



THE FRITZ HABER RESEARCH CENTER  
FOR MOLECULAR DYNAMICS

# Towards time-dependent density functional theory for near-field - electron dynamics



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# Acknowledgments & Thanks

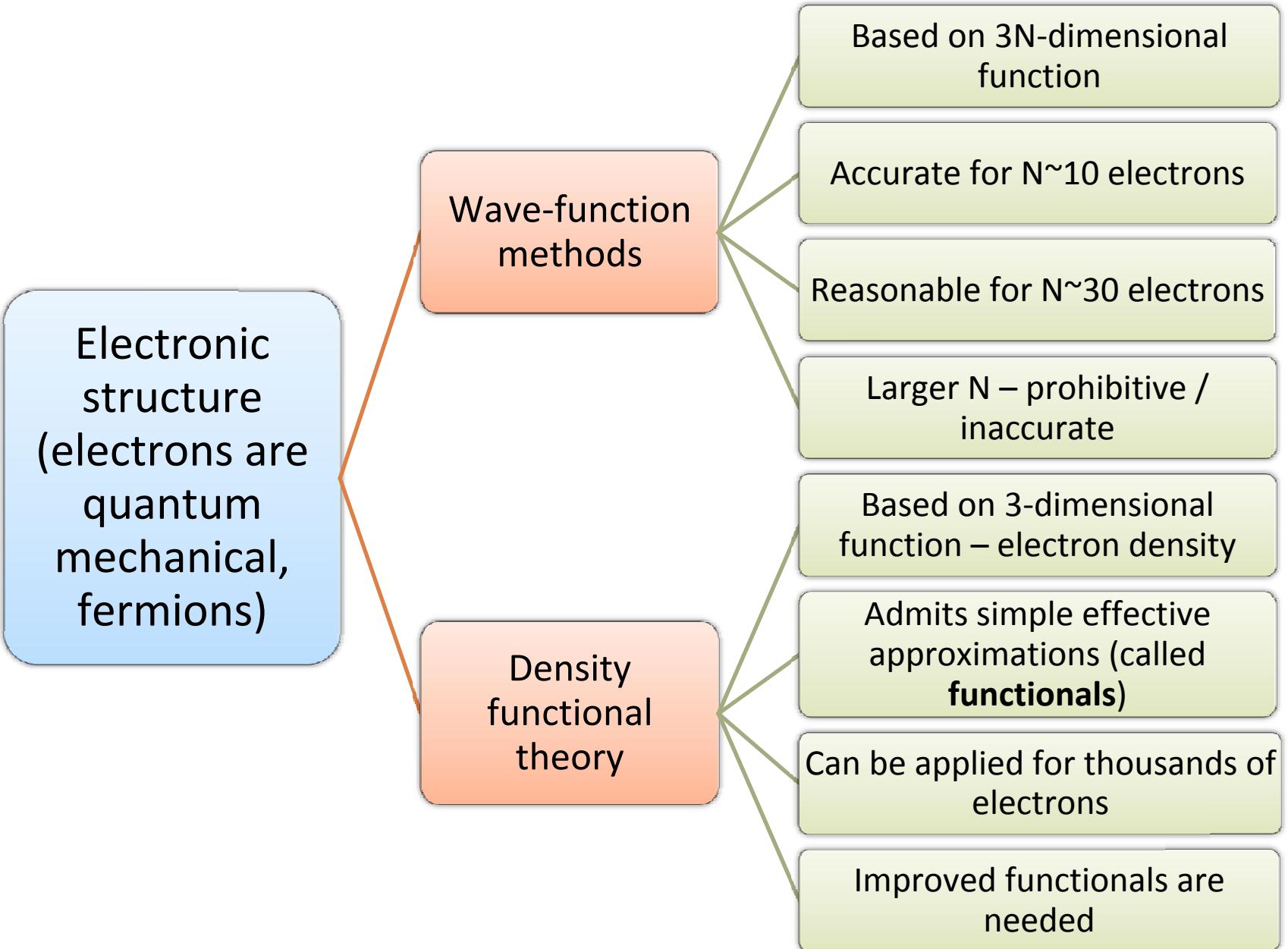
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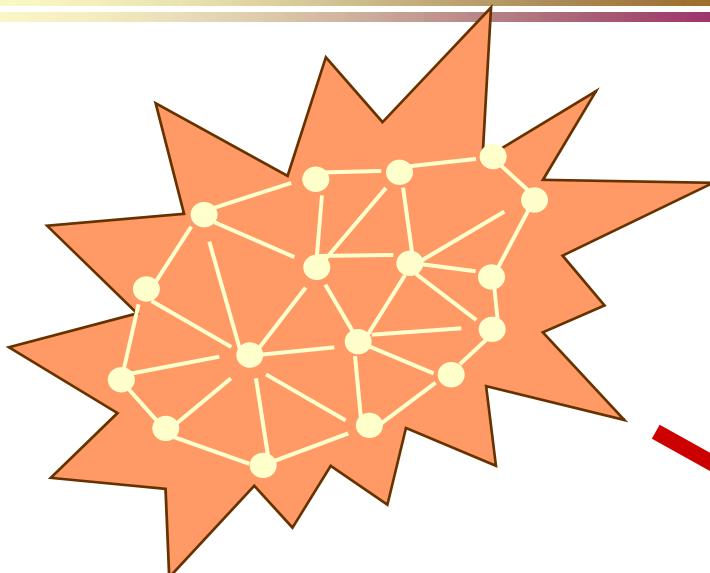
# Outline

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- Short introduction to DFT, TDDFT and near-field
- Combining DFT with near-field setup: problems
- Relation to self repulsion
- Removing long range self repulsion
- Construction of a “well-tempered” functional,  
based on 2 parameters
- Studies of near field-electron dynamics and local  
surface plasmons (LSPs) in metal nanoparticles
- Games: nano-optics based on LSPs



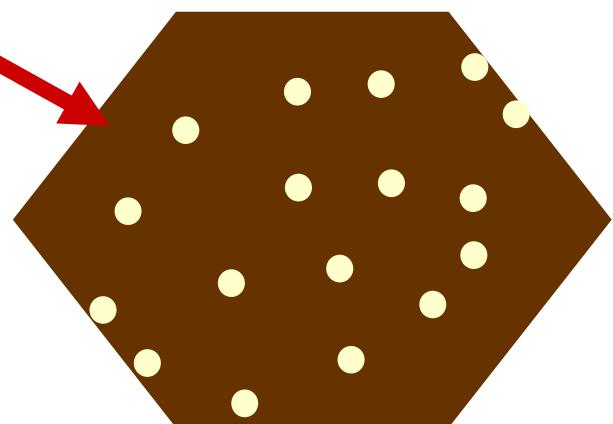
# DFT in a nutshell



Interacting elecs

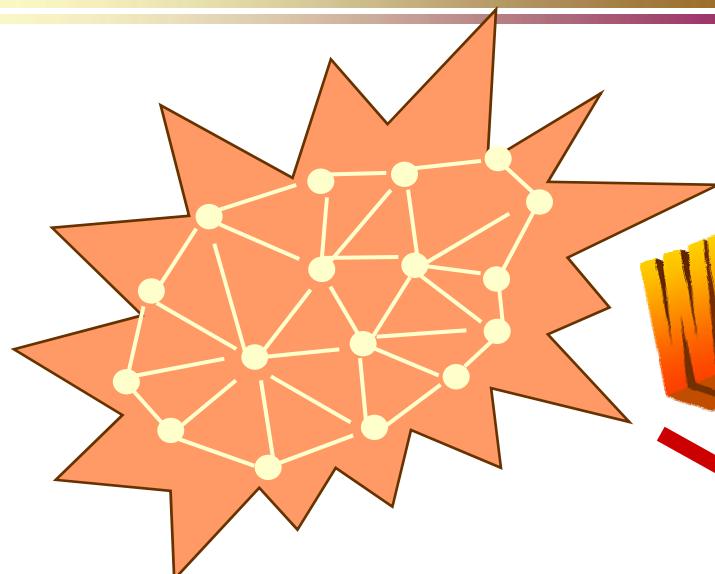
- Explicit of Coulomb law
- Approximate account of electron exchange and correlation
- Determines density  $n(r)$  directly: the wavefunction is not computed
- Determines the electronic energy directly

Non-interacting with same density



W. Kohn and L. J. Sham, Phys. Rev 140, A1133 (1965).

# Time-dependent DFT

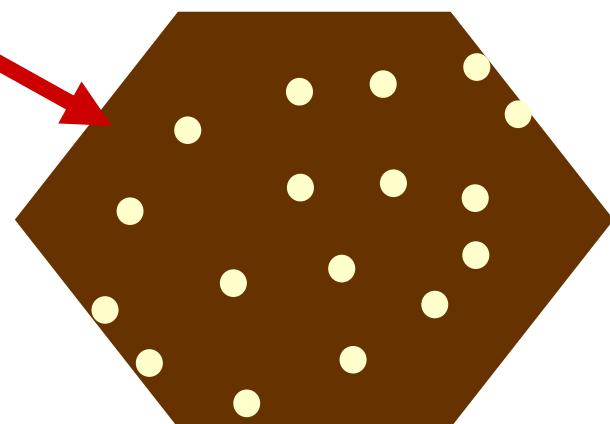


Interacting elecs

- Explicit of Coulomb law
- Approximate account of electron exchange and correlation
- Can be compatible with ground state
- Determines density  $n(r,t)$  directly:
- The wave-function is not computed

What about matrix elements?

Non-interacting with same density



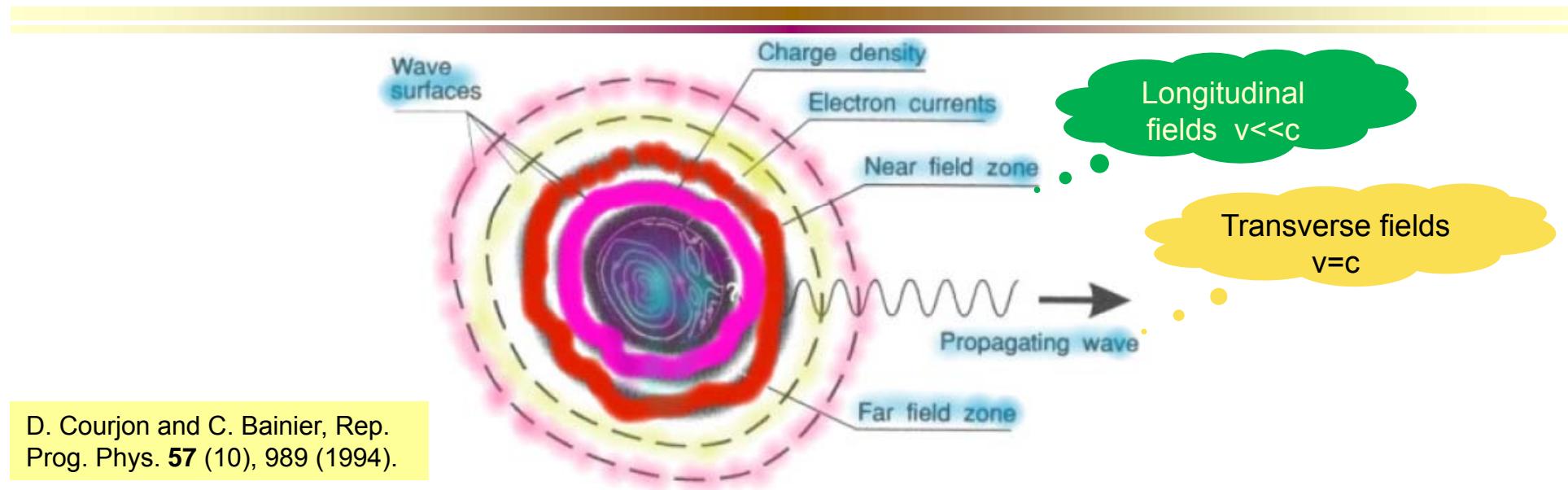
E. Runge and E. K. U. Gross, Phys. Rev. Lett. **52**, 997 (1984).

# Impact of DFT methods

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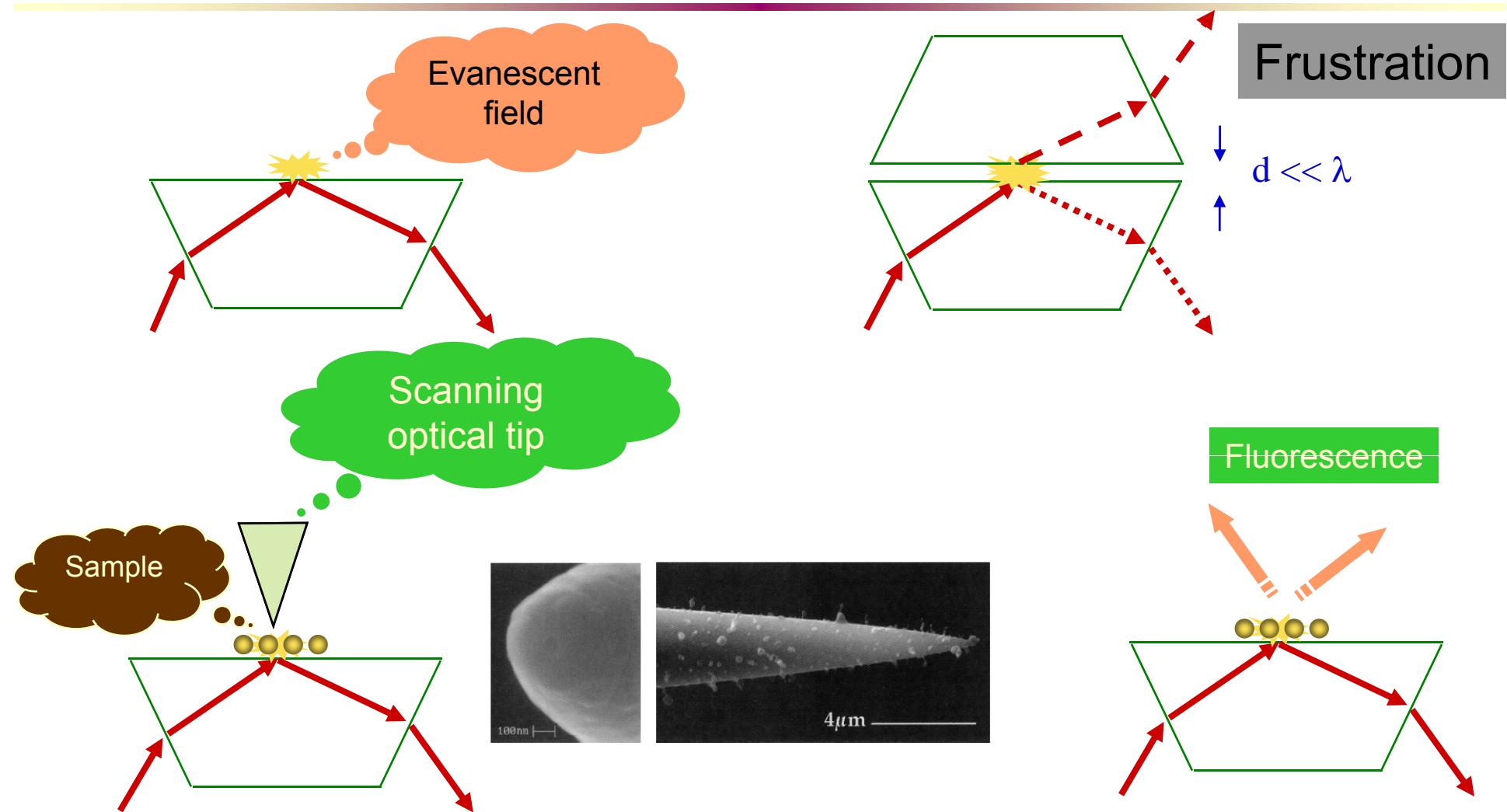
- DFT was embraced by the Chemistry community in mid 90's.
- It has since revolutionized all fields of chemistry
- Tremendously useful in biochemistry and materials science
- TDDFT is newer but is growing fast
- Leads to results comparable and often more reliable than wave-function methods
- Still, as I show both theories still need improvement
  - Dispersion interactions (van der Waals)
  - Polarizability and other static response properties
  - Incorrect charge distribution in weakly interacting systems,
  - Anions and their stability
  - Rydberg excitations

