

# Magnetic-field Kondo-spectroscopy of single molecule magnets

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**Zero-field:** Phys. Rev. Lett. 96, 196601 (2006)  
**Magnetic field:** cond-mat/0605514.

- Single molecule magnets (SMM)

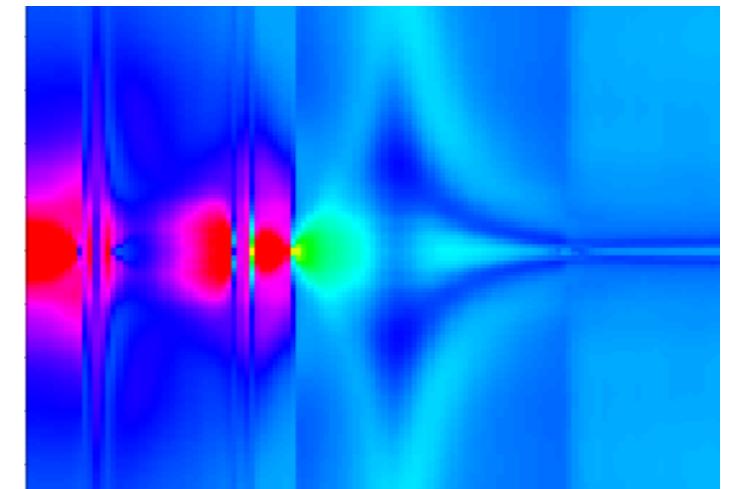
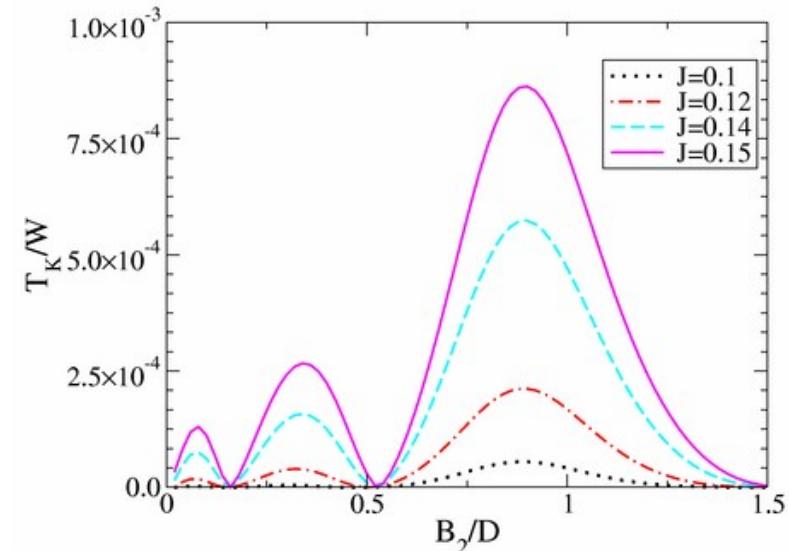
- Magnetic anisotropy:  
barrier + spin-tunneling (QTM)

- QTM-induced Kondo effect

- “Weak” Kondo effect
- “Strong” Kondo effect

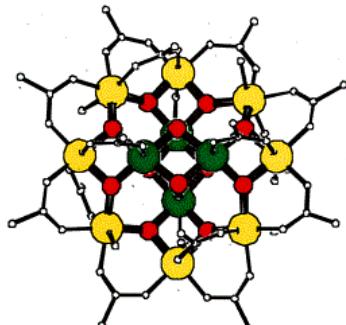
- Magnetic field controlled Kondo effect

Kondo effect  
~ mixing of magnetic states  $M$   
*induced by QTM*  
*controlled by magnetic field*



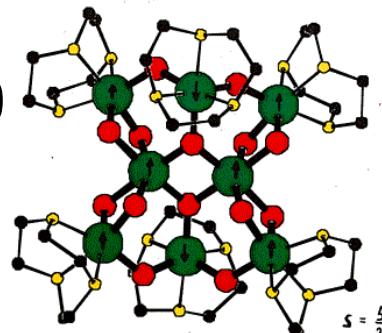
# Single molecule magnets (SMM)

