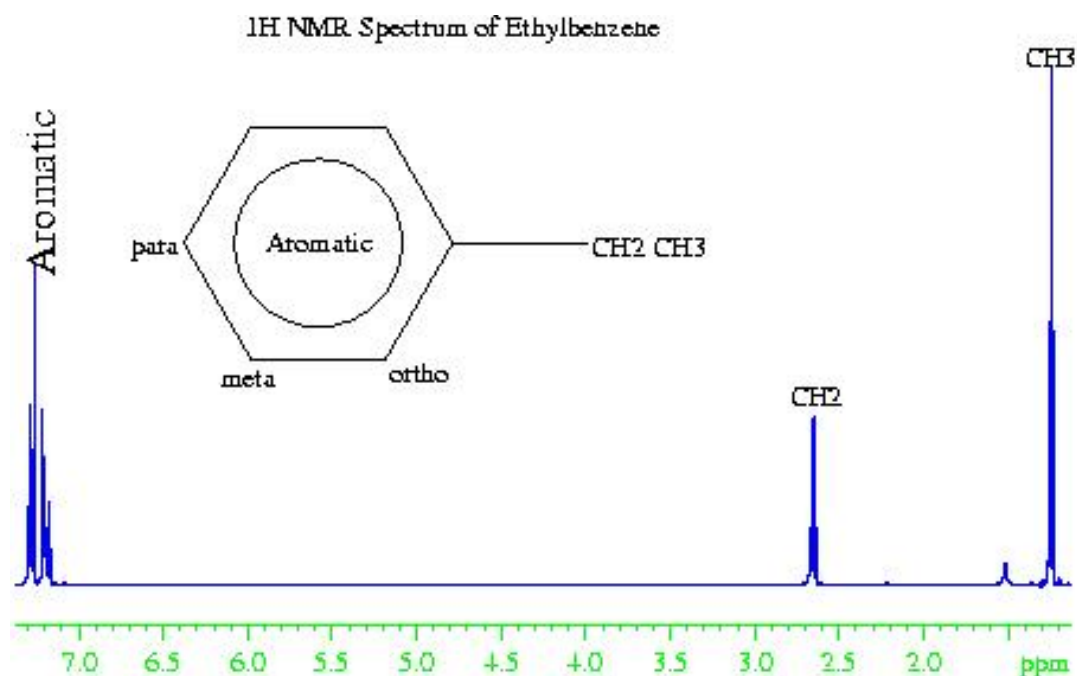
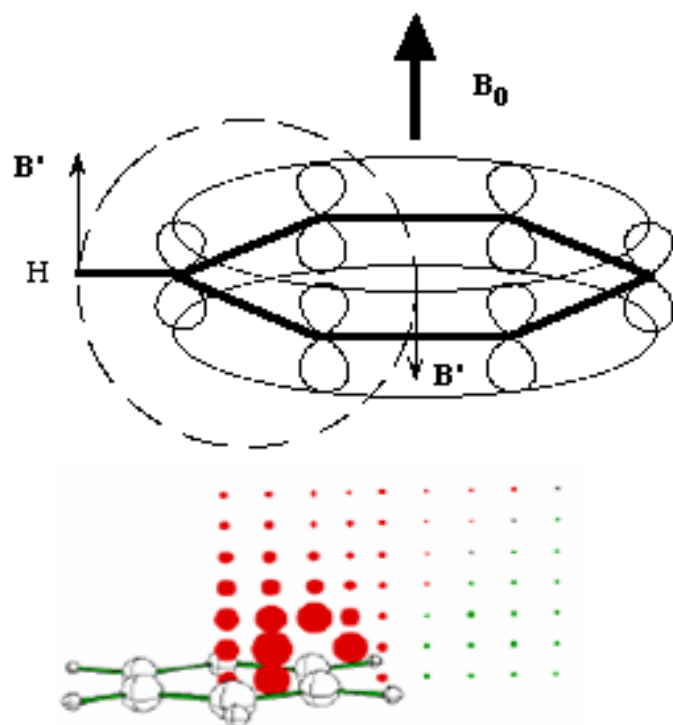


Magnetic properties of aromatic systems



The Pople model

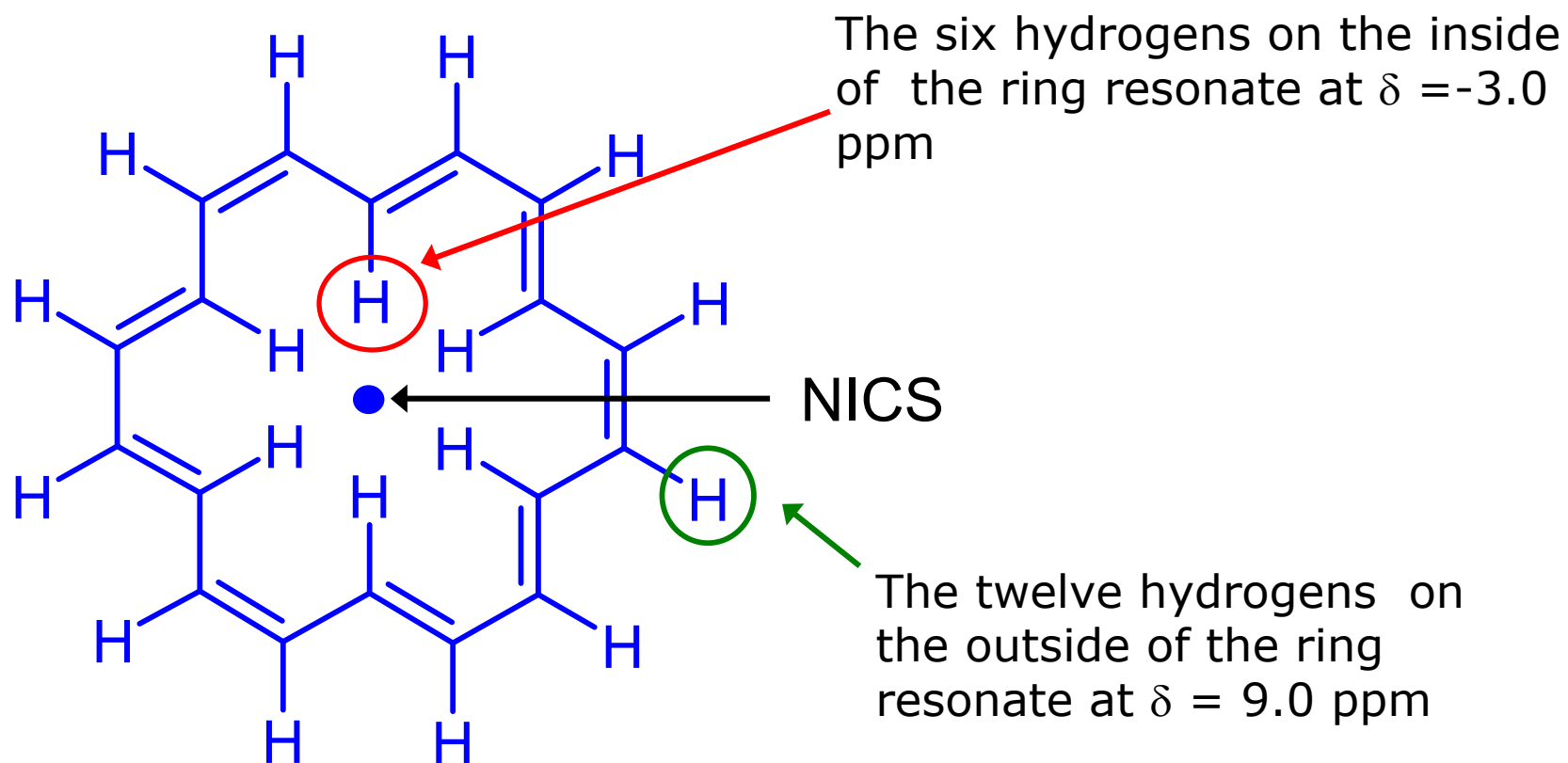
- External magnetic field B_0 induces ring current in π system
- π current induces magnetic counter field B'
- B' increases B_0 at positions of protons (deshielding)
- B' shields ring centre