# Near-field on the nanoscale



- EM fields with optical frequencies yet change on a 10 nm length scale
  - Spectroscopy, including nonlinear
  - Microscopy
- Plasmonics:
  - Waveguides: Transport of EM energy on nm scale

# Near-field scanning optical microscopy

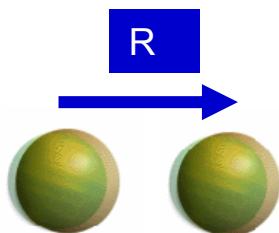


E. Betzig, M. Issacson, and A. Lewis, Appl. Phys. Lett. **51**, 2088 (1987).

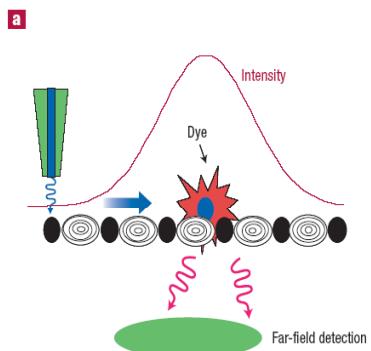
# EM energy transport on nm scale

- Local surface plasmon: collective excitation

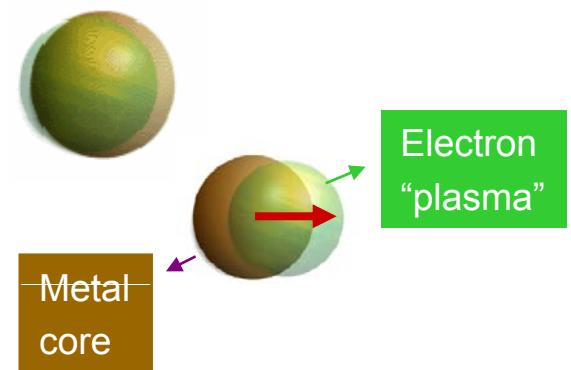
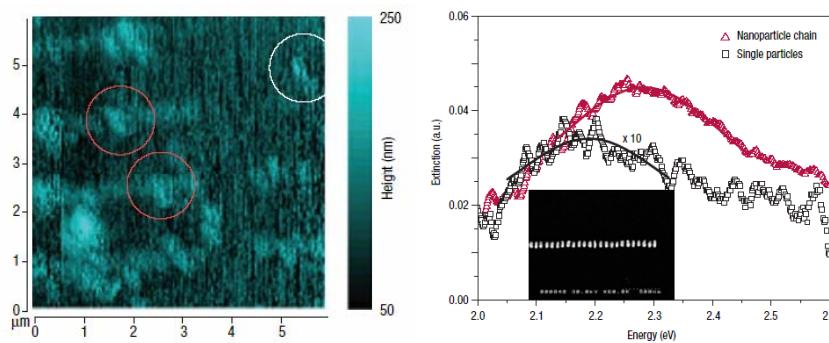
- Dipole coupling of two dots



Longitudinal  
coupling  $\alpha = 0$



Transverse  
coupling  $\alpha = 90^\circ$



$$C = \frac{d_1 d_2 (1 - 3 \cos^2 \alpha)}{R^3}$$

S. A. Maier, P. G. Kik, H. A. Atwater, S. Meltzer, E. Harel, B. E. Koel, and A. A. G. Requicha, Nature Mat. **2**, 229 (2003).

# Why TDDFT is a natural choice

- Maxwell's + Schrödinger equations

$$\begin{aligned}\varepsilon_0 \nabla \cdot \mathbf{E} &= \rho & \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \cdot \mathbf{B} &= 0 & \mu_0^{-1} \nabla \times \mathbf{B} &= \mathbf{j} + \frac{\partial \mathbf{E}}{\partial t}\end{aligned}$$

- Using potentials to describe the fields (Coulomb gauge):  $\mathbf{E} = -\dot{\mathbf{A}} - \nabla\phi \quad \mathbf{B} = \nabla \times \mathbf{A} \quad \nabla \cdot \mathbf{A} = 0$
- We have equations of motion:

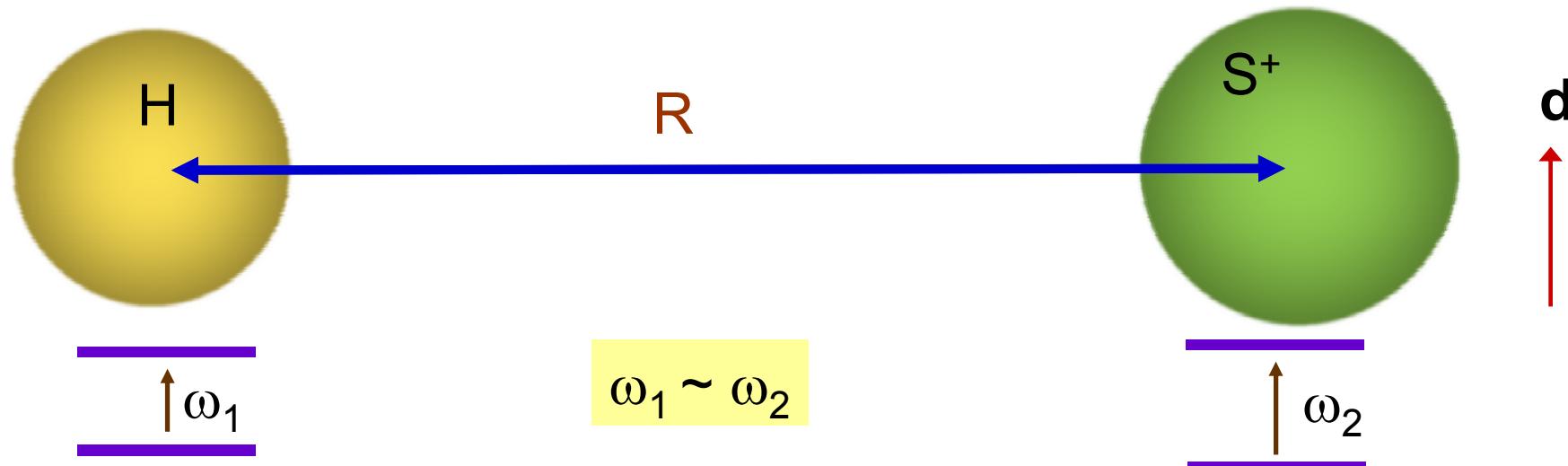
Instantaneous  
TD Poisson:  
TDDFT/TDCDFT

$$\begin{aligned}-\nabla^2 \phi(\mathbf{r}, t) &= \varepsilon_0^{-1} \rho(\mathbf{r}, t) & -\nabla^2 \mathbf{A} + \frac{1}{c^2} \frac{\partial^2 \mathbf{A}}{\partial t^2} &= \mu_0 \mathbf{j}_\perp \\ \mathbf{j}_\perp &= \mathbf{j} - \varepsilon_0^{-1} \nabla \dot{\phi} \\ i\dot{\Psi} &= \left\{ \sum_{i=1}^N \left( \hat{\mathbf{p}}_i - \frac{q_i}{c} \mathbf{A}(\hat{\mathbf{r}}_i, t) \right)^2 + q_i \phi(\hat{\mathbf{r}}_i, t) \right\} \Psi\end{aligned}$$

Usually can  
replace  $\mathbf{A}$  by  $\mathbf{A}_{\text{ext}}$   
( $\mu_0 \ll 1$ )

Retardation.  
Wave  
propagation  
 $R\omega \gg c$

# Dipole coupling theory



$$C = \frac{d_H^{01} d_{S^+}^{01}}{R^3}$$

Basically: two QM states:  $|H_{exc}S^+_{gs}\rangle, |H_{gs}S^+_{exc}\rangle$

$$H = \begin{pmatrix} \omega_1 & C \\ C & \omega_2 \end{pmatrix} = \bar{E} + \begin{pmatrix} \Delta & C \\ C & -\Delta \end{pmatrix}$$

$$\bar{E} = \underbrace{\frac{\omega_1 + \omega_2}{2}}_{Average} \quad \underbrace{2\Delta = \omega_1 - \omega_2}_{mismatch}$$

$$E_{\pm} = \bar{E} \pm \Omega \quad \Omega = \sqrt{\Delta^2 + C^2}$$

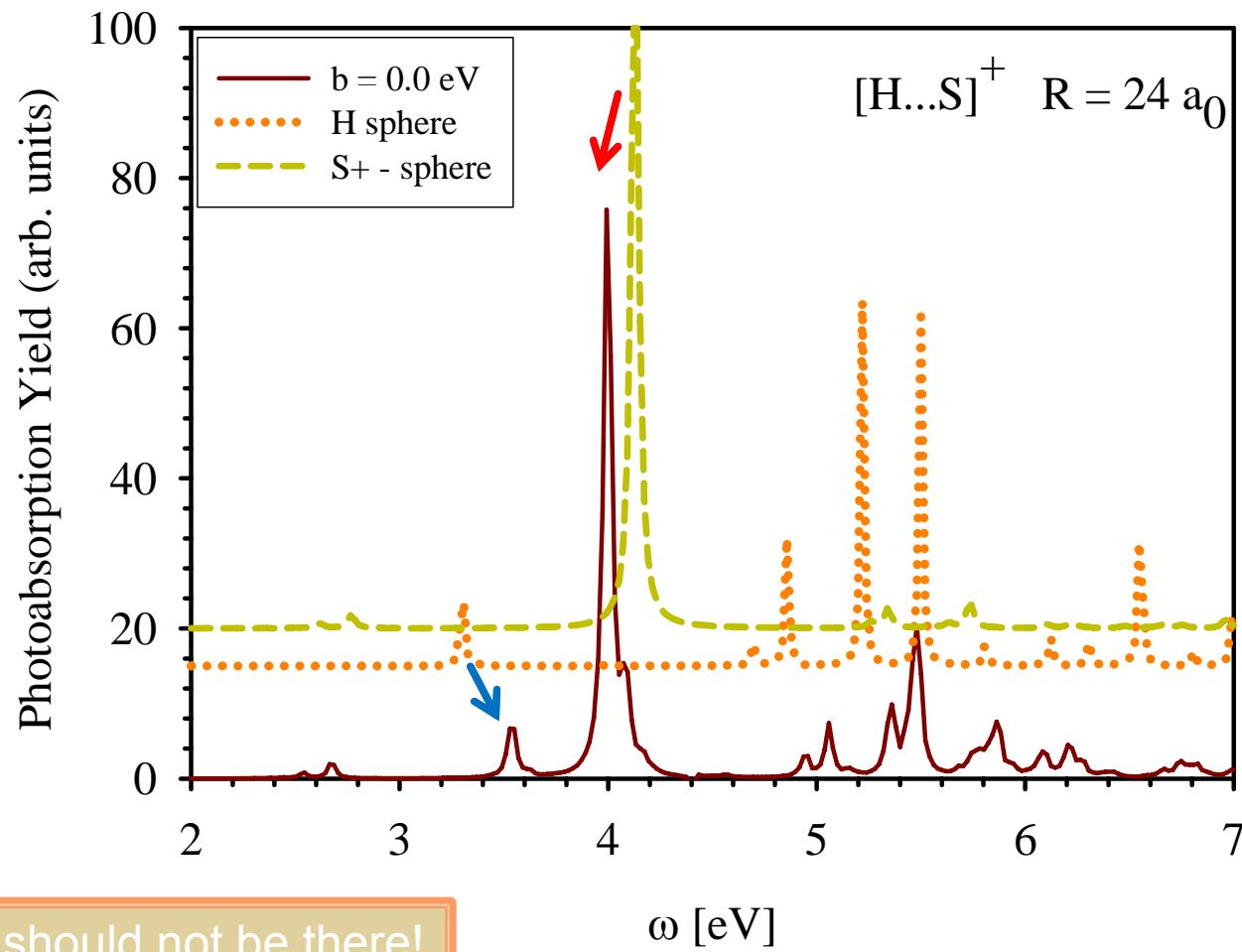
$$C \ll \Delta \quad \rightarrow \quad \Omega = \Delta + \frac{C^2}{2\Delta}$$

$$C \gg \Delta \quad \rightarrow \quad \Omega = C$$

$$\begin{pmatrix} D_+ \\ D_- \end{pmatrix} = \begin{pmatrix} \cos \theta/2 & \sin \theta/2 \\ -\sin \theta/2 & \cos \theta/2 \end{pmatrix} \begin{pmatrix} d_H \\ d_{S^+} \end{pmatrix}$$

$$\tan \theta = \frac{C}{\Delta}$$

# Spurious splitting



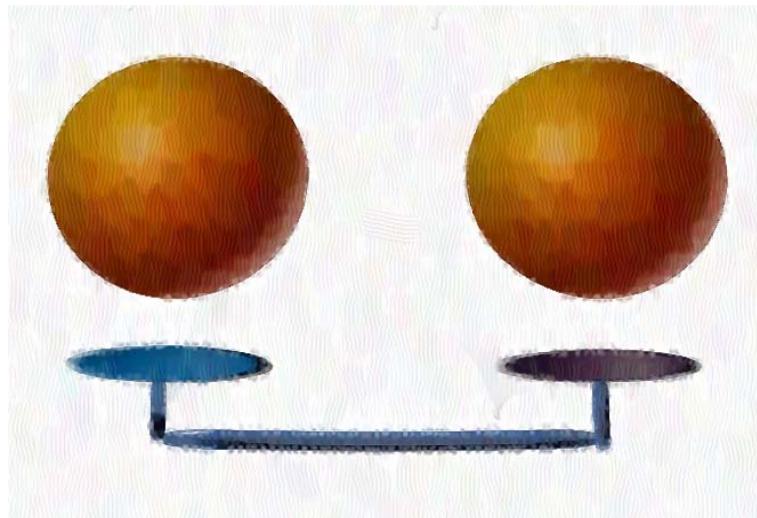
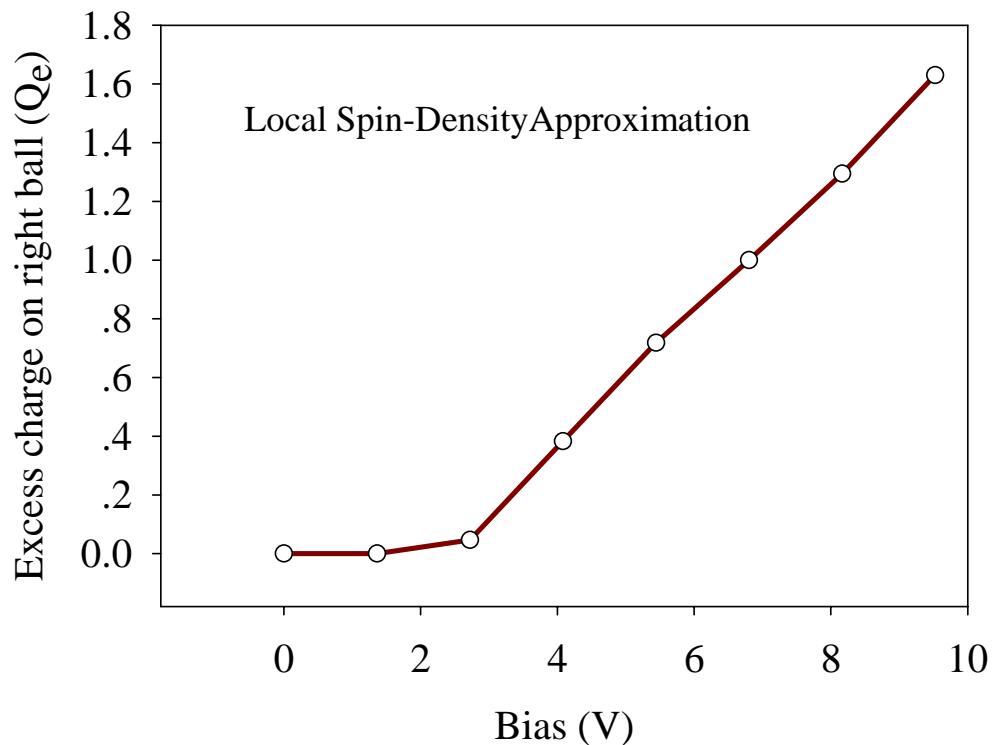
# Source of problem: DFT