Mn12,  
S=10

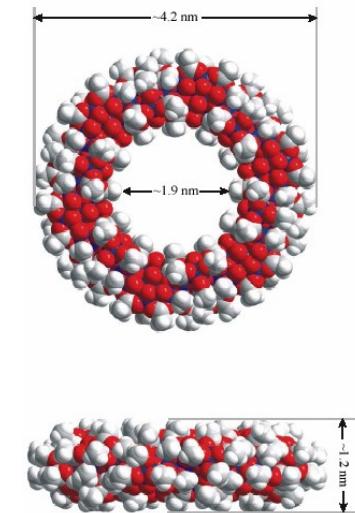


$$8(S=2) - 4(S=3/2) = 10$$

Fe8,  
S=10



Mn84,  
S=6



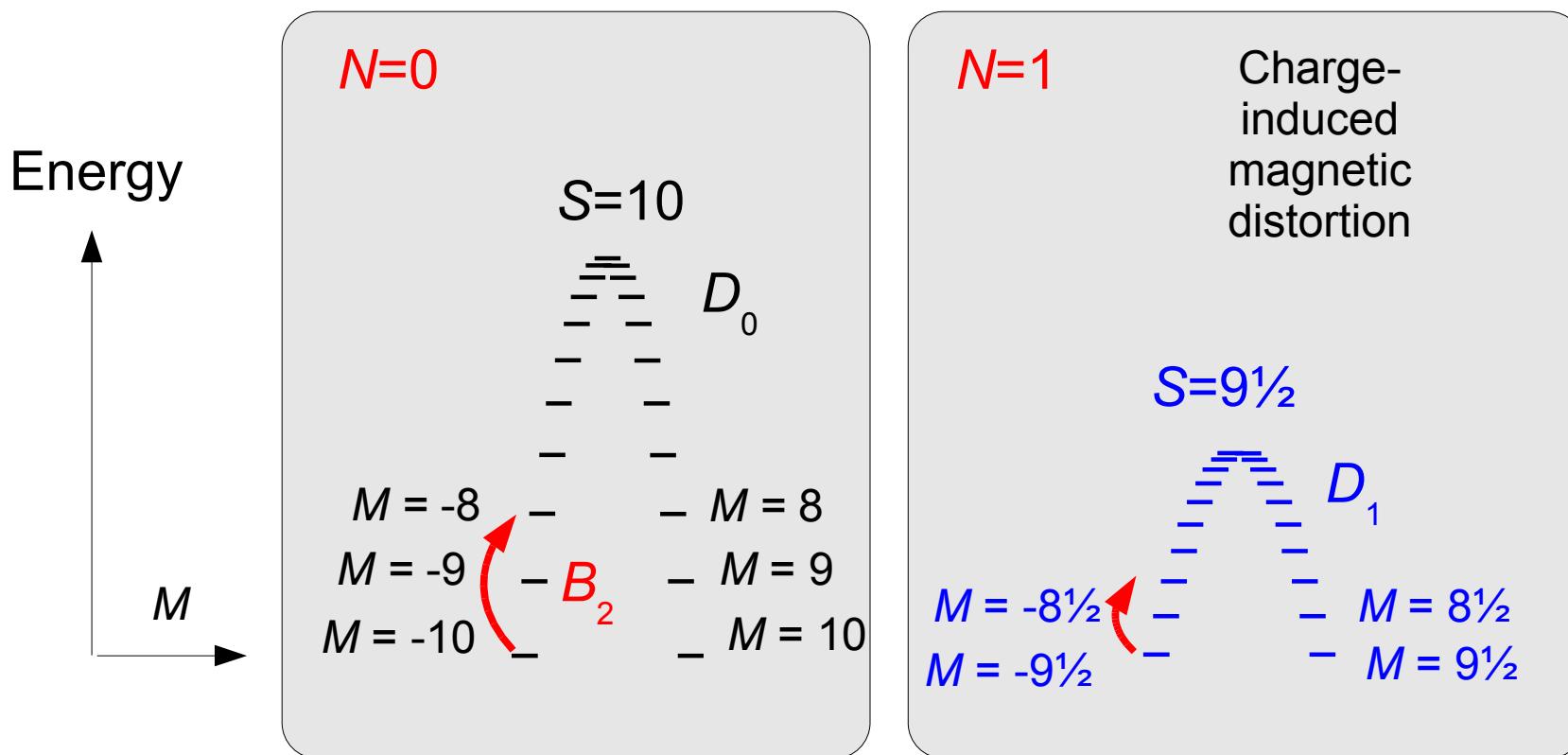
Sessoli et. al. J. Am. Chem. Soc 115, 1804 (1993)

Thomas et. al. Nature 383, 145 (1996)

Friedman et al. Phys. Rev. Lett. 76, 3830 (1996)

- Big, finite spin  $S >> 1/2 \sim$  intramolecular exchange
- Magnetic anisotropy  $\sim$  intramolecular spin-orbit coupling
- Discrete magnetic symmetry  $\sim$  geometry of magn. core

# Magnetic anisotropy



$$H_{MAB} = - D_N S_z^2 \quad \text{Magnetic anisotropy barrier}$$

$$H_{QTM} = - \frac{1}{2} B_2 (S_+^2 + S_-^2) \quad \text{Quantum tunneling of magnetization (QTM)}$$

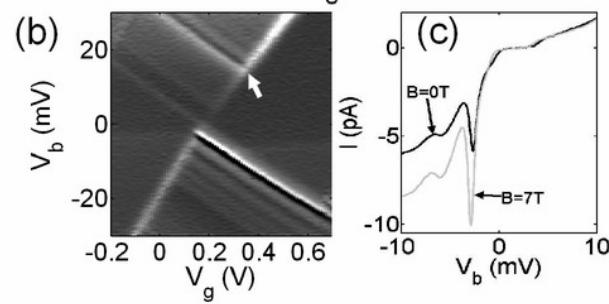
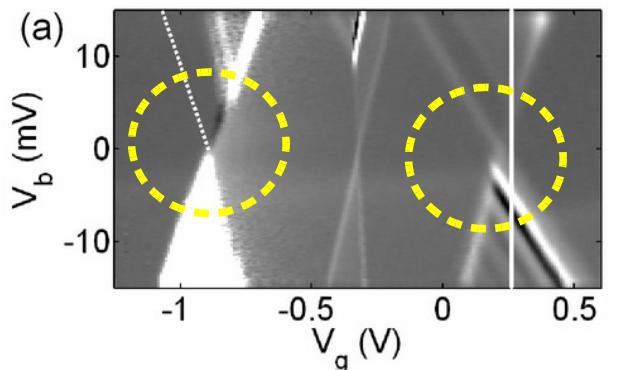
Symmetry: 2-fold rotation axis