Nucleus-independent chemical shifts (NICS)
Schleyer et al., J. Am. Chem. Soc. 1996, 118, 6317

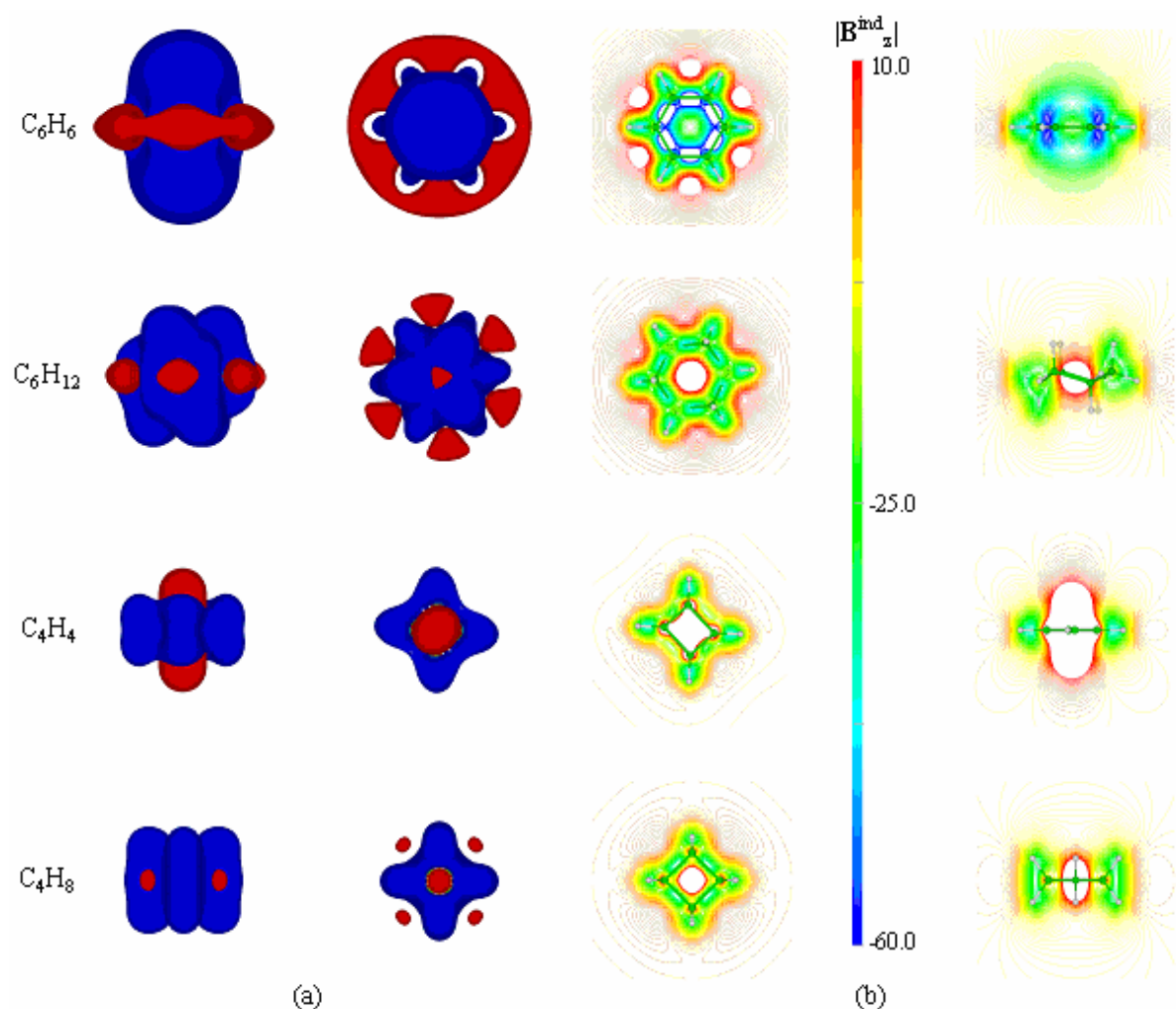


Experimental evidence: [18] annulene





What about antiaromatic and non-aromatic molecules?



a) Isosurfaces of the z component of the induced magnetic field (IMF, B_z^{ind}). $|B_z^{ind}| = 4$ mT and $B_{ext} = 1$ T perpendicular to the molecular plane, given in top and front view of the molecule. Blue and red indicate shielding ($|B_z^{ind}| < 0$) and deshielding areas, respectively.

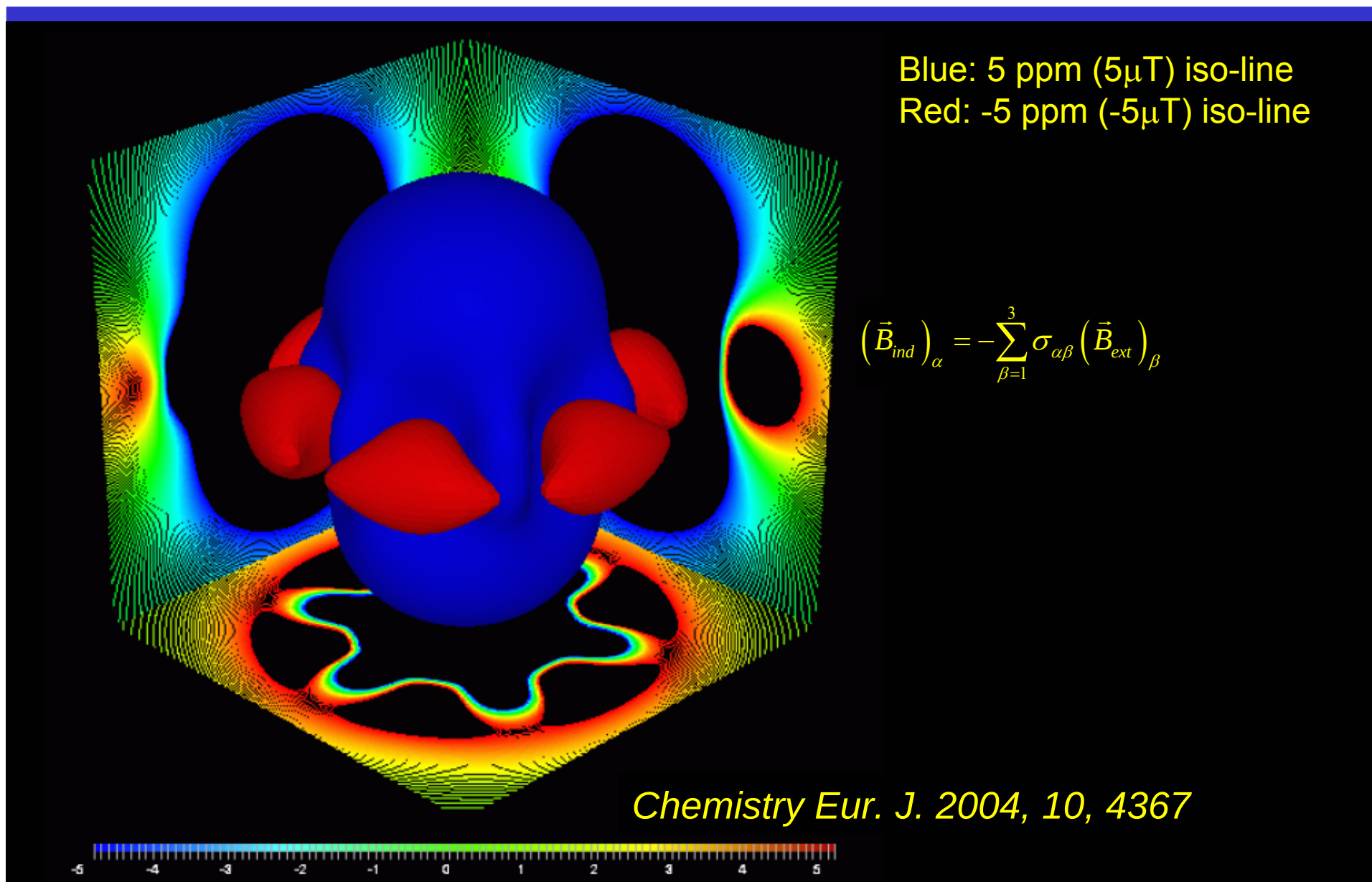
b) Contour lines of B_z^{ind} in the molecular plane and perpendicular to the molecular plane through the origin. The scale is given in ppm (or mT for an external field of 1 T).