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- Incorrect charge distribution
- The spheres share partial charges
- This makes the HOMO of the system highly nonlocal
- In TDDFT: too much sensitivity in one sphere concerning the other.

Weakly coupled systems have integer number of electrons

# LDA/GGA violate charge quantization



2 jellium balls  
 $r_s=2.2$   
20 elecs each

In the case of the H and S<sup>+</sup> spheres,  
the charge  
On each sphere was non-integer,  
although they were distant

## Self repulsion

- An electron is repelled by itself
- The most severe is the self-interaction in the Hartree energy

## DFT: the non-physical behavior impairs

- e-Density in weakly-coupled systems (charge quantization)
- Static response (polarizability, etc.)
- Prediction of stability of anions (especially atoms)

## Will of course affect TDDFT!

- Charge transfer excitations (Dreuw + Head-Gordon)
- Rydberg states
- Spurious shifts resulting from unphysical ultra-nonlocality

# A DFT with correct long-range behavior

- The XC Energy is defined as:

$$E_{XC}[n] = T[n] - T_s[n] + U[n] - E_H[n]$$

- Can write it, using adiabatic connection, as:

$$E_{XC}[n] = \int_0^\infty \left\langle \Psi_{\gamma'} \left| \hat{W}_{\gamma'} \right| \Psi_{\gamma'} \right\rangle d\gamma' - E_H[n]$$

$$\hat{W}_\gamma = \frac{1}{2} \sum_{i \neq j} w_\gamma(\hat{r}_{ij}); \quad w_\gamma(r) = e^{-\gamma r}$$

- Where:

$$\Psi_\gamma = \text{gs with } n(\mathbf{r}) \text{ under } u_\gamma(r) = \frac{1 - e^{-\gamma r}}{r}$$

J. Harris and R. O. Jones, J. Phys. F 4, 1170 (1974).

D. C. Langreth and J. P. Perdew, Sol. Stat. Comm. 17, 1425 (1975).

O. Gunnarsson and B. I. Lundqvist, Phys. Rev. B 13, 4274 (1976).

W. Yang, J. Chem. Phys. 109, 10107 (1998).

# Evaluating the integral

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- An approximation:

$$\begin{aligned}\int_0^\infty \langle \Psi_{\gamma'} | \hat{W}_{\gamma'} | \Psi_{\gamma'} \rangle d\gamma' &= \int_0^\gamma \langle \Psi_{\gamma'} | \hat{W}_{\gamma'} | \Psi_{\gamma'} \rangle d\gamma' + \int_\gamma^\infty \langle \Psi_{\gamma'} | \hat{W}_{\gamma'} | \Psi_{\gamma'} \rangle d\gamma' \\ &\approx \int_0^\gamma \langle \Psi_0 | \hat{W}_{\gamma'} | \Psi_0 \rangle d\gamma' + \int_\gamma^\infty \langle \Psi_\infty | \hat{W}_{\gamma'} | \Psi_\infty \rangle d\gamma'\end{aligned}$$

- Leading to:

$$\begin{aligned}\int_0^\infty \langle \Psi_{\gamma'} | \hat{W}_{\gamma'} | \Psi_{\gamma'} \rangle d\gamma' &\approx \langle \Psi_0 | \hat{U}_\gamma | \Psi_0 \rangle + \langle \Psi_\infty | \hat{Y}_\gamma | \Psi_\infty \rangle \\ \hat{U}_\gamma &= \frac{1}{2} \sum_{i \neq j} u_\gamma(\hat{r}_{ij}) \quad \hat{Y}_\gamma = \frac{1}{2} \sum_{i \neq j} y_\gamma(\hat{r}_{ij}) \\ u_\gamma(r) &= (1 - e^{-\gamma r})/r \quad y_\gamma(r) = e^{-\gamma r}/r\end{aligned}$$

# The approximation is exact ?!

$$E_{XC} [n] \approx \langle \Psi_0 | \hat{U}_\gamma | \Psi_0 \rangle + \langle \Psi_\infty | \hat{Y}_\gamma | \Psi_\infty \rangle - E_H [n]$$
$$y_\gamma (r) = e^{-\gamma r} / r \quad u_\gamma (r) = (1 - e^{-\gamma r}) / r$$

The error in the approximation is:

$$\Delta E_{XC}^\gamma = [T[n] + \langle \Psi_\infty | \hat{U}_\gamma | \Psi_\infty \rangle] - [T_s[n] + \langle \Psi_0 | \hat{U}_\gamma | \Psi_0 \rangle]$$

when  $\gamma = 0$        $\Delta E_{XC}^{\gamma=0} = T[n] - T_s[n] \geq 0$

when  $\gamma = \infty$      $\Delta E_{XC}^{\gamma=\infty} = E_c[n] \leq 0$

Conclusion: There exists  $0 \leq \gamma \leq \infty$  for which  
the approximation is Exact

# Summary of theory

- Turn off the Coulomb interaction from the inside out
- The following is the *exact* Kohn-Sham energy functional

$$E_{v,N}[n] = T_s[n] + E_{ext}[n] + E_H[n] + K_X^\gamma[n] + E_{XC}^\gamma[n]$$

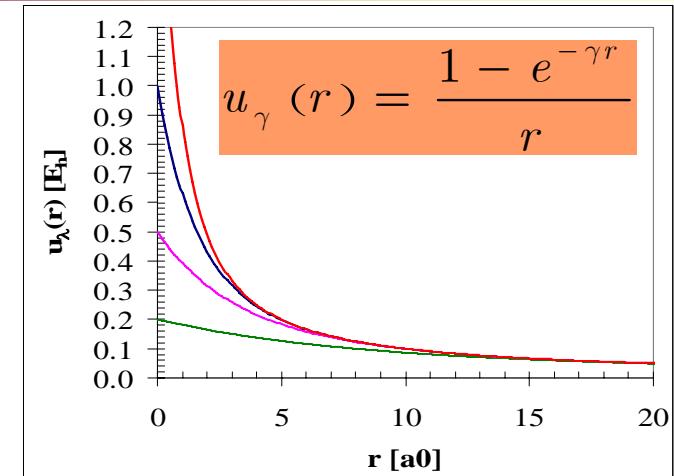
$$K_X^\gamma[n] = \frac{1}{2} \int \left| P[n](\mathbf{r}, \mathbf{r}') \right|^2 u_\gamma(|\mathbf{r} - \mathbf{r}'|) d^3r d^3r'$$

$$E_{XC}^\gamma[n] = \langle \Psi_\infty | \hat{Y}_\gamma | \Psi_\infty \rangle - \frac{1}{2} \int n(\mathbf{r}) n(\mathbf{r}') y_\gamma(|\mathbf{r} - \mathbf{r}'|) d^3r d^3r'$$

$$= \frac{1}{2} \int [g(\mathbf{r}, \mathbf{r}') - 1] n(\mathbf{r}) n(\mathbf{r}') y_\gamma(|\mathbf{r} - \mathbf{r}'|) d^3r d^3r'$$

$$y_\gamma(r) = \frac{e^{-\gamma r}}{r} \quad \Psi_\infty = \text{exact wf}$$

- Need approximations for  $\gamma[n]$ ,  $E_{XC}^\gamma[n]$



Related prior work:

- Savin in *Recent Advances in Density Functional Methods Part I*, edited by D. P. Chong (World Scientific, Singapore, 1995), p. 129.
- Hirao et al J. Chem. Phys. 115 (8), 3540 (2001).

# $\gamma=1$ Approximation

- We do not know the n dependence of  $\gamma$
- Let's take a constant  $\gamma[n] = \text{const} = 1/a_0^{-1}$

$$\begin{aligned} E_{XC}^\gamma[n] &= \langle \Psi_\infty | \hat{Y}_\gamma | \Psi_\infty \rangle - \frac{1}{2} \int n(\mathbf{r}) n(\mathbf{r}') y_\gamma(|\mathbf{r} - \mathbf{r}'|) d^3r d^3r' \\ &\approx \int \varepsilon_{XC}^\gamma(n(\mathbf{r})) n(\mathbf{r}) d^3r \end{aligned}$$

$$\varepsilon_{XC}^\gamma = \varepsilon_X^\gamma + \varepsilon_C^\gamma$$

$\varepsilon_X^\gamma$  = known analytical Yukawa XE per particle for HEG

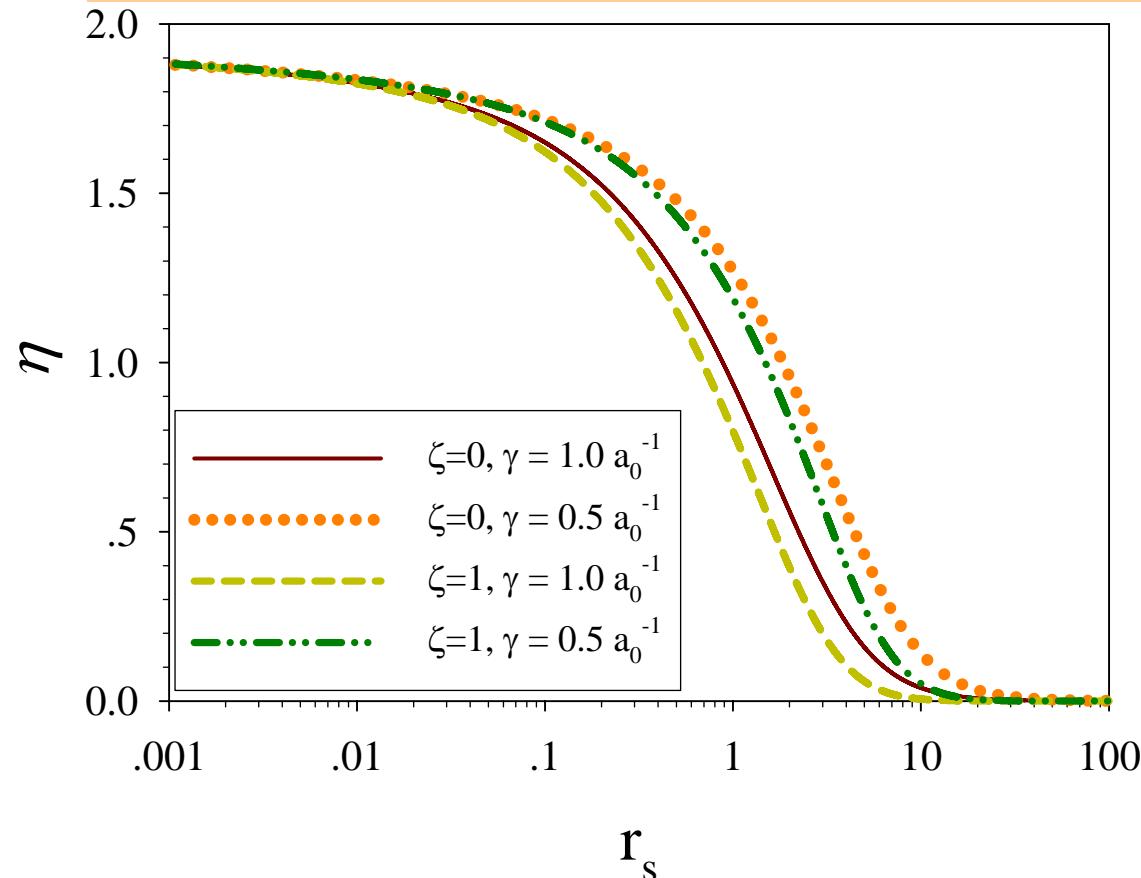
$\varepsilon_C^\gamma = \eta \varepsilon_{LDA}^{HEG}$  = Remaining CE per particle for HEG

$$E_X = \underbrace{K_X^\gamma}_{\substack{\text{nonlocal} \\ \text{c-Yukawa X}}} + \underbrace{\int \varepsilon_X^\gamma(n) n d^3r}_{\text{Local Yukawa X}}$$

Caveat: Not exact for HEG!