$$B_2 / D_N < 1$$

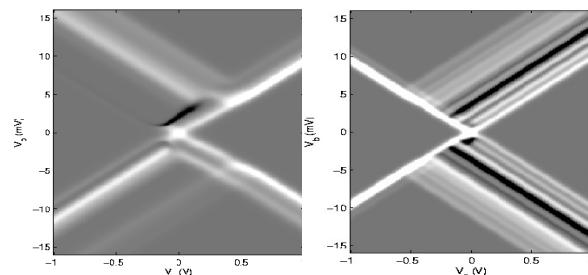
$$D \sim 5 \cdot 10^{-2} \text{ meV}$$

H. van der Zant Delft  
A. Cornia Modena

Phys. Rev. Lett. 96, 206801 (2006)



C. Romeike, M. R. Wegewijs, H. Schoeller  
Aachen

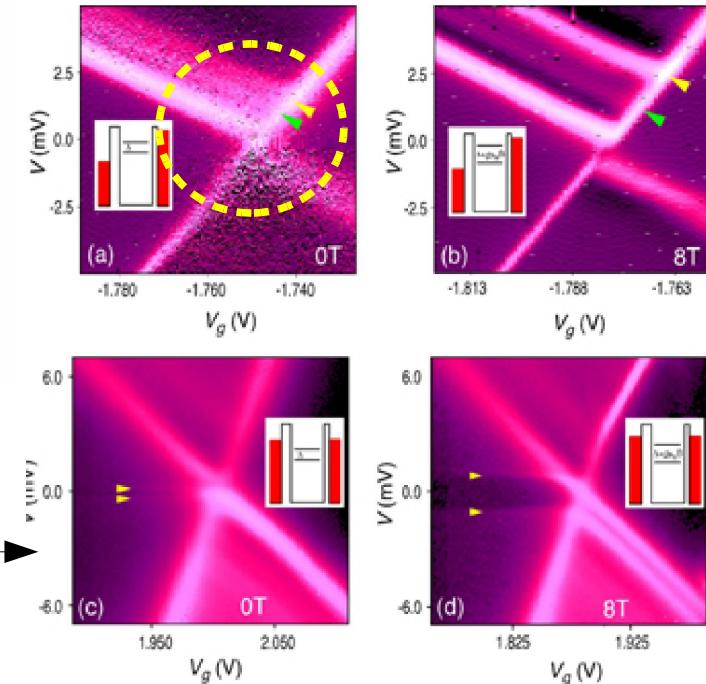


Magnetic-blockade  
& full suppression  
Seveal spin multiplets  
per charge state

# Experiment

M.-H. Jo, H. Park, J. Long  
Harvard

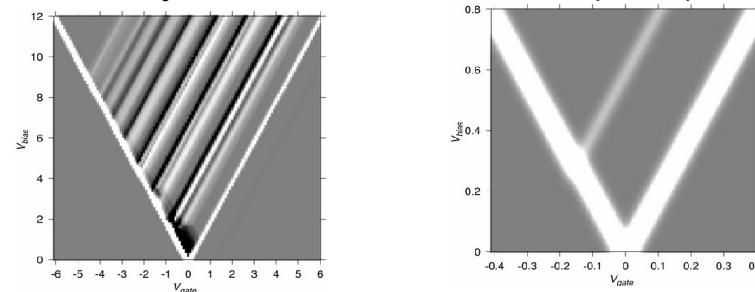
cond-mat/0603276



Mn12 with  
different ligands

Theory

Phys. Rev. Lett. 96, 196805 (2006).



Yes: QTM visible!

No: ~ 1 out of 100  
transitions visible....

Charge-dependent  
magnetic parameters?

Kim & Kim PRL04  
Elastic cotunneling  
& QTM

F. Elste, C. Timm  
Berlin

Magnetic read/write  
cond-mat/0601294

Spin-amplification  
cond-mat/0511291  
cond-mat/0410641

# $S = \frac{1}{2}$ Kondo effect

**$S = \text{molecular spin}$**

$$S = \sum_{kk'\sigma\sigma'} a_{k\sigma}^\dagger \sigma_{\sigma,\sigma'} a_{k\sigma}/2 \quad = \text{reservoir spin}$$