Chemistry – Eur. J. 2004, 10, 4367

Email: thomas.heine@chemie.tu-dresden.de



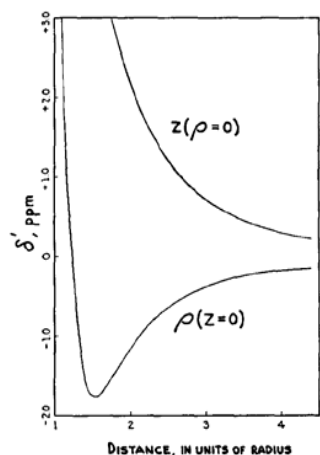
Induced magnetic field (IMF) of benzene





Chemical shieldings at non-nuclear positions

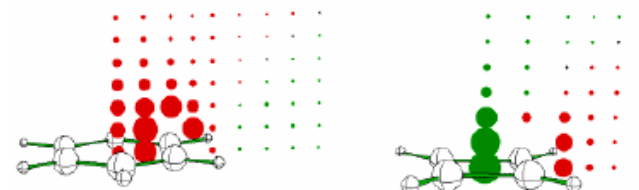
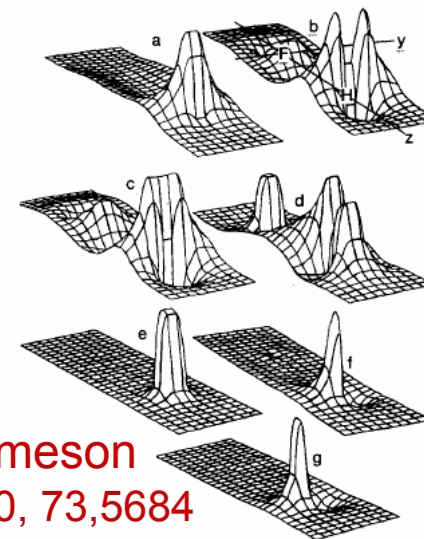
They give the shielding of an external magnetic field by the molecule



Isoshielding lines
Johnson & Bovey
J. Chem. Phys. 1958, 29, 1012

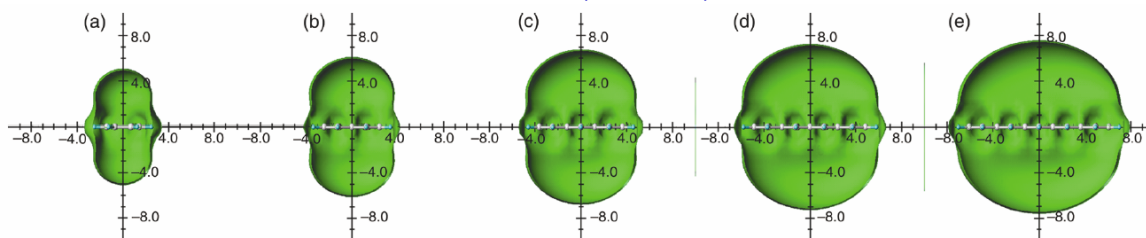
Neutron chemical shift
Wolinski,
J. Chem. Phys. 1997, 106, 6061

Shielding density
Buckingham & Jameson
J. Chem. Phys. 1980, 73, 5684



Isochemical Shielding Surface (ICSS)
Klod & Kleinpeter,
J. Chem. Soc. Perkin Trans. 2, 2001, 1893

Nucleus-independent chemical shifts
(NICS) Schleyer et al.,
J. Am. Chem. Soc. 1996, 118, 6317





Commercial break

AMERICAN CHEMICAL SOCIETY

COMING
SOON—
IN
OCTOBER
2005

CHEMICAL REVIEWS

Thematic Issue...
Delocalization — Pi and Sigma
Guest Editor:
Prof. Paul von Ragué Schleyer
University of Georgia
Volume 105, Issue 10

Chemical Reviews is one of the most highly regarded and highest ranked journals covering the general topic of chemistry. Since 1985, Chemical Reviews has been publishing periodic thematic issues. These quasi-monographs can be ordered individually, while supplies last, at the special ACS-member price of \$35 per issue (non-members: \$45). They represent real value to both the student and the professor of chemistry.

ACS offers two free options for e-mail notification of new Chemical Reviews articles published on the Web. With ASAP Alerts, you can receive daily or weekly e-mail messages alerting you as soon as individual articles are released on the Web. With Table of Contents Alerts, you receive e-mail alerts of the table of contents of complete issues on the day they are posted on the Web. To sign up, go to <http://pubs.acs.org> and click on the tab at the top of the page.

For a complete listing of all Chemical Reviews thematic issues, go to <http://pubs.acs.org/CR>

 **ACS PUBLICATIONS**
HIGH QUALITY. HIGH IMPACT.

The magnetic shielding function of molecules and pi electron delocalization

T. Heine, C. Corminboeuf, G. Seifert
Chem. Rev. **105** (2005) 3889-3910.

Description of Electron Delocalization via the Analysis of Molecular Fields

G. Merino, A. Vela, and T. Heine
Chem. Rev. **105** (2005) 3812-3841.



Magnetic shielding in DFT

Traditional concept

- (Ramsey, Phys. Rev. 1950, 78, 699)

$$\sigma_{\alpha\beta} = \frac{\partial^2 E}{\partial (\vec{B}_{ext})_{\alpha} \partial (\vec{\mu})_{\beta}}$$

- Holds at position of a nucleus with moment $\vec{\mu}$
- Implemented in most electronic structure codes (CPHF and beyond, DFT)

Chem. Rev. 105 (2005) 3889-3910.