# The value of $\eta$ for HEG

$$\eta = \frac{1}{2\varepsilon_c^{LDA}} \int \left(1 - g^{HEG}(\mathbf{r} - \mathbf{r}')\right) n(\mathbf{r}) n(\mathbf{r}') y_\gamma(|\mathbf{r} - \mathbf{r}'|) d^3r d^3r'$$

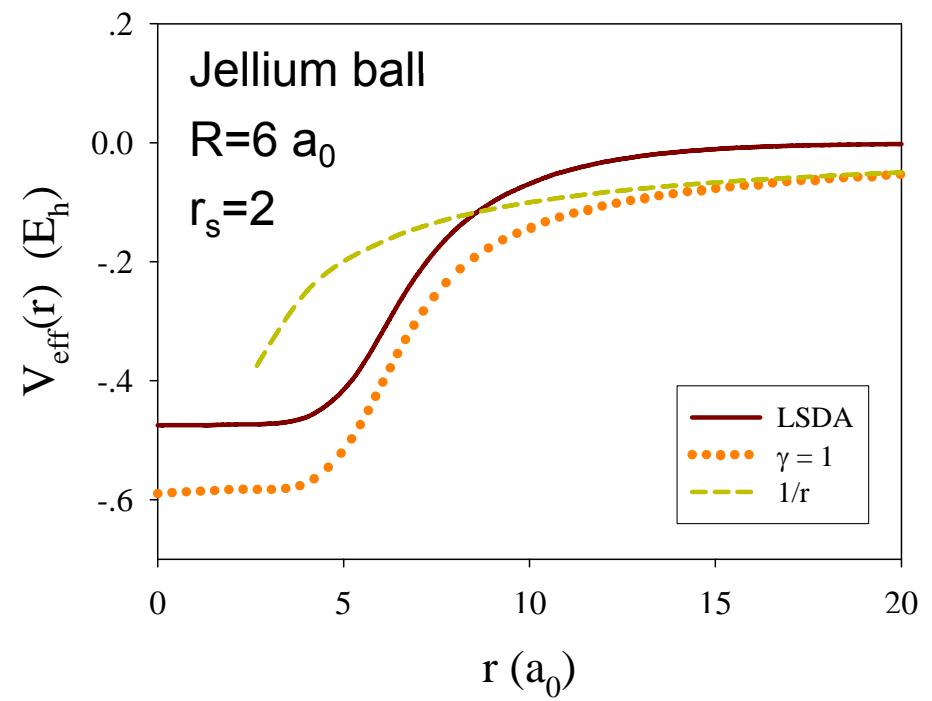
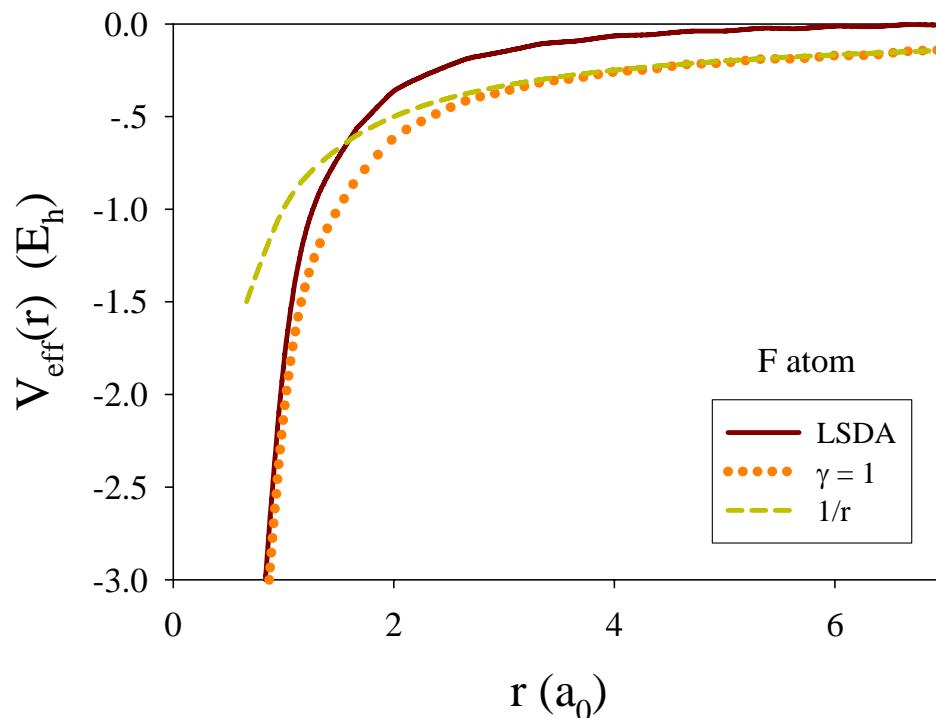


R. Baer E. Livshits and D. Neuhauser, Chem. Phys. 329, 266 (2006)

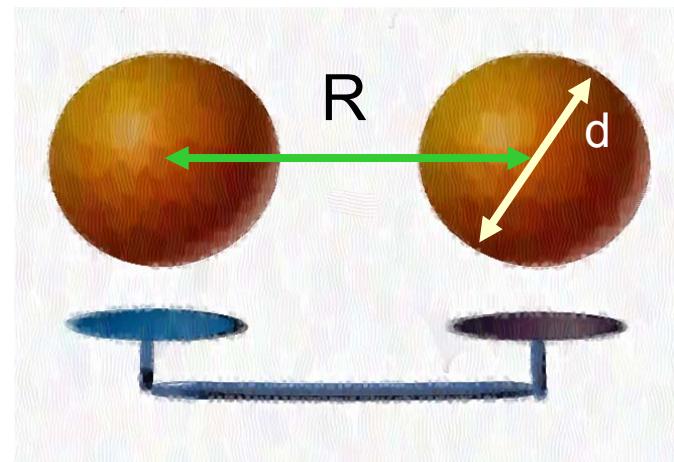
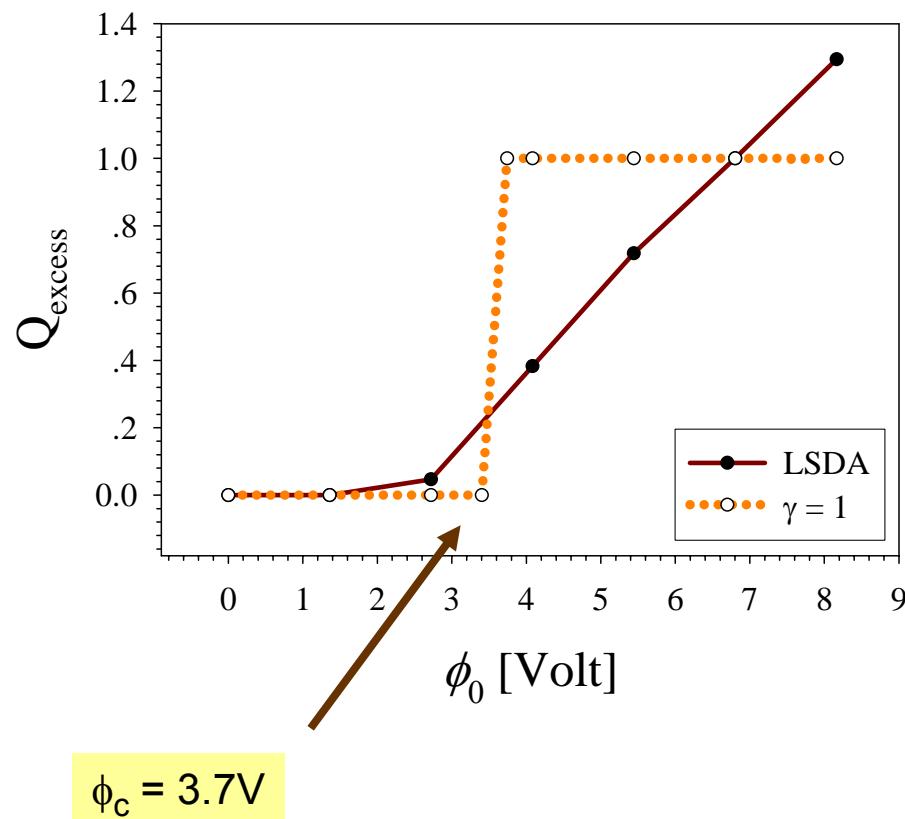
Pair correlation function taken from:  
P. Gori-Giorgi and J. P. Perdew, Phys. Rev. B 66, 165118 (2002).

# Correct asymptotic potential

The asymptotic effective potential of neutral system should be  $\rightarrow -1/r$



# Charge transfer under bias: quantization



$$\phi_c \approx IP - EA - \frac{1}{R - d}$$

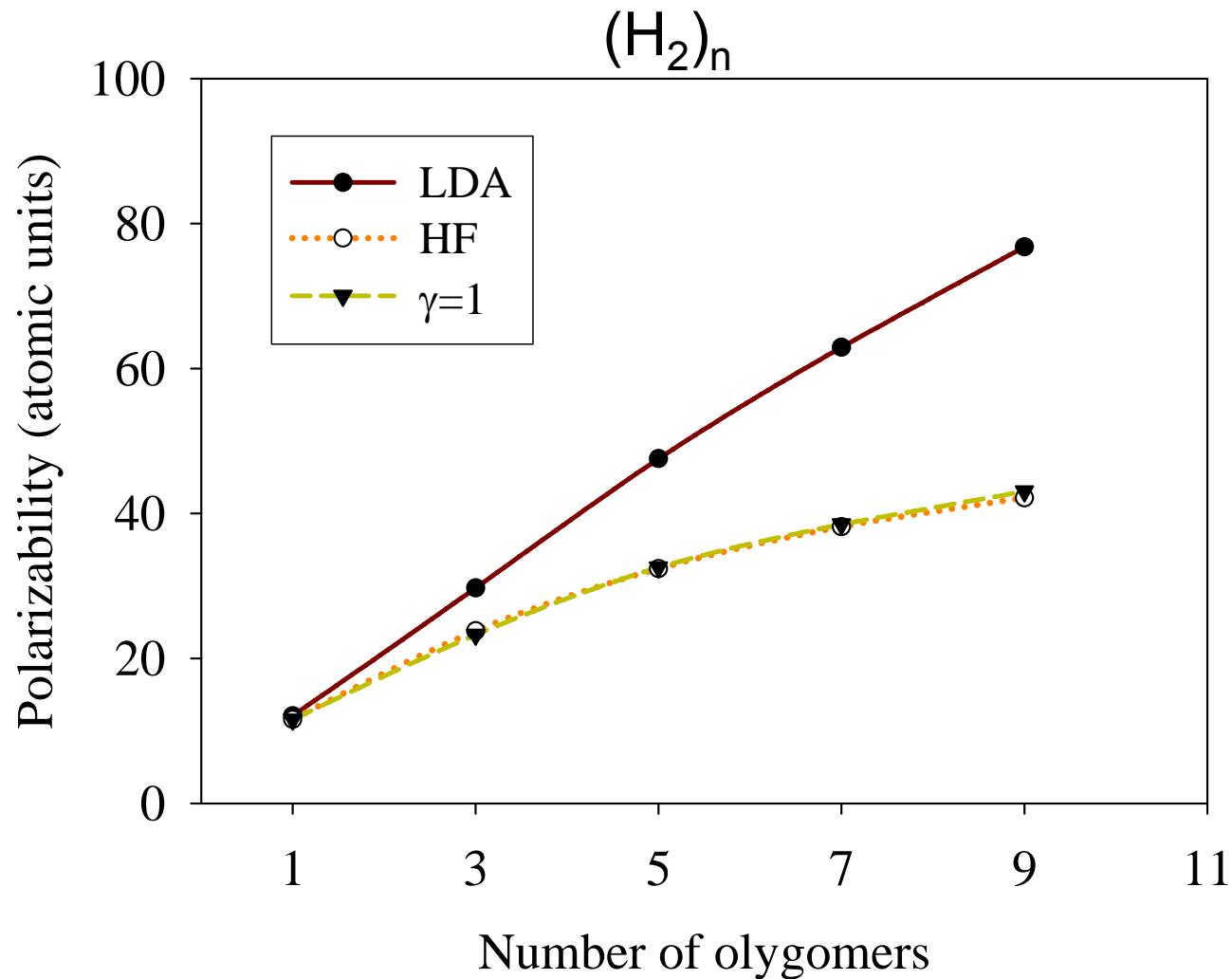
$$R = 28a_0 \quad d = 12a_0$$

$\Delta\text{SCF}$ (eV)			HOMO (eV)		
IP	EA	$\Phi_c$	IP	EA	$\Phi_c$
5.6	0.5	3.5	6.2	0.8	3.7

# Chemical Bond, Atomic EA

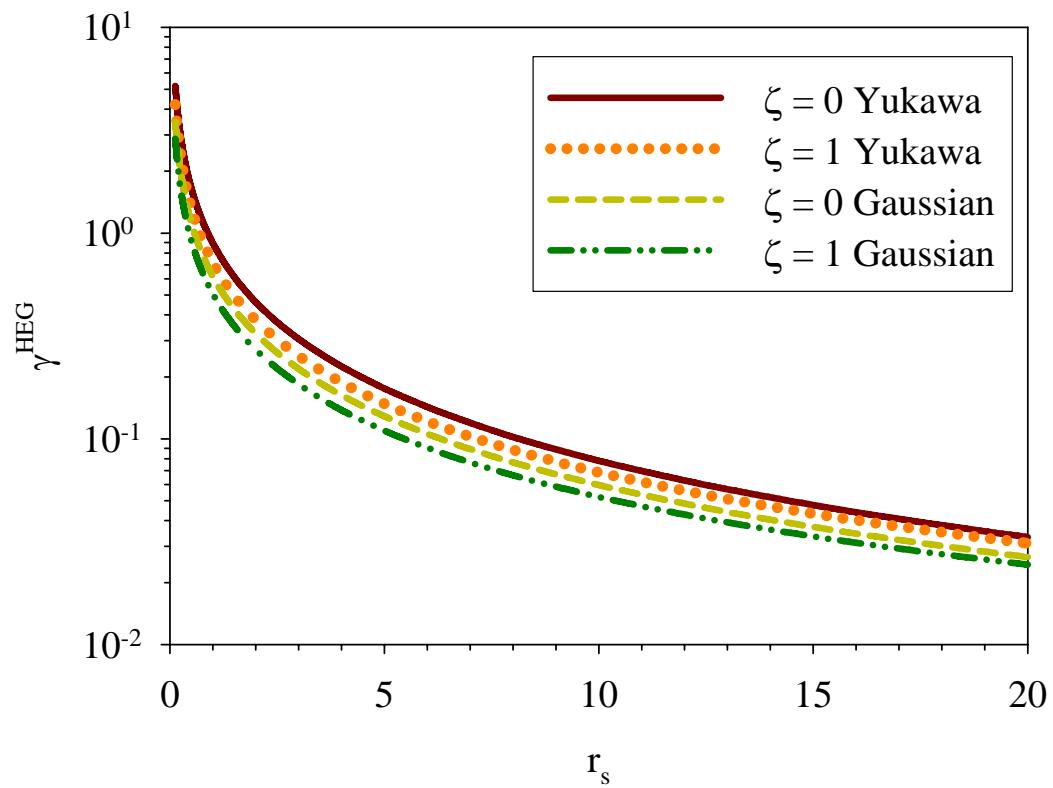
Atom (X)	$\Delta E (X_2)$ kcal/mol	$R_e (X_2)$ Angstrom	$\omega_e (X_2)$ $\text{cm}^{-1}$	EA (X) eV
C	Exp. 145 $\gamma=1$ 132 LSDA 169	1.242 1.27 1.25	1855 1810 1770	1.26 1.33
N	Exp. 225 $\gamma=1$ 223 LSDA 256	1.098 1.06 1.089	2358 2540 2520	Unstable Unstable
O	Exp. 118 $\gamma=1$ 122 LSDA 167	1.208 1.14 1.20	1580 1640 1590	1.46 1.50
F	exp. 37 $\gamma=1$ 35 LSDA 75	1.412 1.330 1.390	916 1200 1000	3.40 3.73

# Polarizability



# Enforce compatibility with HEG

- The exact HEG parameter:  $\gamma_{\text{HEG}}(r_s)$   
 $\eta(\gamma_{\text{HEG}}(r_s), r_s) = 1$
- Can use for molecule
- Get a theory which
  - has correct long range
  - Compatible with HEG
- Caveats:
  - Can be absurd
  - Or: has small effect