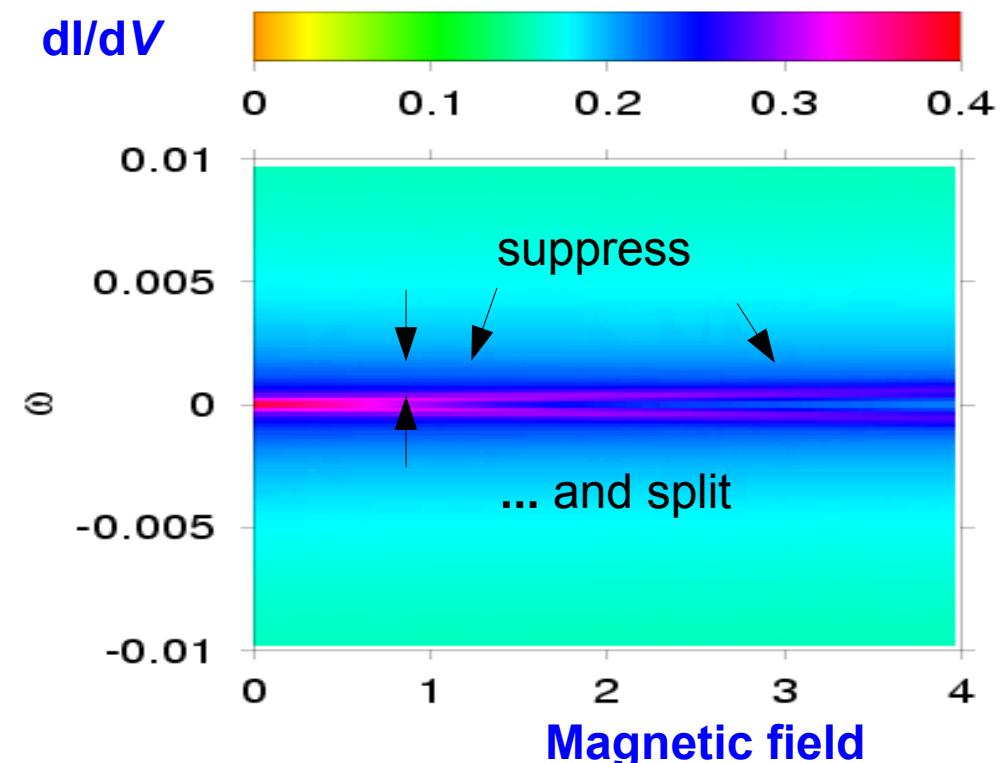
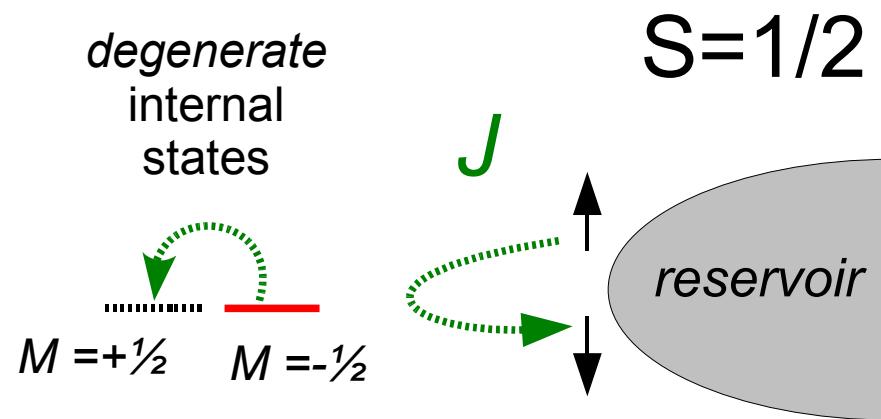
$$\rho J \sim \frac{\Gamma}{E_{add}(V_g)} \quad \begin{matrix} \text{STM} \\ \text{3-terminal} \end{matrix}$$

$$W = 1/\rho \quad \begin{matrix} \text{bandwidth} \\ \text{reservoir} \end{matrix}$$

$$H_K = J \mathbf{S} \cdot \mathbf{s} + \sum_{k\sigma} \epsilon_k a_{k\sigma}^\dagger a_{k\sigma}$$

AF exchange scattering

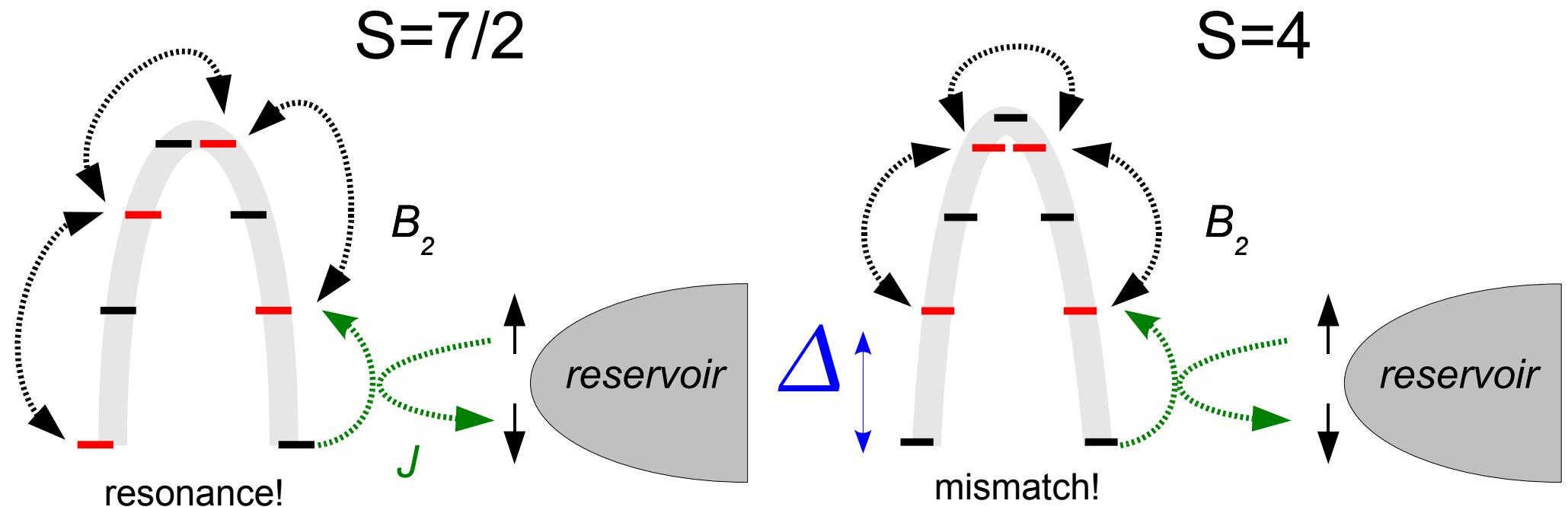
**Kondo  $dI/dV$ -peak  
Width  $\sim T_K \gg T$**