Alternative concept

- (Eschrig et al., Solid State Comm. 1985, 56, 777; Bieger et al., Chem. Phys. Lett. 1985, 115, 275):

- Biot-Savart's law:

$$\vec{B}_{ind}(\vec{r}) = \frac{1}{c} \int \frac{\vec{j}(\vec{r}') \times \vec{r}}{(r')^3} d^3 r'$$

- Shielding from induced field:

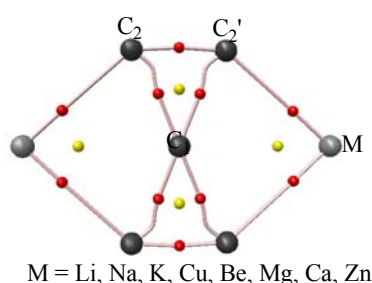
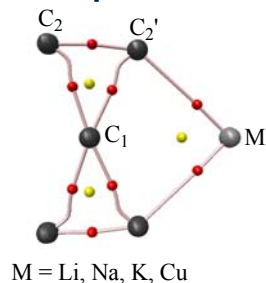
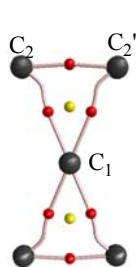
$$(\vec{B}_{ind})_{\alpha} = - \sum_{\beta=1}^3 \sigma_{\alpha\beta} (\vec{B}_{ext})_{\beta}$$

- Holds in full space
- Requires current density $\vec{j}(\vec{r})$



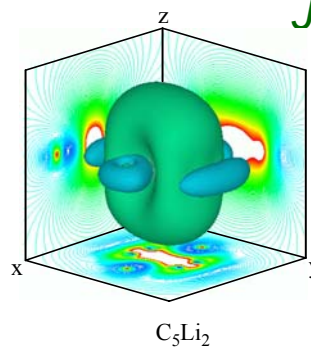
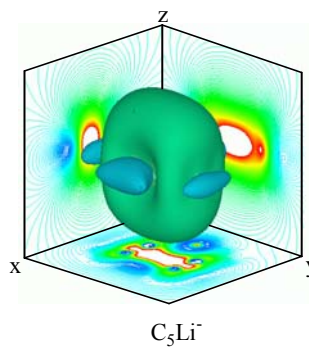
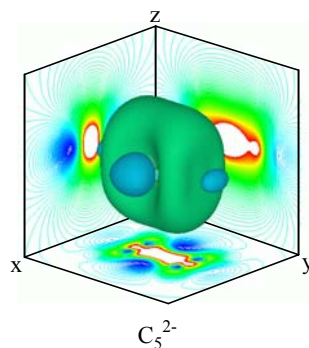
Molecular stability and electron delocalization

- Non-bound electrons can interact and be stabilized. Most well-known example: "aromaticity" (Hückel-rules).
- Magnetic properties (shieldings, induced magnetic fields, ring currents) characterize diatropic (=shielding=stabilizing) and paratropic (=deshielding=destabilizing) electronic systems
- New examples: planar tetracoordinate carbon (ptC) based on C_5^{2-}



Topological analysis of $\rho(\vec{r})$

J. Am. Chem. Soc. 2004, 126, 1610.

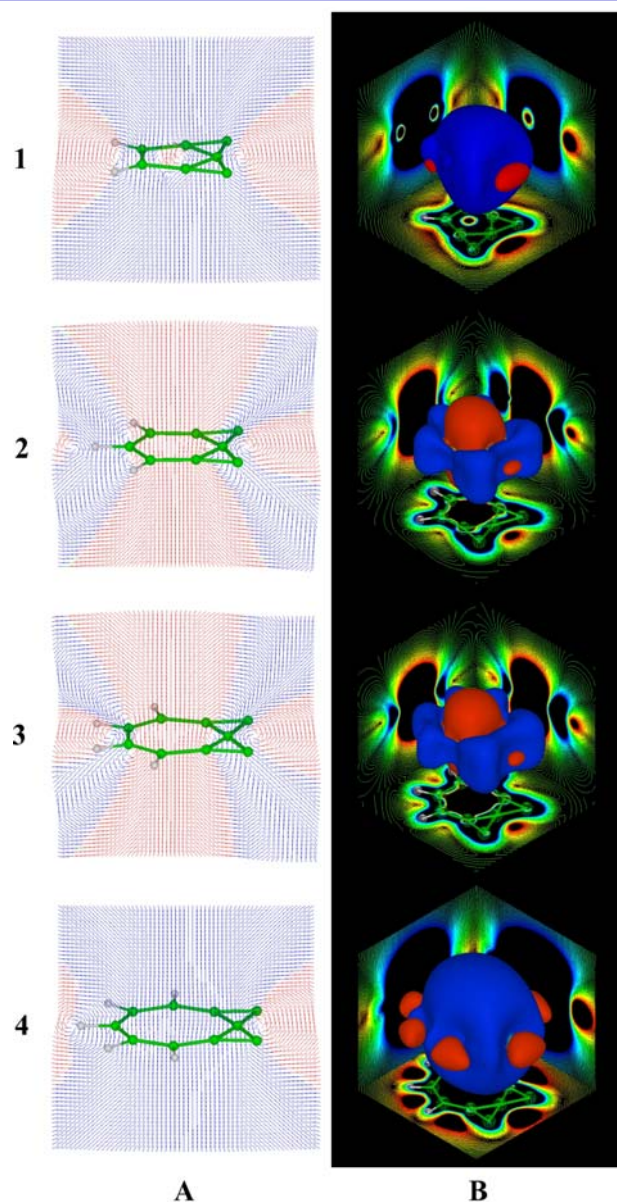


Induced magnetic field

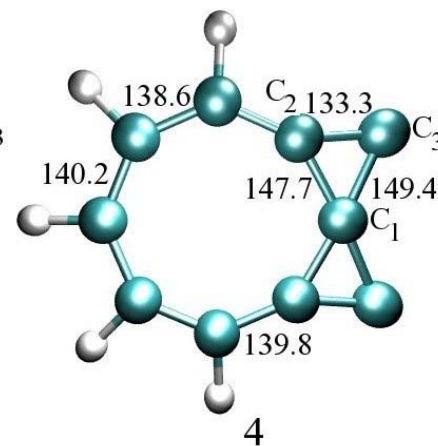
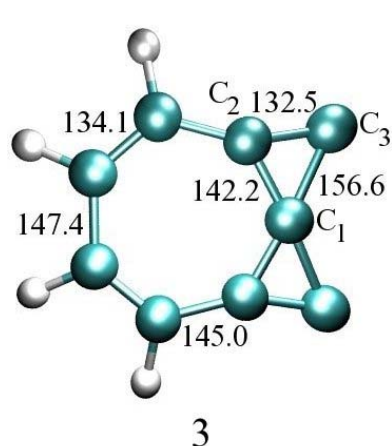
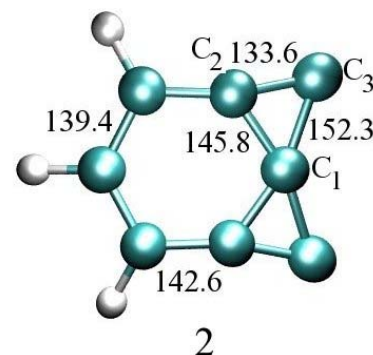
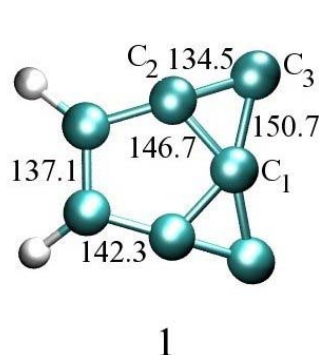