# 2 parameter Semiempirical functional

$$E_{XC}[n] = w\epsilon_X^\gamma(n) + K^\gamma[n] + E_c^{LYP}$$

Fit to atomization energy and bond lengths [G2(1) database of 55 molecules, using QCHEM®. cc-pVTZ basis.] Obtaining:  $\gamma=0.5$  and  $w=0.9$

Atomization energy	BNL-LYP	B3LYP
Average Error (kcal)	(-16) +2.1 (+15)	(-9) +2.7 (16)
RMS Error (kcal)	5.8	4.6
Average Relative Error	-1.2%	-1.5%
RMS Average Relative Error	6.8%	4.9%

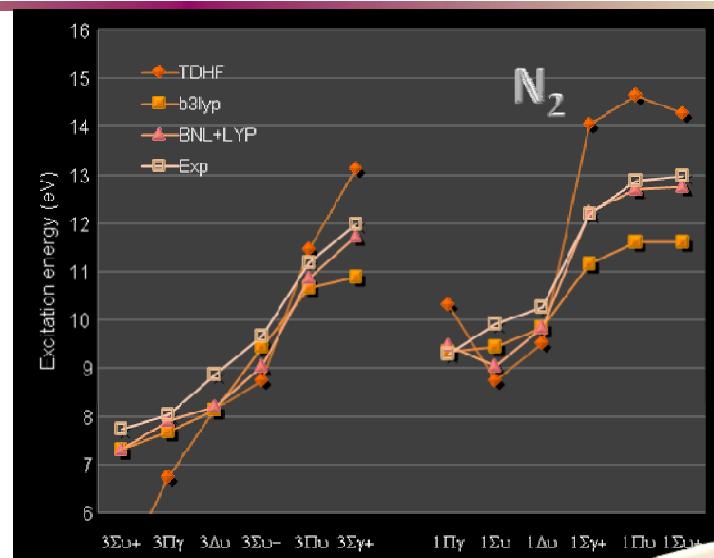
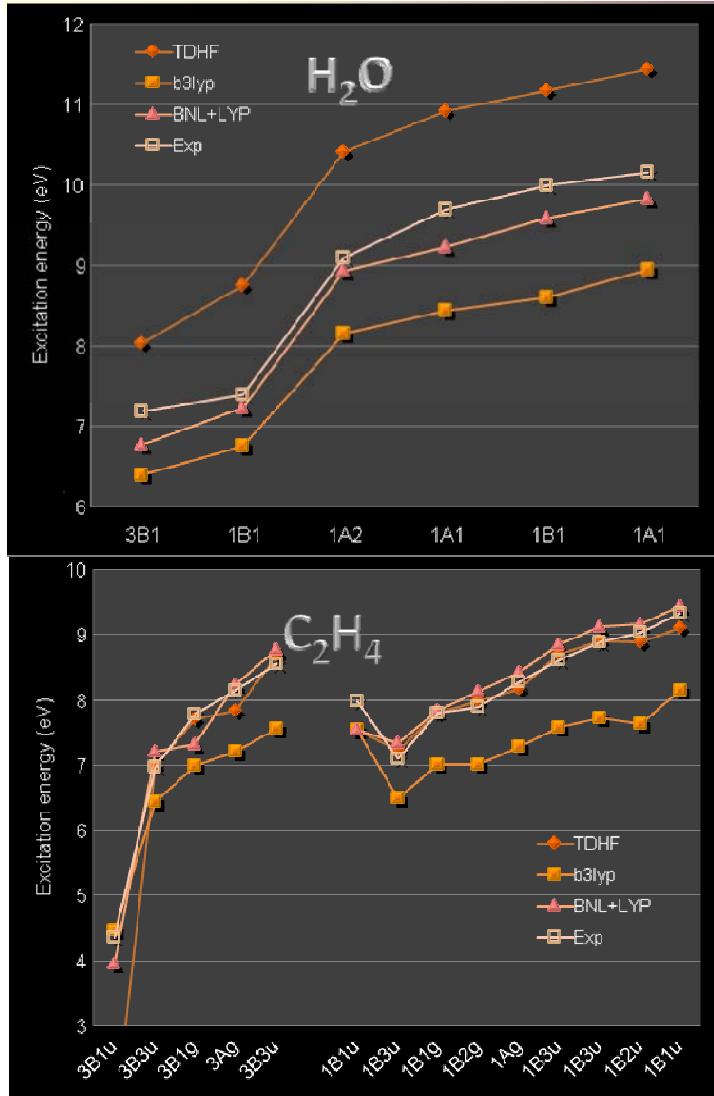
Bond lengths	BNL-LYP	B3LYP
Average Error (A)	(-0.07) +0.01 (+0.07)	(-0.02) +0.01 (0.05)
RMS Error (A)	+0.02	+0.01
Average Relative Error	+1.1%	0.7%
RMS Average Relative Error	1.7%	0.9%

# IP's and EA's

IP	Experiment	BNL-LYP		B3LYP	
		by ΔSCF	by HOMO	by ΔSCF	by HOMO
<b>BeH</b>	8.2	8.3	8.2	8.4	16.8
<b>CH</b>	10.6	10.8	10.8	10.9	6.9
<b>NH</b>	13.5	13.4	13.2	13.5	9.0
<b>OH</b>	13.0	16.0	12.8	16.0	8.5
<b>CN</b>	13.6	15.6	14.3	15.0	10.4

EA	Experiment	BNL-LYP		B3LYP	
		by ΔSCF	by HOMO	by ΔSCF	by HOMO
<b>BeH</b>	0.7	0.1	0.4	0.2	unbound
<b>CH</b>	1.2	0.7	1.1	0.7	unbound
<b>NH</b>	0.4	-0.6	0.4	-0.6	unbound
<b>OH</b>	1.8	0.6	0.9	0.6	unbound
<b>CN</b>	3.9	3.9	4.4	3.6	0.4

# Vertical excitations with new functional



## Oscillator strengths

$\text{C}_2\text{H}_4$	TDHF	B3LYP	BNL-LYP	Exp
$^1\text{B}_{1u}$	39.9	26.14	36.71	29
$^1\text{B}_{3u}$	8.56	5.75	7.61	4

For each  
func

$\text{N}_2$	TDHF	B3LYP	BNL-LYP	Exp
$^1\Pi_u$	0.0121	0.0729	0.1409	0.243
$^1\Sigma_u$	0.6283	0.031	0.2865	0.279

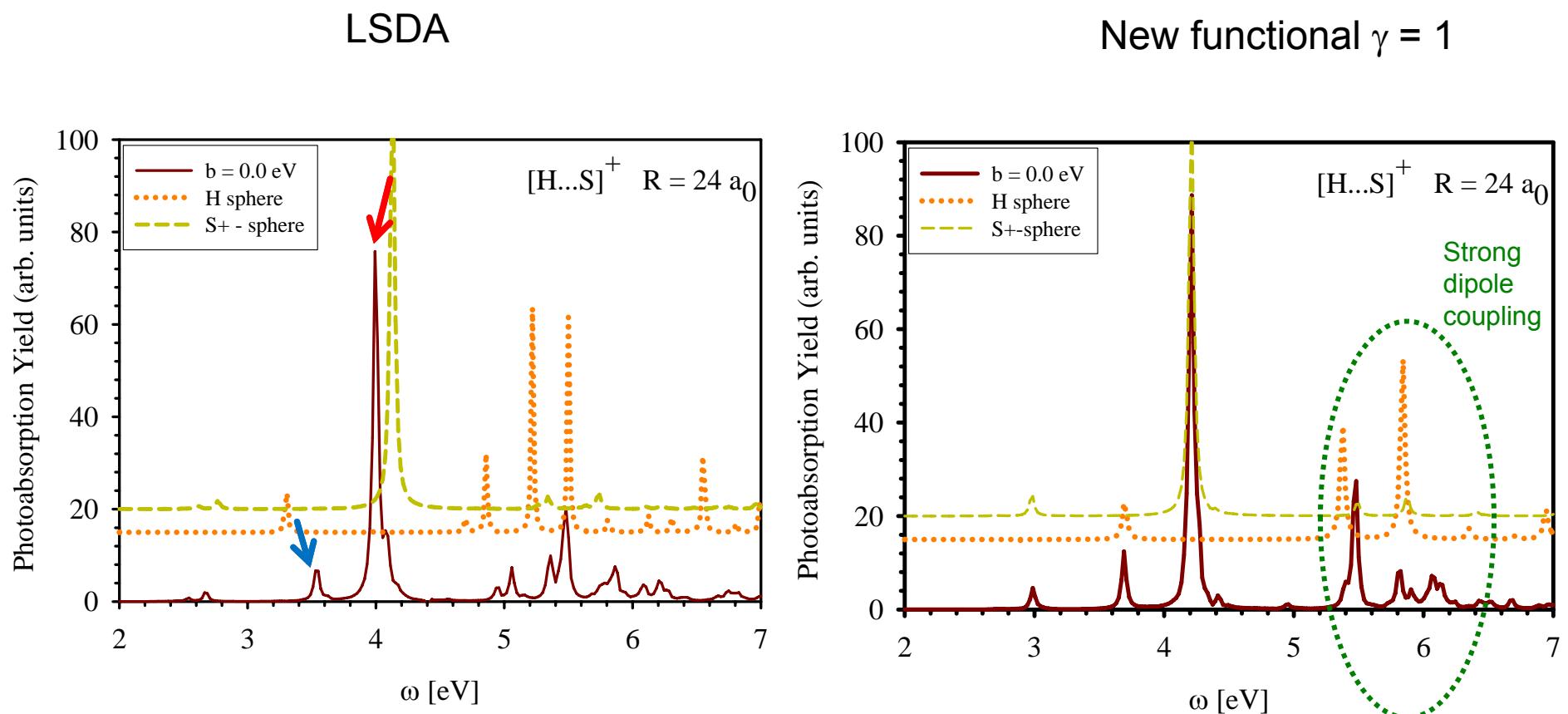
S. Hirata and M. Head-Gordon, Chem. Phys. Lett. 314, 291 (1999).

# Balanced functional

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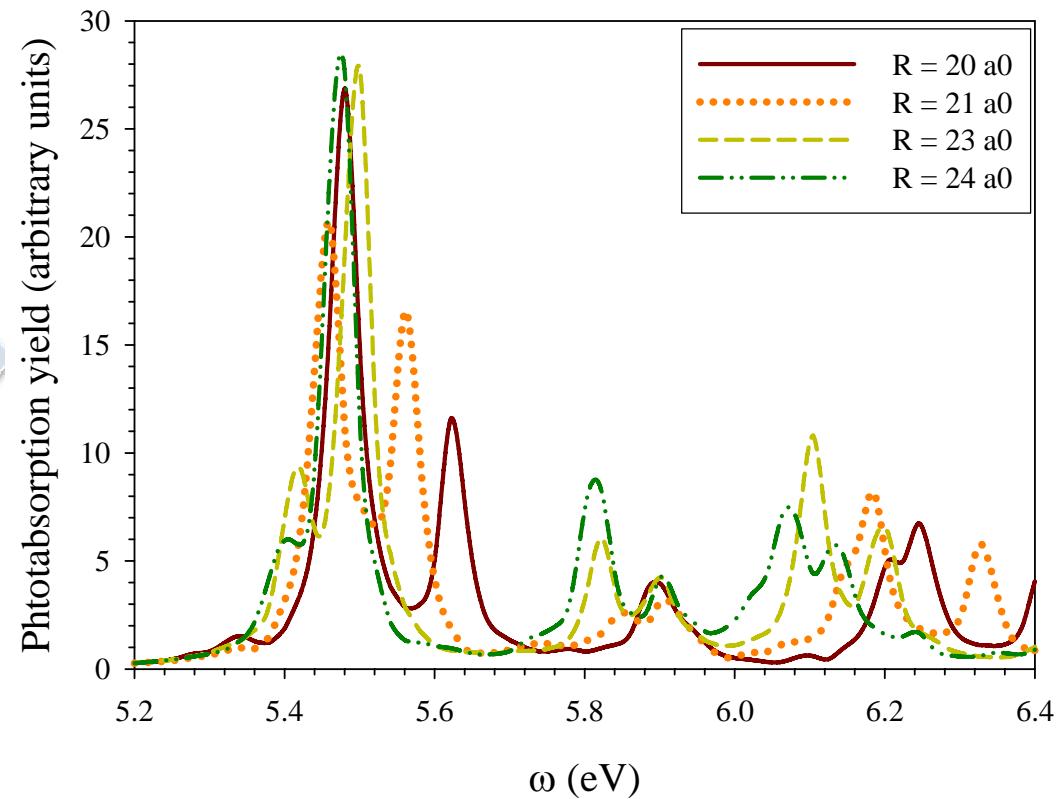
- New functional is balanced
- Can do atomization energies and structures very similar to B3LYP (somewhat less well)
- Better than B3LYP in:
  - Charge quantization
  - Consistency of IP's
  - EA for small systems
  - Static Polarizability
  - Vertical excitations
  - Rydberg excitations

# Back to near-field: Spurious splitting: fixed

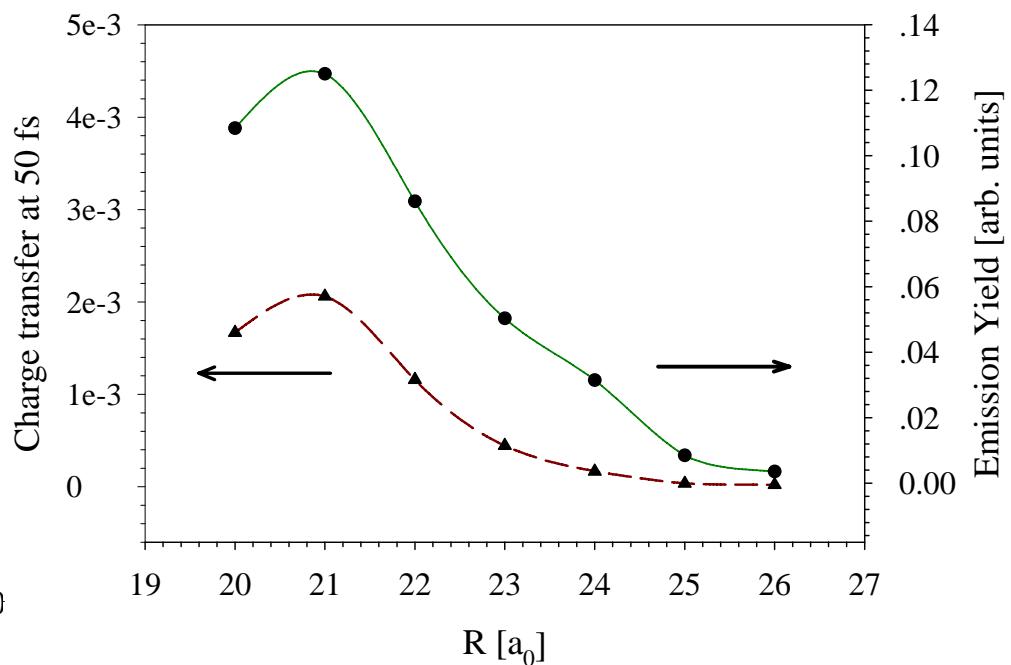
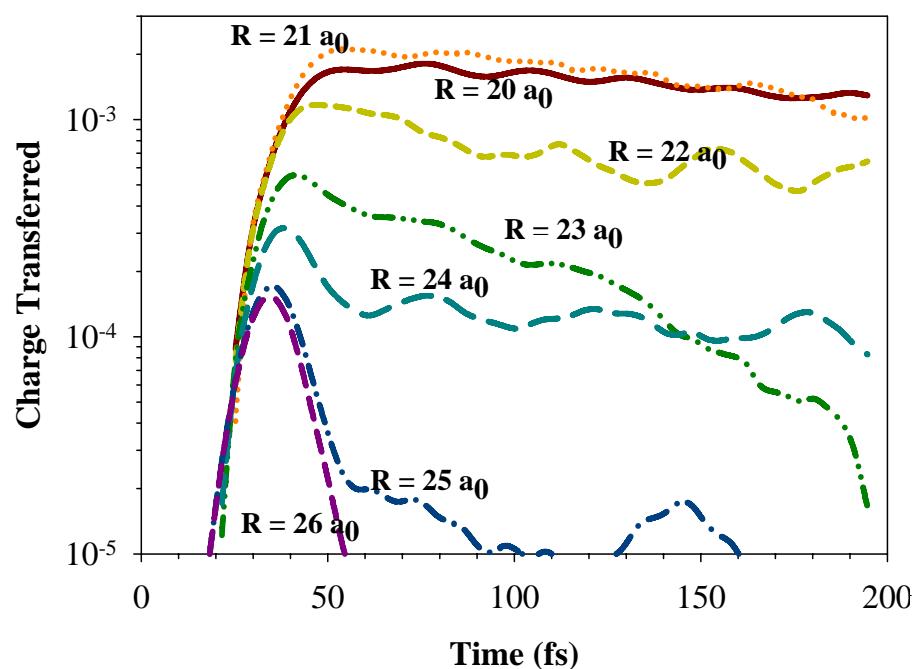