# $S > \frac{1}{2}$ Kondo effect with anisotropy

$$H_{MAB} = -D S_z^2 \quad H_{QTM} = -\frac{1}{2} B_2 (S_+^2 + S_-^2) \quad H_K = J \mathbf{S} \cdot \mathbf{s} + \sum_{k\sigma} \epsilon_k a_{k\sigma}^\dagger a_{k\sigma}$$

**suppresses**  
underscreened Kondo      **assists** spin reversal  
pseudo-spin Kondo      **completes**  
spin reversal



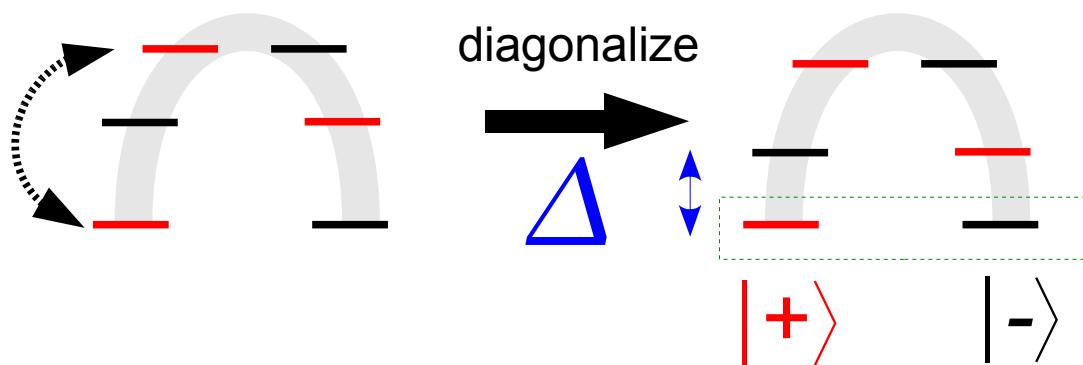
“Weak” vs “Strong” Kondo coupling  
 $T_K \gtrsim \Delta \sim 2SD \sim 1 \text{ meV}$  (magnetic scale)

$B_2 \ll D$

# Weak Kondo effect in SMMs

Phys. Rev. Lett. 96, 196601 (2006).

$$T_K(J, \Delta) \ll \Delta$$



Cut-off:  
 $W_{\text{eff}} \sim \Delta(B_2, D)$

$$\frac{d J^\alpha}{d \ln W} = - \rho J^\beta J^\gamma$$

$$\alpha, \beta, \gamma \in \{x, y, z\}$$

$$H_K = \sum_{i=xyz} J^i \mathbf{P}^i \cdot \mathbf{s}^i + \sum_{k\sigma} \epsilon_k a_{k\sigma}^\dagger a_{k\sigma}$$