Organic cycles containing a ptC



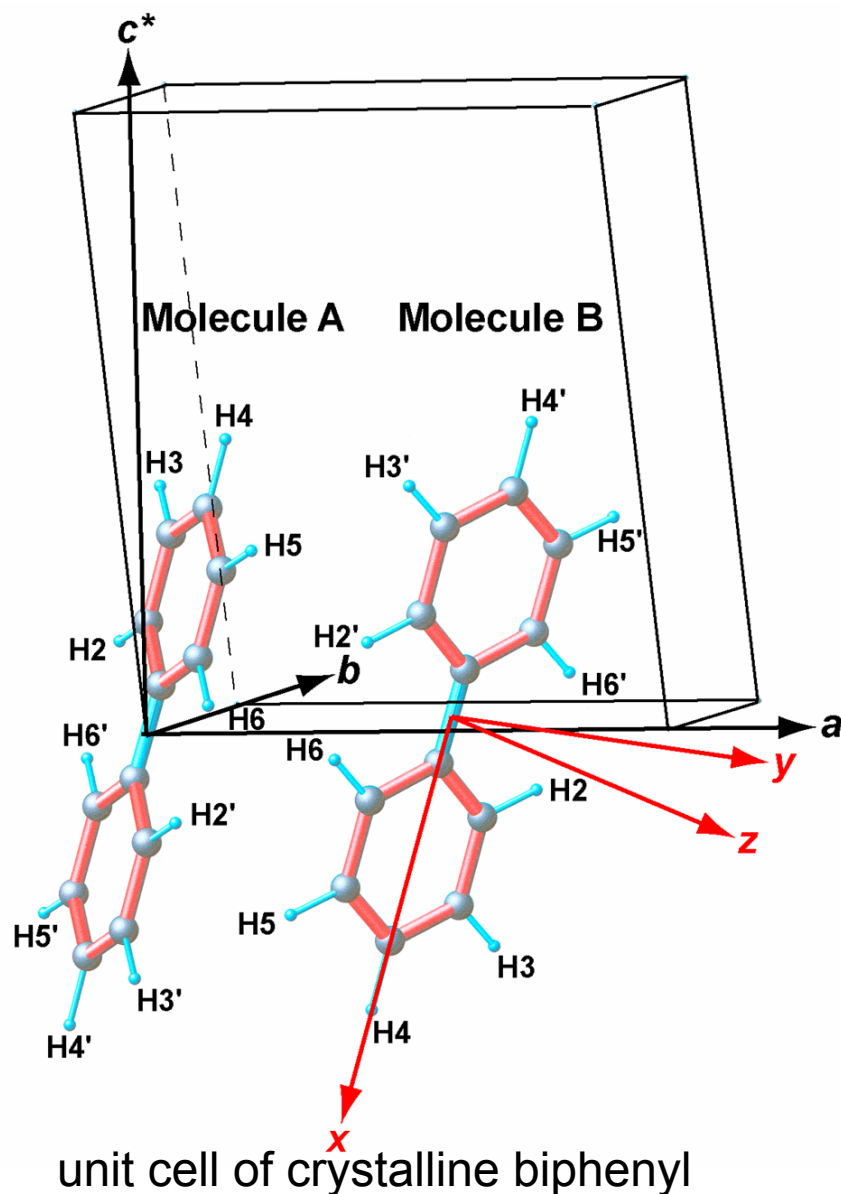
Cyclic hydrocarbons containing a ptC
Mechanical vs. electronic stabilization (for
“aromatic” isomers: life time of 5-10 ps at 300 K)



Org. Lett. 2005, 7, 1509.



The shielding tensor of biphenyl



Biphenyl: van-der-Waals crystal

^1H NMR (multi-pulse NMR)
measurement at low T (250K) to avoid
flipping of phenyl rings

Direct assignment of ^1H NMR shift
tensors to protons impossible

^1H NMR computations of single
biphenyl molecule fail to describe ^1H
NMR solid state chemical shift (tensor)
(cf. Wolinski et al., J. Am. Chem. Soc.
1990, 112, 8251)

J. Magn. Res. 2005, 175, 52

Email: thomas.heine@chemie.tu-dresden.de



Induced magnetic field (IMF) of benzene

Blue: 5 ppm (5 μ T) iso-line
Red: -5 ppm (-5 μ T) iso-line

$$\left(\vec{B}_{ind}\right)_{\alpha} = -\sum_{\beta=1}^3 \sigma_{\alpha\beta} \left(\vec{B}_{ext}\right)_{\beta}$$

Chemistry Eur. J. 2004, 10, 4367





Computation of ^1H NMR chemical shift

$$\left(\vec{B}_{ind}\right)_\alpha = -\sum_{\beta=1}^3 \sigma_{\alpha\beta} \left(\vec{B}_{ext}\right)_\beta$$

$$\vec{B}_{ind} = \underbrace{\vec{B}_{ind}^0}_{\text{short range}} + \underbrace{\sum_i \vec{B}_{ind}^i}_{\text{long range}} \Rightarrow \sigma_{\alpha\beta} = \underbrace{\sigma_{\alpha\beta}^0}_{\sim 30 \text{ ppm}} + \sum_i \underbrace{\sigma_{\alpha\beta}^i}_{< 5 \text{ ppm}} + \underbrace{O\left(\frac{|\vec{B}_{ind}^{i \neq 0}|}{|\vec{B}_{ext}|}\right)}_{\sim 5 \cdot 10^{-6} \text{ ppm}}$$

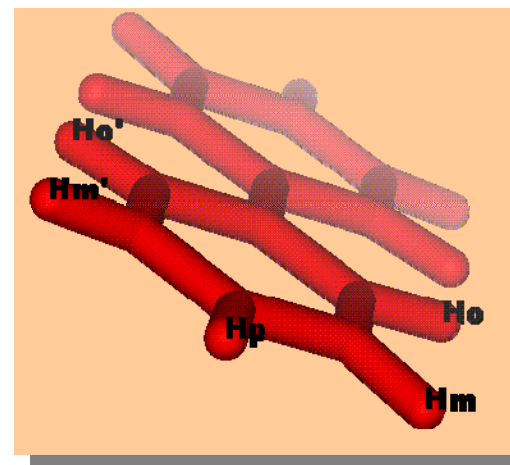
- Approach works for non-polar molecules
 - Explicit tests
 - Similar work for C_2H_2
(Pecul et al., Solid State NMR 1997, 8, 139)
- Does not work for
 - polar molecules (Martin et al., Org. Lett. 2001, 3, 3823)
 - intermolecular interactions (Caramori et al., J. Org. Chem. 2005, 70, 3242.)