- Illuminate at 5.6 eV
- Observe emission vs.  $R$

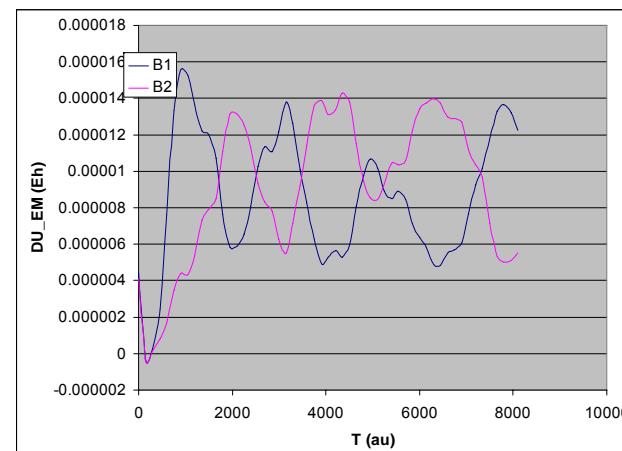
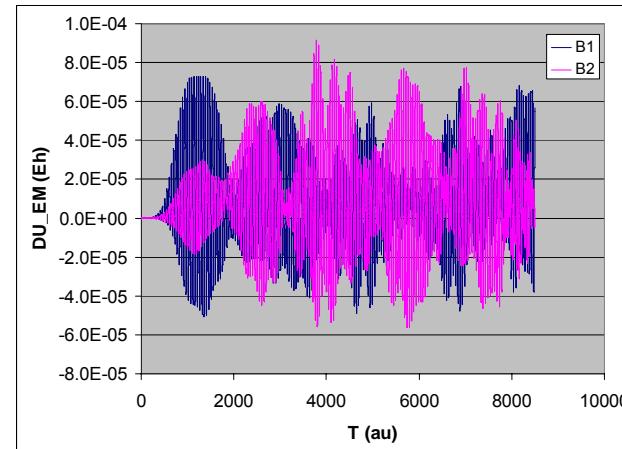


# Charge transfer dynamics



# EM Energy transport

- 2 small silver clusters (diam ~1nm) at small distances (~3 nm)
- We excite left cluster and watch EM energy in left and right clusters
- EM energy oscillates, period equal to coupling. T=50fs
- In this case C=0.1eV
- In experiment large dots and C=0.3eV



M. L. Brongersma, J. W. Hartman, and H. A. Atwater, Phys. Rev. B 62, 16356 (2000).  
R. Baer and D. Neuhauser work in progress (2006).

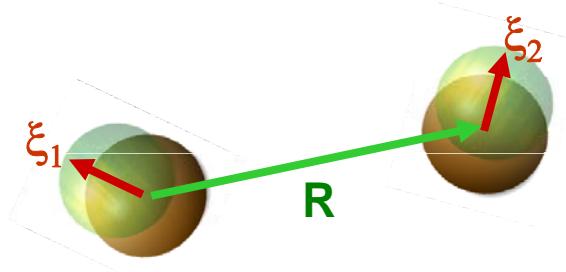
# “Optical” devices on molecular scale

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- Linear arrays of dipole-coupled centers
- We assume long coherence time
  - Presently not a justified assumption
  - There are encouraging results (Ag)
  - Synthetic challenge: find suitable materials
- Meanwhile, we play with this theoretically: what to expect from such coherent systems?

# Polariton model: Hamiltonian

- Weak excitation
- In noble metal nano-particles, local surface plasmon-polariton
- N-site system, dipole interaction



$$E(\vec{\xi}_1, \vec{\xi}_2; \vec{R}) = \frac{(\vec{\xi}_1 \cdot \vec{\xi}_2) R^2 - 3(\vec{\xi}_1 \cdot \vec{R})(\vec{\xi}_2 \cdot \vec{R})}{R^5}$$

$N$  sites  $\rightarrow 3N$  Hilbert space

$$\psi_i = \begin{pmatrix} \psi_{i,x} \\ \psi_{i,y} \\ \psi_{i,z} \end{pmatrix} \quad H_{i\alpha,j\beta} = E(\xi_\alpha, \xi_\beta; R_{ij})$$

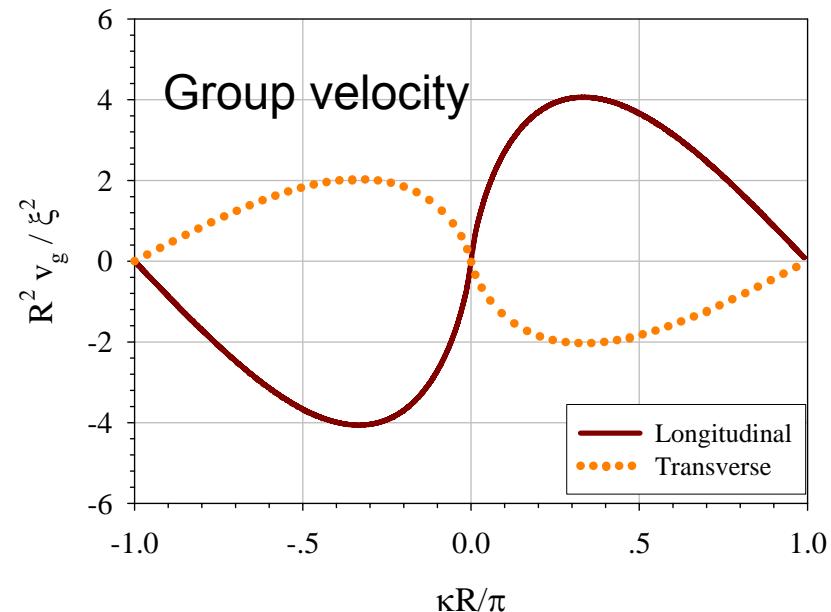
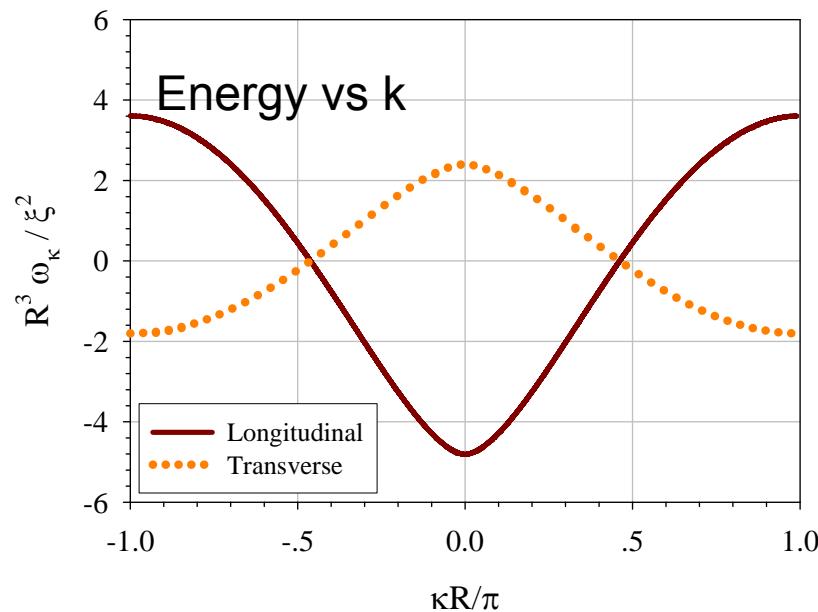
Dynamics - Schrodinger Waves:

$$i\dot{\psi}(t) = H\psi(t)$$

U. Fano, Phys. Rev 103, 1202 (1956).

J. J. Hopfield, Phys. Rev 112, 1555 (1958).

# Dispersion relation and group velocity

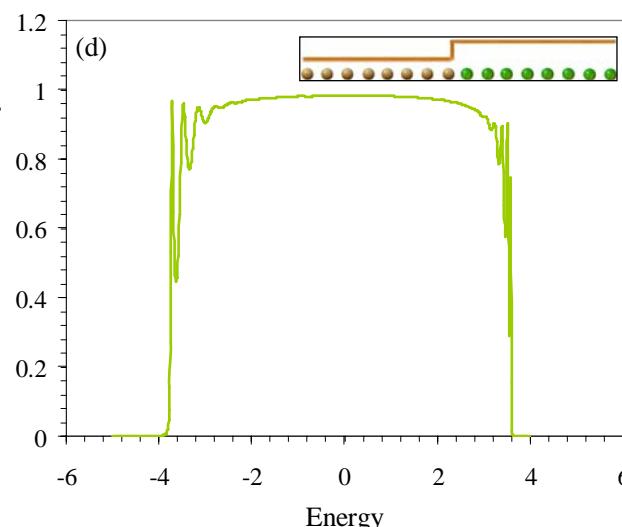
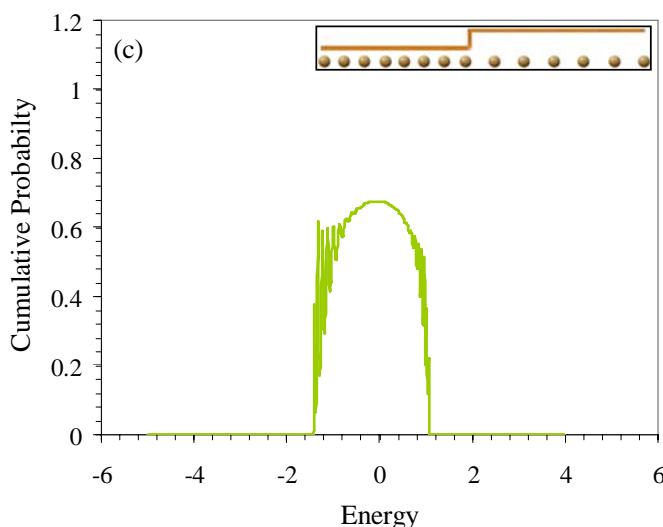
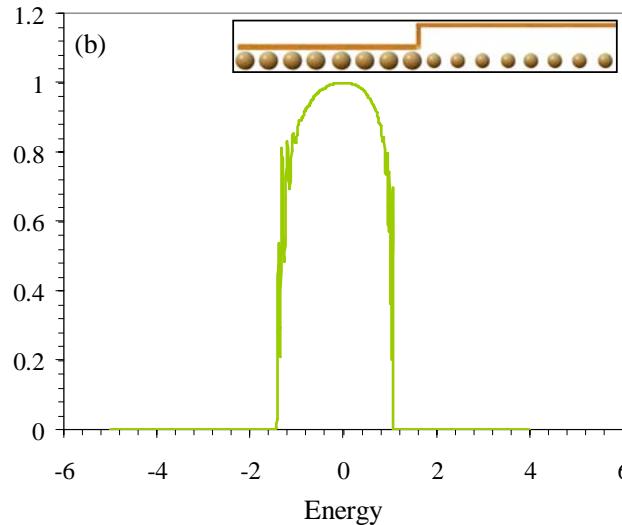
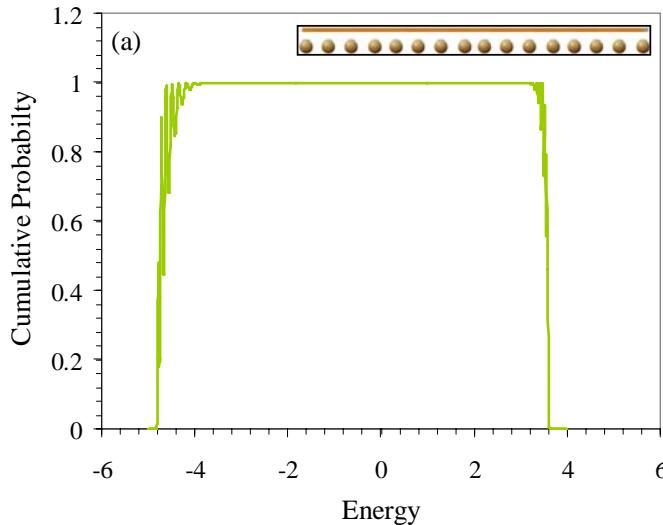


- Energy bands: L waves  $[-4.4 \rightarrow 3.6]$  T waves  $[-1.8 \rightarrow 2.2]$
- Longitudinal waves move in direction of  $k$
- Transverse waves move in opposite direction to  $k$  “negative refractive index...”
- For low  $k$ , the larger  $k$  the large velocity. Subsequently – opposite behavior.
- At  $k=0.46\pi$  the two waves have same energy and group velocity light-like (indep. of  $k$ )