truncate: pseudo-spin-½  $\mathbf{P}$

$$J^z = 2J \langle + | S_z | + \rangle$$

$$J^{x,y} = J \langle + | S_+ \pm S_- | - \rangle$$

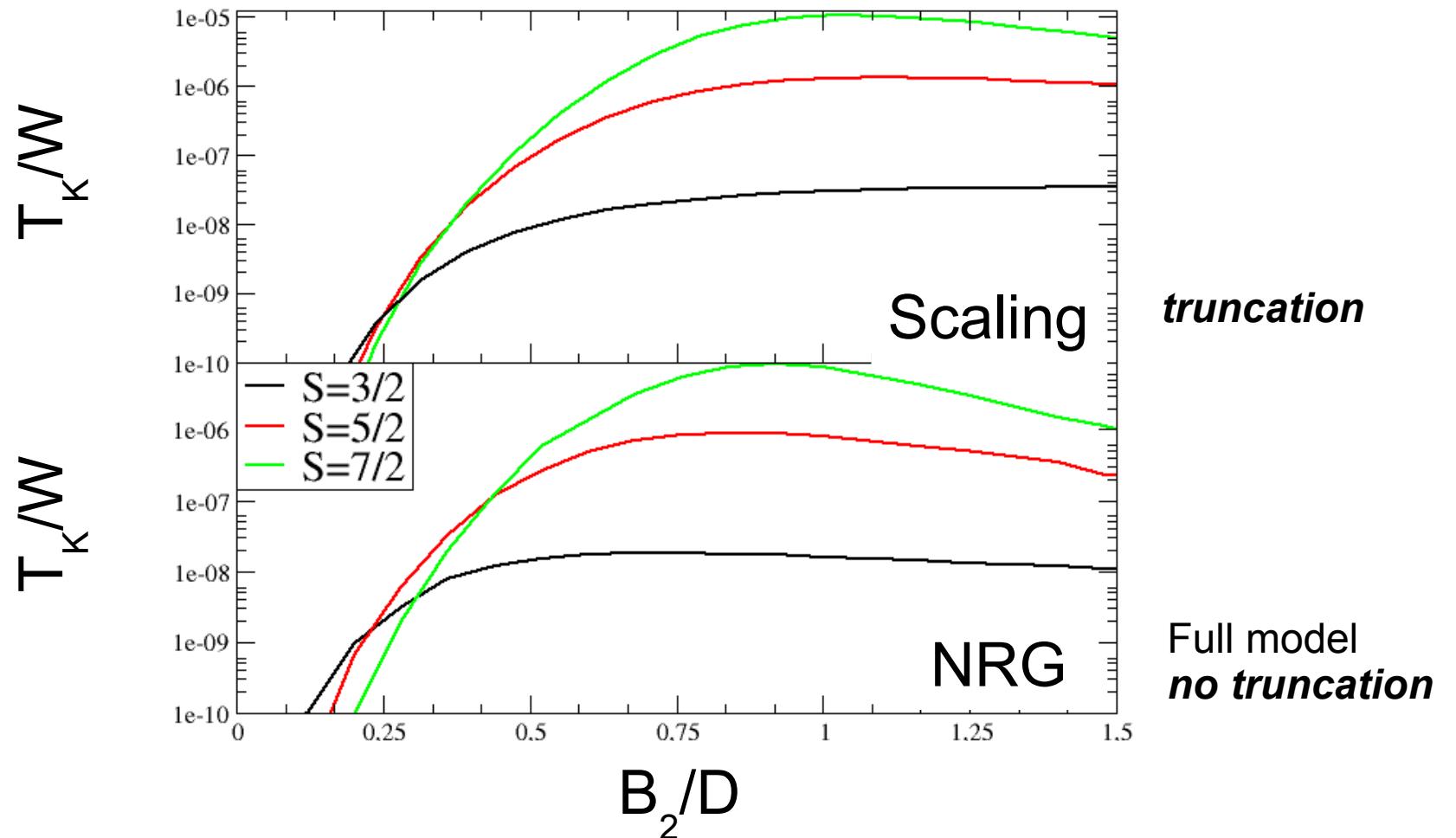
Poor-man scaling:  
 fully anisotropic exchange