Computational methodology



Proton Labels



IGLO PBE/IGLOIII/GEN-A2*

	single biphenyl	3 biphenyl	Single+ NICS of 18	Single+ NICS of 57	Expt.
H _p	0.00	0.00	0.00	0.00	0.00
H _m	0.27	0.03	0.57	0.43	0.41
H _{m'}	0.28	1.19	1.42	1.36	1.39
H _o	0.89	0.97	1.45	1.37	1.27
H _{o'}	0.88	0.06	0.60	0.58	0.49

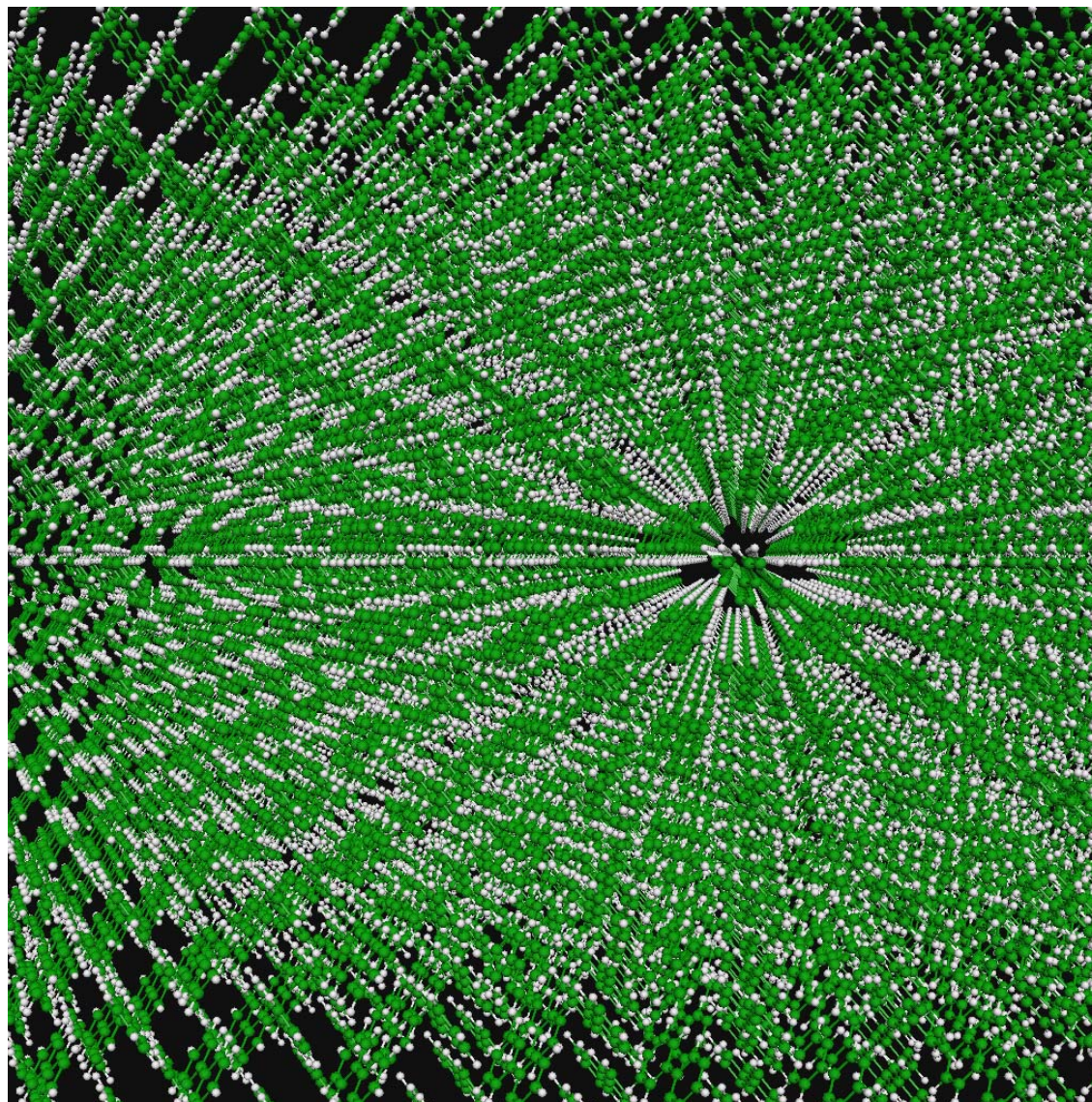
These
protons
exchange
when the
two rings
flip

values are in ppm

Isotropic shieldings referenced to $\sigma_{\text{iso}}(\text{para})$



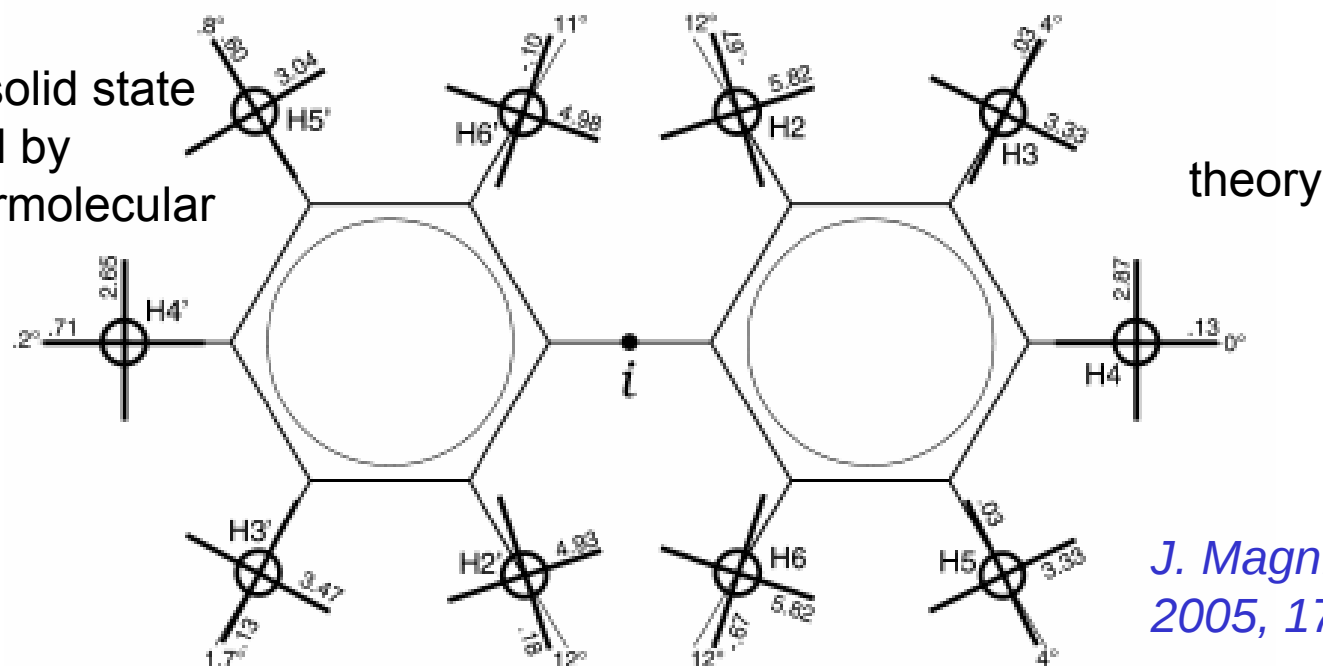
Cluster model of biphenyl





^1H NMR shielding tensor for isolated biphenyl

Experiment – solid state
NMR corrected by
calculated intermolecular
contributions