S. Maier, P. G. Kik, H. A. Atwater, S. Meltzer, A. A. G. Requicha, and B. E. Koel, Proc. SPIE 4810 (2002).

R. Baer and D. Neuhauser, J. Chem Phys., In press (2006).

# Step barriers



$\xi-\xi'$

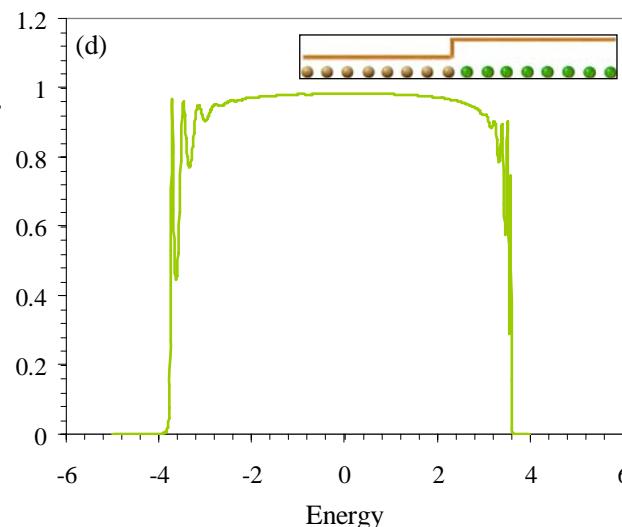
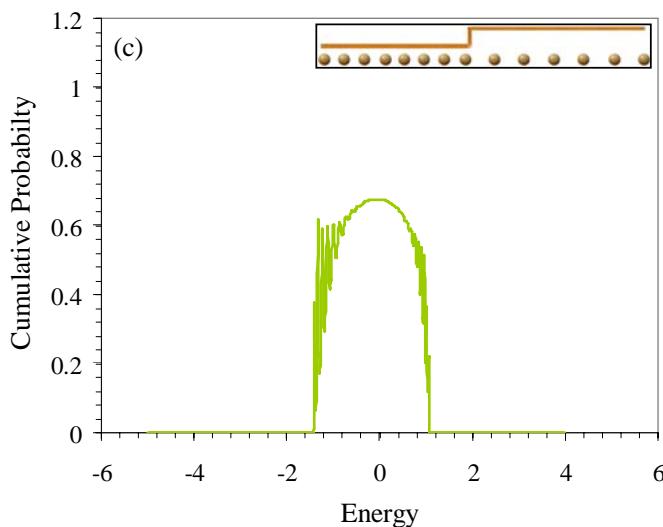
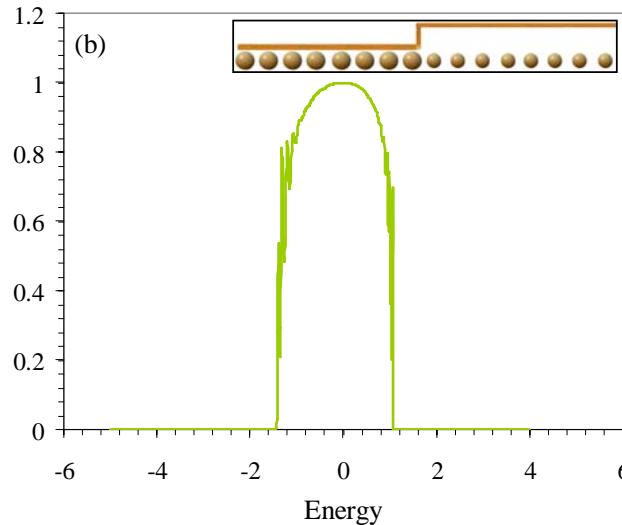
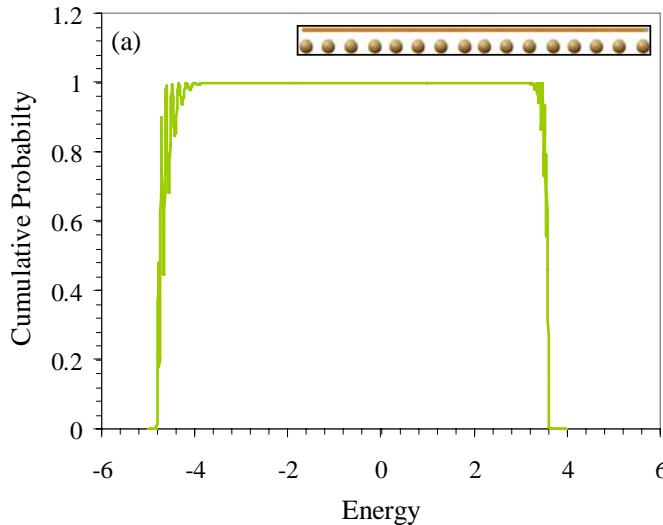
- The bandwidth is smaller
- $k$  doesn't change

$R-R'$

- Bandwidth smaller
- Length scale changes
- $k$  change  $\rightarrow$  reduce transmission

$\omega-\omega'$

# Step barriers



$\xi-\xi'$

- The bandwidth is smaller
- $k$  doesn't change

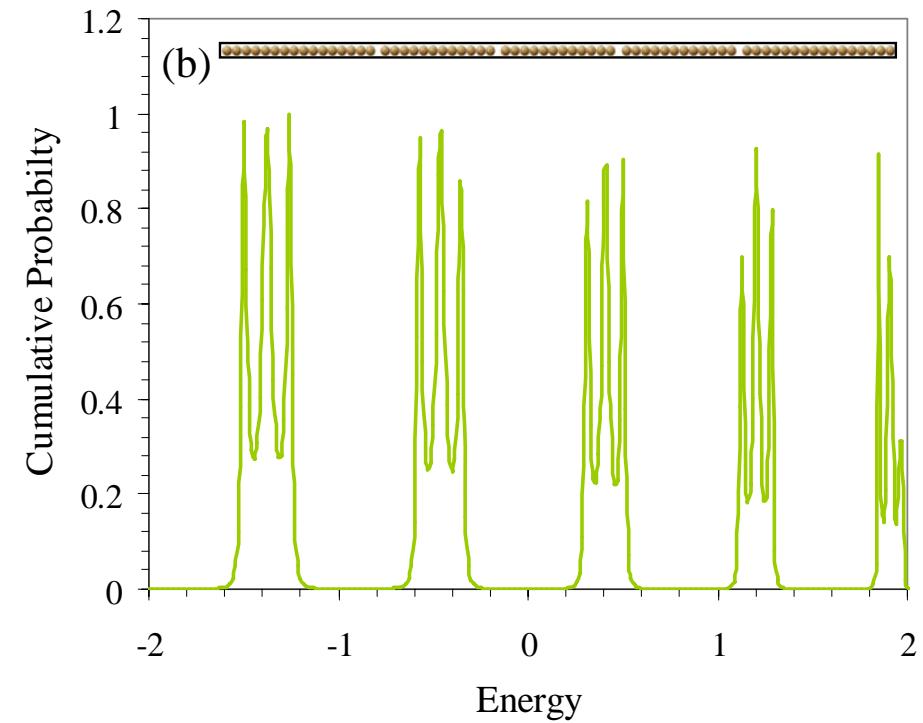
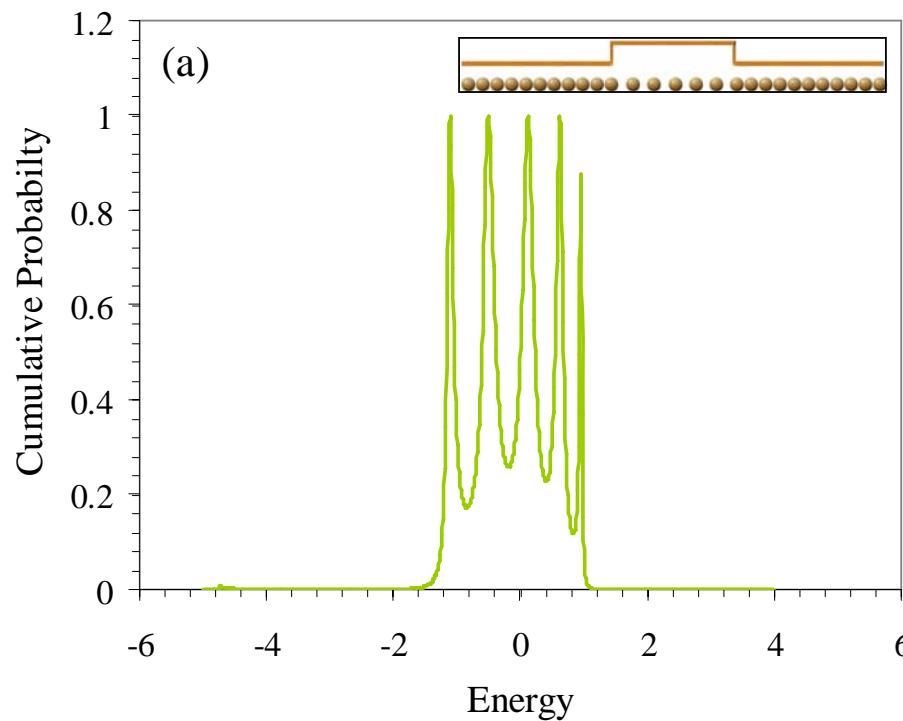
$R-R'$

- Bandwidth smaller
- Length scale changes
- $k$  change  $\rightarrow$  reduce transmission

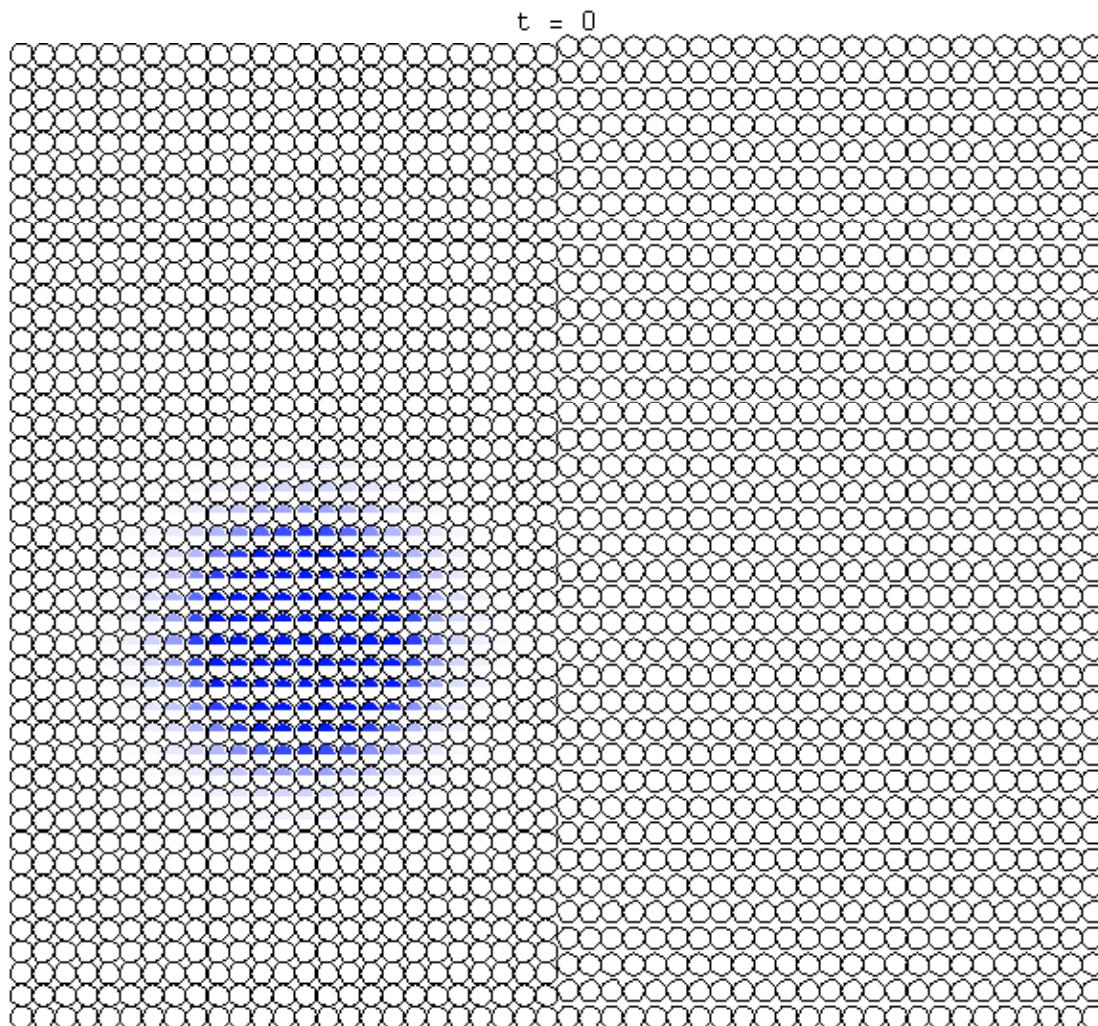
$\omega-\omega'$

# Interference and total reflection

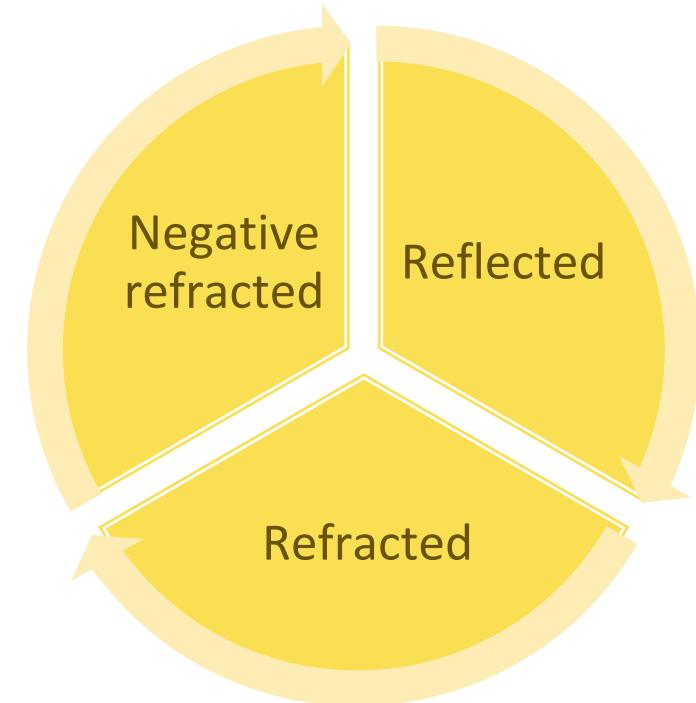
- Using interference one can have total reflection also at  $E=0$



# Nano-optics in 2D lattices



Trifurcation:



# midSummary

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- After fixing the self repulsion problem we:
  - Studied the dipole coupled spectrum of a model “tip-system”
  - We saw strong sensitivity to distance when the distance is small - due in part to charge transfer and in part to dipole coupling
- Fantasized about coherent molecular sized optical devices based on dipole coupling

# Electron dephasing

- Metals and metallic nanodots are lossy...
- Fast dephasing not well described in usual TDDFT
- Must address “memory effects”
- Must obey known exact constraints
  - Translational invariance (TDDFT)
  - Rotational invariance (TDCDFT)
  - Get for free: also net XC force/Torque is zero
- Based on linear response kernel for the homogeneous electron gas (Gross-Kohn param.)

Vignale, Phys. Rev. Lett. 74, 3233 (1995).