J. Magn. Res.
2005, 175, 52

Proton	method	isotropic	Principal axis components			Icosahedral representaion						difference
			11	22	33							
para	i.m.	0.00	-3.36	0.71	2.65	1.26	1.24	1.03	0.95	-2.33	-2.14	0.27
	q.ch.	0.00	-3.00	0.13	2.87	0.90	0.88	1.25	1.25	-2.14	-2.14	
meta	i.m.	-0.22	-3.40	0.14	3.26	0.90	3.25	-0.40	-0.24	-1.70	-1.81	0.13
	q.ch.	-0.28	-3.37	0.03	3.33	1.01	3.29	-0.47	-0.47	-1.68	-1.68	
ortho	i.m.	-0.90	-5.00	0.04	4.96	4.70	2.04	-0.98	-1.01	-2.19	-2.57	0.45
	q.ch.	-0.88	-5.16	-0.67	5.82	5.33	2.29	-1.56	-1.56	-2.25	-2.25	



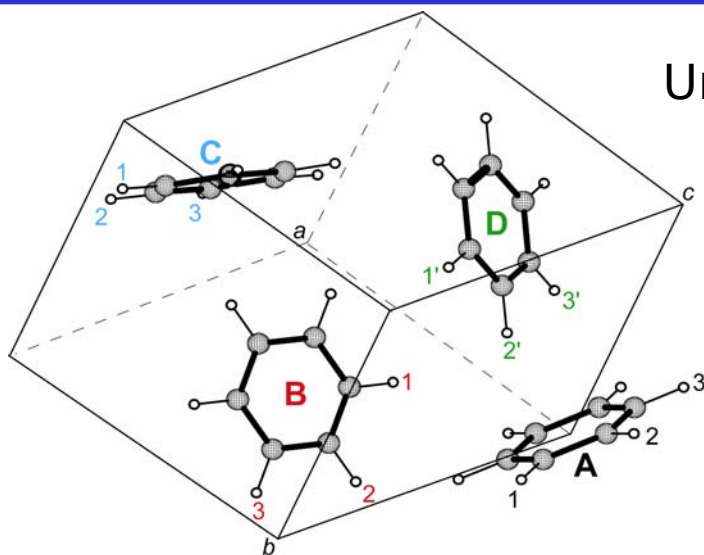
One fatal conclusion

*“The good news of this work is that there is no more a need to perform such (multiple pulse NMR on benzene) an experiment. Actually, proton shielding tensors are hardly anymore a reason to perform line-narrowing multiple pulse experiments. There are adequate, even superior, alternatives: first, single crystal deuteron NMR in very high applied fields [16] and, second, **calculation by the quantum chemical method explored and tested against experiment here**, perhaps supplemented by the old susceptibility method. After elimination of systematic errors, **these theoretical methods allow with reasonable effort to access proton shielding tensors on a sub-ppm accuracy level not only in the isolated molecule but also in the natural crystal environment**. In a forthcoming publication we shall give a fuller account of these methods and shall apply them to benzene (T. Heine, C. Corminboeuf, G. Grossmann, U. Haeberlen).”*

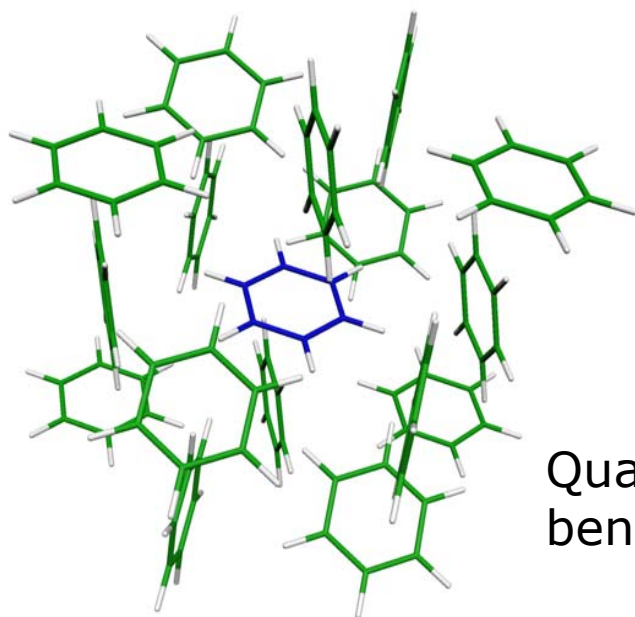
U. Haeberlen in *J. Magn. Res.* 2005, 175, 52



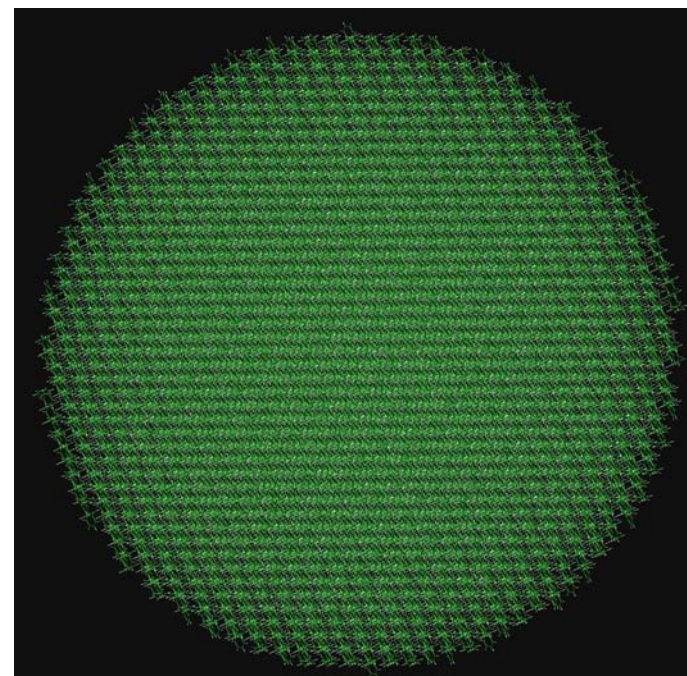
^1H NMR chemical shift of benzene



Unit cell contains 4 molecules



Long-range interactions of a cluster of 72 Å considered (13445 molecules)

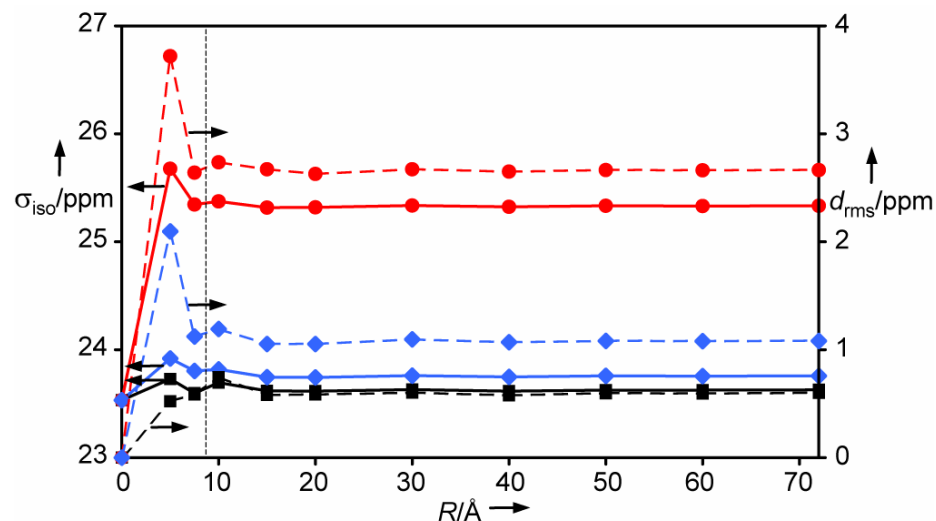


Angew. Chem., 2006, 118, 2006, 7450.