E. K. U. Gross and W. Kohn, Phys. Rev. Lett. 55 (26), 2850 (1985).

Y. Kurzweil and R. Baer, Phys. Rev. B 73 (7), 075413 (2006).

# Practical memory

- We follow an idea of Vignale, to obtain TI functional and we add an important ingredient:
- The XC force should be zero (otherwise Ehrenfest's theorem is not obeyed)

$$-\int n(\mathbf{r}, t) \nabla v_{XC}(\mathbf{r}, t) d^3r = 0$$

# Memory KS-equation from an action

- The TDDFT dynamical equations are:

$$i\dot{\psi}_n(\mathbf{R}, t) = \left[ -\frac{1}{2}\nabla^2 + v_{ext}(\mathbf{R}, t) + v_H(\mathbf{R}, t) + v_{adiab}(\mathbf{R}, t) + v_{mem}(\mathbf{R}, t) \right] \psi_n(\mathbf{R}, t)$$

$$v_{mem}[n](\mathbf{R}, t) = V_{mem}[N](\mathbf{R} - \mathbf{D}(t)) + \mathbf{E}_{mem}(t) \cdot (\mathbf{R} - \mathbf{D}(t)) M'[n(\mathbf{R}, t)]$$

$$V_{mem}[N](\mathbf{r}, t) = \int_0^t F'_{mem}(N(\mathbf{r}, t), t - t') \dot{N}(\mathbf{r}, t') dt'$$

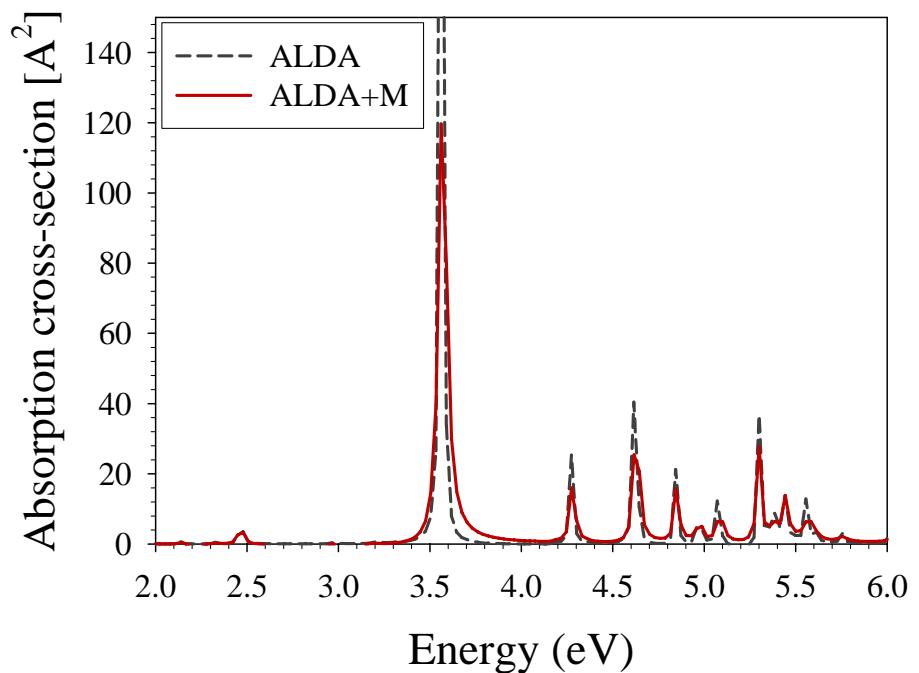
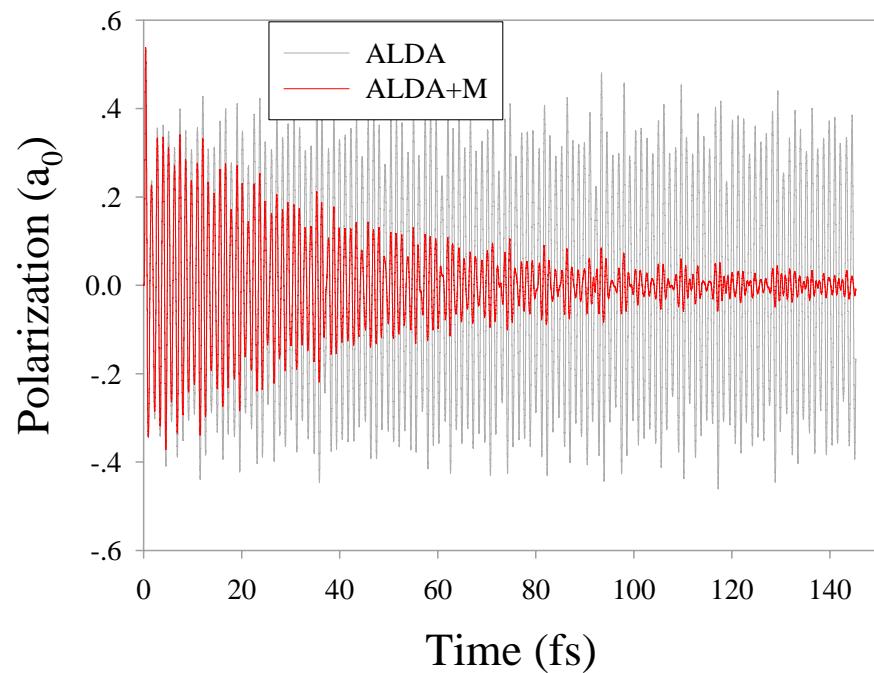
$$N(\mathbf{r}, t) = n(\mathbf{r} + \mathbf{D}(t), t) = n(\mathbf{R}(t), t)$$

$$\mathbf{E}_{mem}(t) = \frac{1}{Q(t)} \int V_{mem}(\mathbf{r}, t) \nabla n(\mathbf{r} + \mathbf{D}(t), t) d^3r$$

$$\mathbf{D}[n](t) = \frac{1}{Q(t)} \int \mathbf{R} M[n(\mathbf{R}, t)] d^3R \quad Q(t) = \int M[n(\mathbf{R}, t)] d^3R$$

Center  
of mass

# Dephasing: dipole oscillations $\text{Au}_{18}$ or $\text{Ag}_{18}$

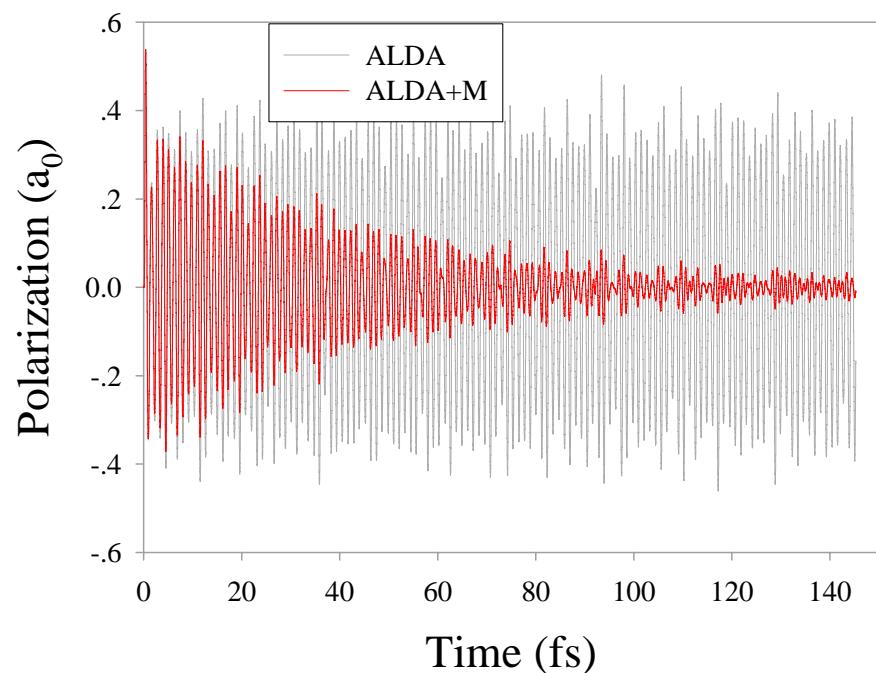


Estimated Decay time:  $T_2 \sim 30$  fs.

Too large. Experiments indicate  $T_2 < 10$  fs

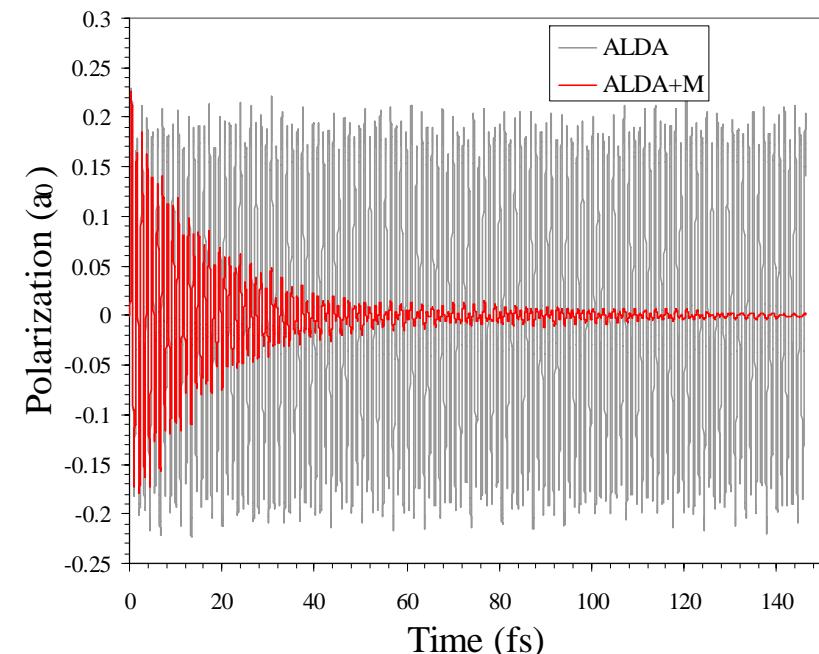
J. Lehmann, M. Merschdorf, W. Pfeiffer, A. Thon, S. Voll, and G. Gerber, Phys. Rev. Lett. 85, 2921 (2000).  
Link and El-Sayed, Ann. Rev. Phys. Chem. 54, 331 (2003)..

# Atomic core effects on dipole decay



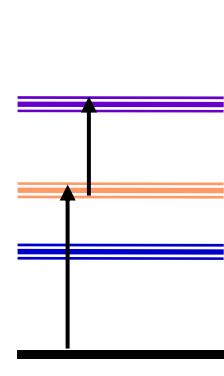
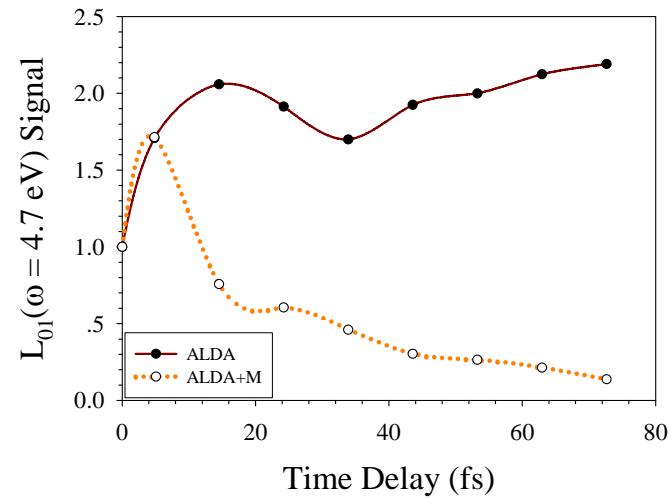
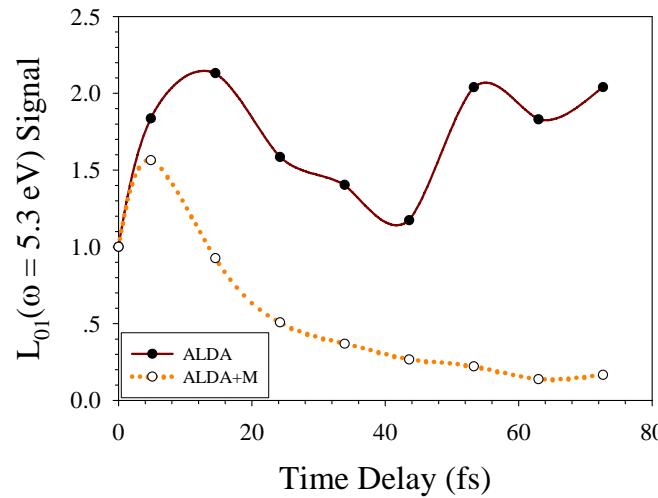
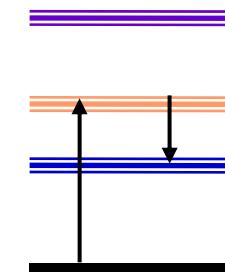
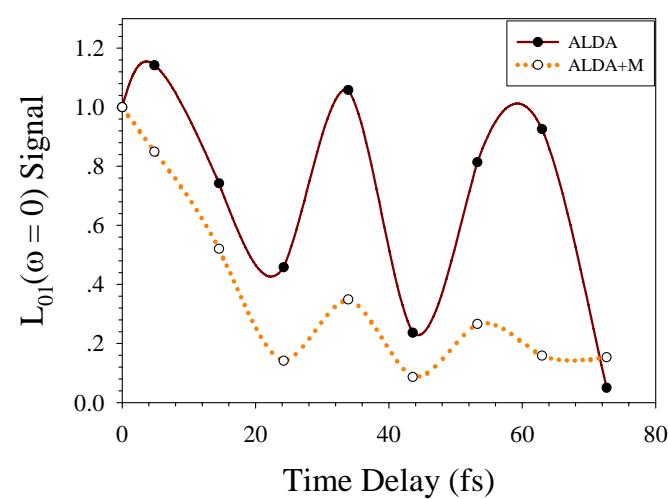
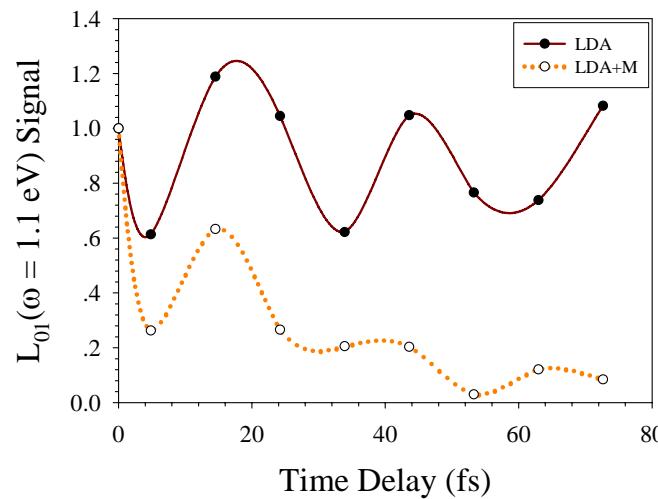
Jellium cluster

$T_2 = 30$  fs



S-electron pp  
Atomistic cluster  
 $T_2 = 15$  fs

# Damping of coherence following plasmon excitation



Y. Kurzweil and R. Baer, Phys. Rev. B 73 (7), 075413 (2006).

# Summary

- The functional allows incorporation of memory
- Meanwhile, we use HEG memory.
- Could be problematic for finite systems
- We have a method to remove “self memory” (otherwise even the H atom has memory...)
- Found that memory effects can be seen in nonlinear regime, such as pump-probe.
- Found that the atomic potential has a strong effect on the plasmon decay time.