Quantum-chemical calculation of a cluster of 17 benzene molecules (204 atoms)

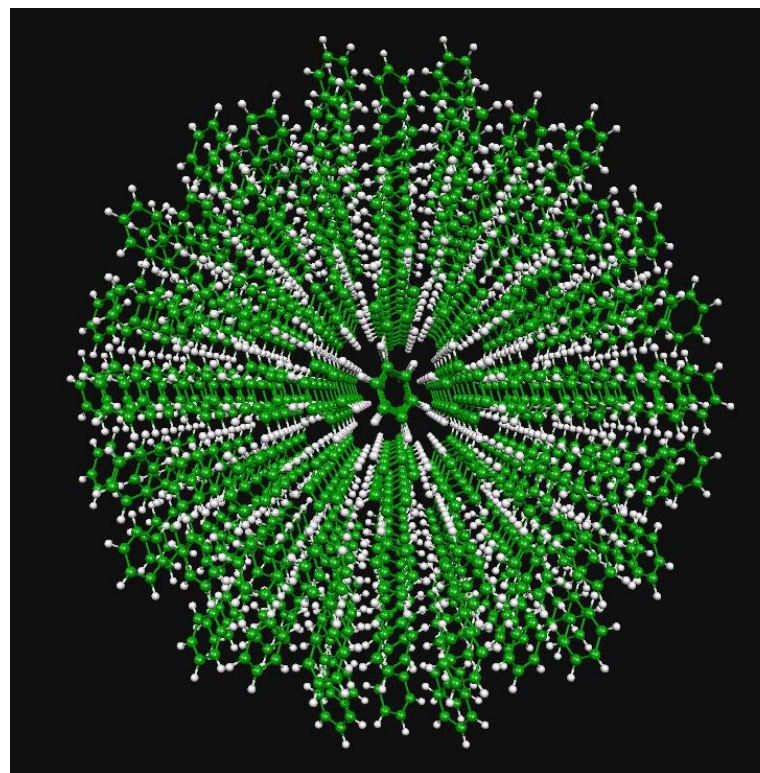


^1H NMR chemical shift of benzene



$$d_{rms} = \sqrt{\frac{6}{\sum_{i=1}^6 (\sigma_{i,R} - \sigma_{i,R=0}) / 6}}$$

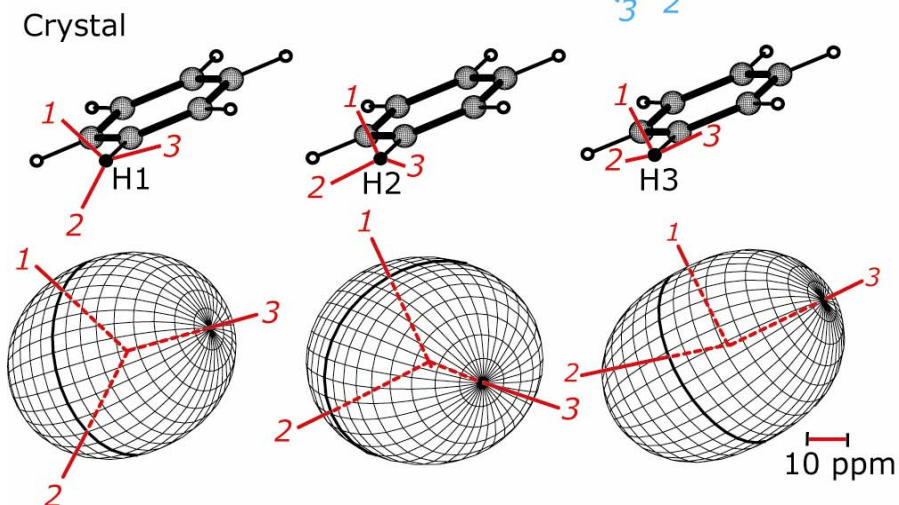
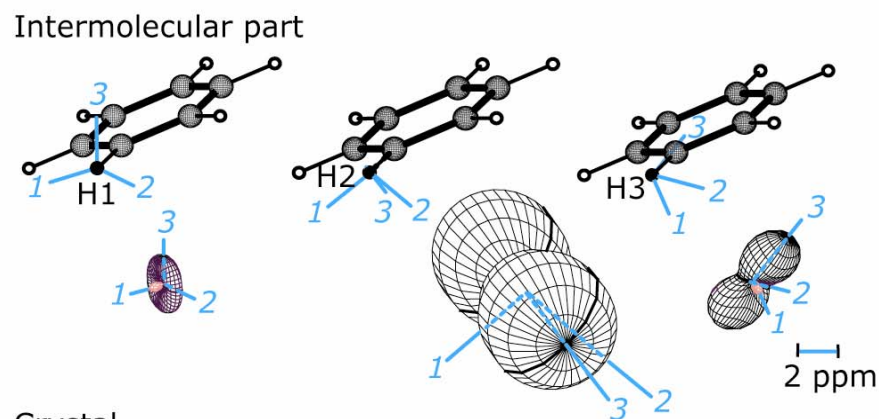
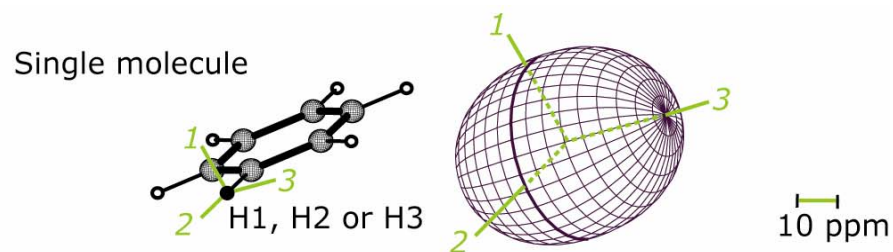
Three distinct protons
Shieldings differ considerably
20 Å sphere is needed:
293 molecules



Angew. Chem., 2006, 118, 2006, 7450.



^1H NMR chemical shift of benzene



	H1 / ppm	H2 / ppm	H3 / ppm
σ_{iso}	23.63	25.33	23.76
σ_{11}	21.03	20.67	19.97
σ_{22}	22.77	24.34	22.96
σ_{33}	27.08	30.99	28.35

Tensorial representation as suggested by Radeaglia.

T. Heine, C. Corminboeuf, G. Großmann, U. Haeberlen, Angew. Chem., 2006, 118, 2006, 7450.



Acknowledgments

- Gabriel Merino
- Clémence Corminboeuf
- Lyuben Zhechkov
- Gotthard Seifert
- Gisbert Grossmann
- Ulrich Häberlen
- Knut Vietze
- Serguei Patchkovskii
- Sergei Yurchenko
- Rafael Islas
- Agnieszka Kuc
- deMon and deMon-NMR developers
- VU developers
- Paul v. Ragué Schleyer