QTM modulates magnetic state *mixing*

Modifies exchange: *strength & anisotropy*

$$J^{x,y,z}(B_2/D)$$

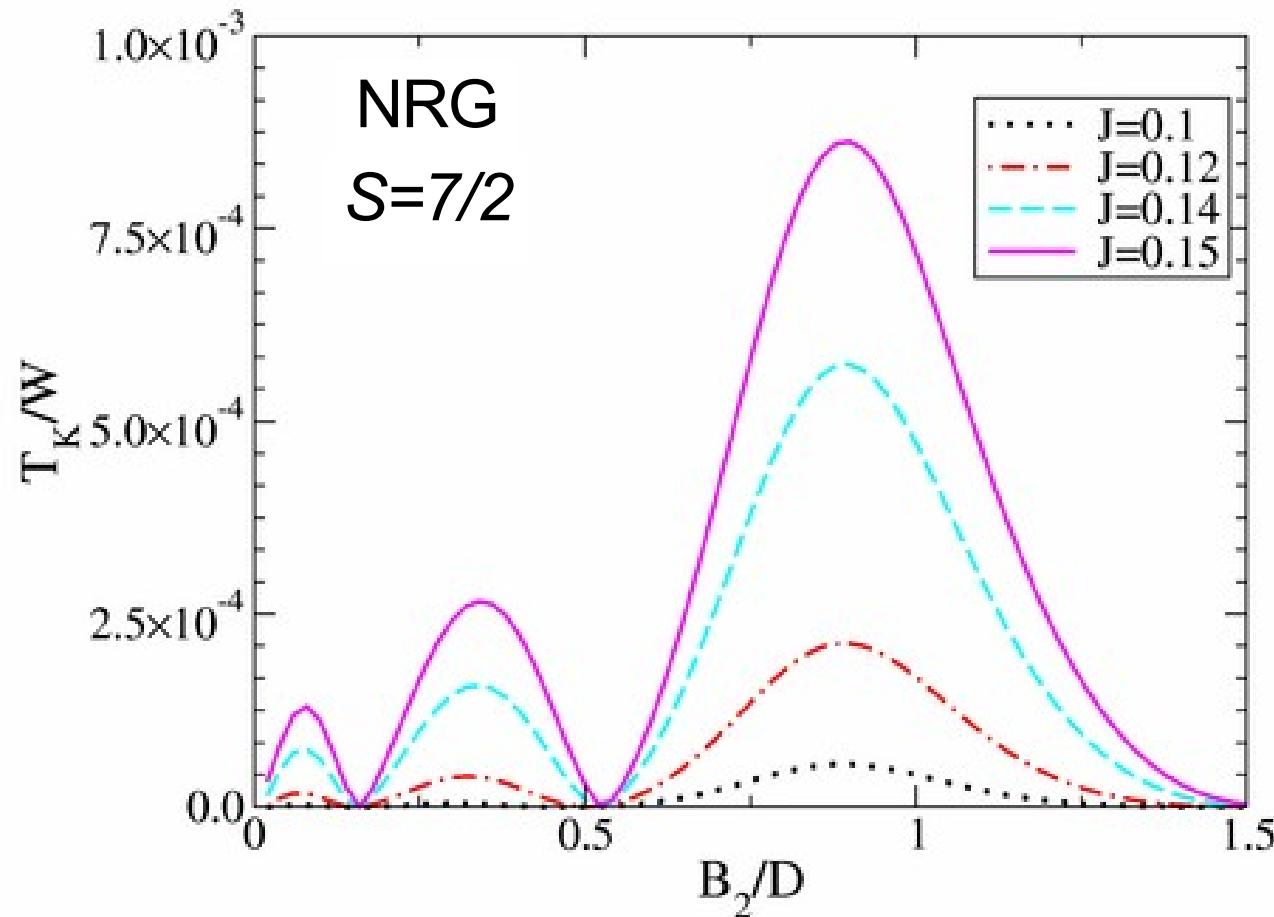
# $T_K$ tuned by QTM



Parameters:  $W=1$ ,  $D=0.005W$ ,  $J=0.1W$

# Strong Kondo effect in SMMs

C. Romeike, M. Wegewijs, H. Schoeller, W. Hofstetter, cond-mat/0605514.

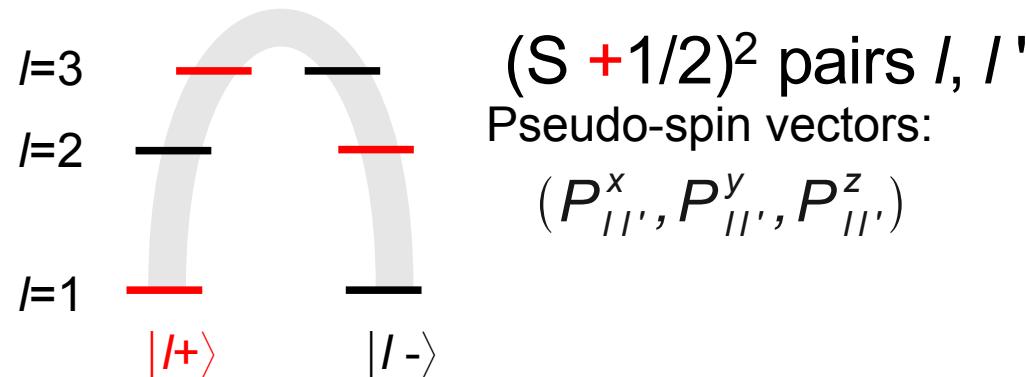


S -1/2 peaks & dips  
*intramolecular origin*

$$T_K(J, \Delta) \gg \Delta$$

# Excited state spin scattering

S +1/2 Kramers doublets



$$H_K = \sum_{II'} \sum_{i=xyz} J_{II'}^i P_{II'}^i s^i + \sum_I E_I N_{II} + \sum_{k\sigma} \epsilon_k a_{k\sigma}^\dagger a_{k\sigma}$$

$$J_{II'}^{x,y} = J \langle +I | S_+ \pm S_- | -I' \rangle \quad J_{II'}^z = 2J \langle +I | S_z | +I' \rangle$$

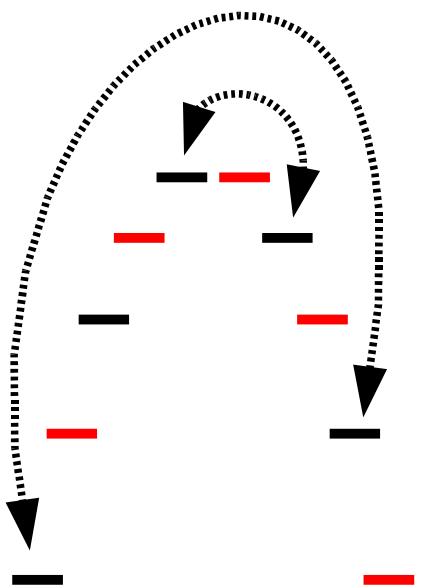
anticrossing  
many exchange couplings change

# QTM induced anticrossings

Large  $M$  / low energy:

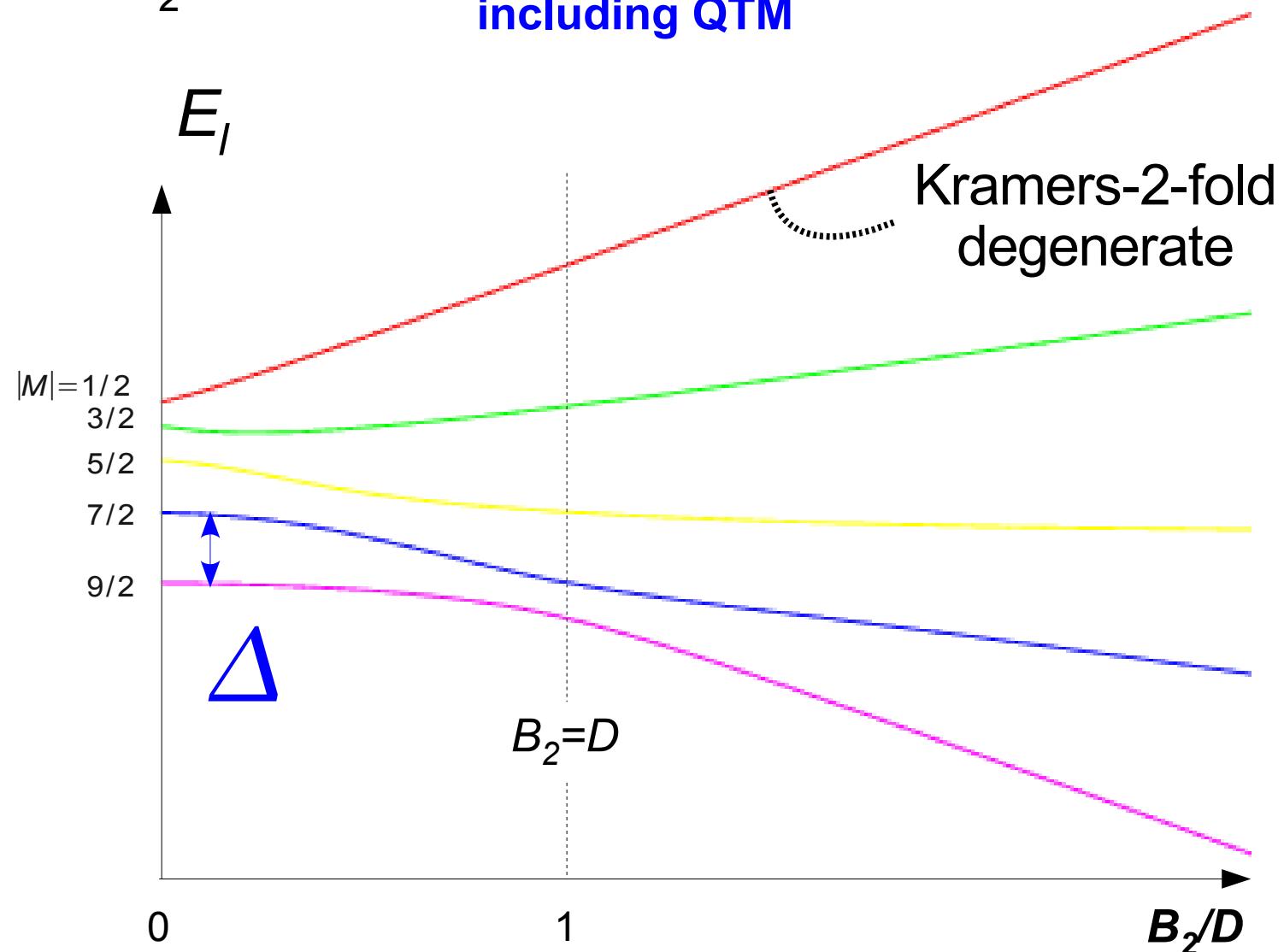
- Large initial splitting
- Coupled in high order of  $B_2$

$S=9/2$



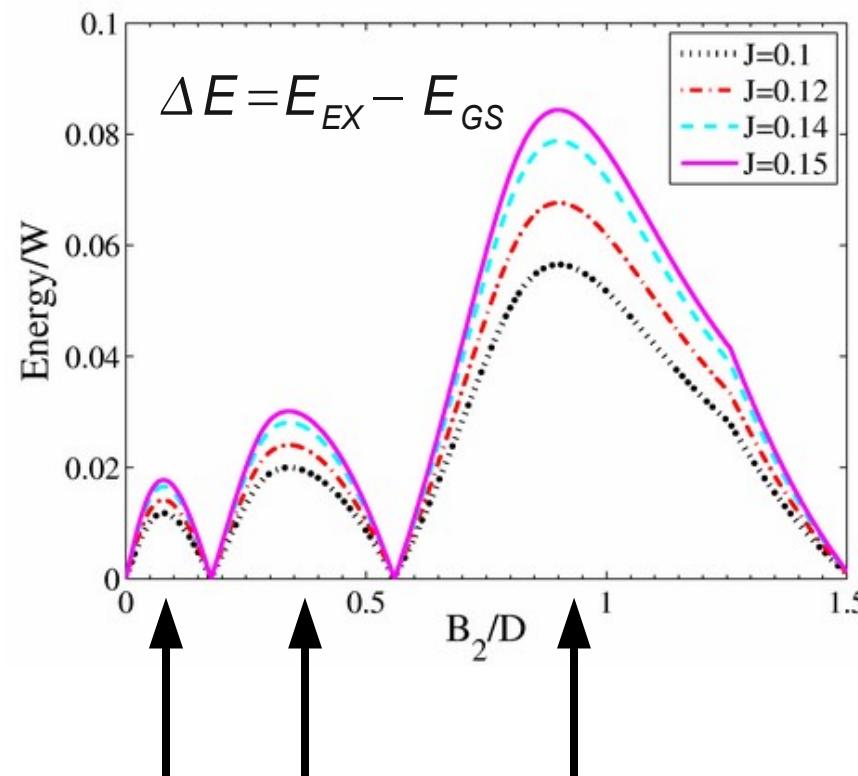
Progressive mixing  
of wavefunctions  
with low  $M$

Molecular eigenenergies  
including QTM

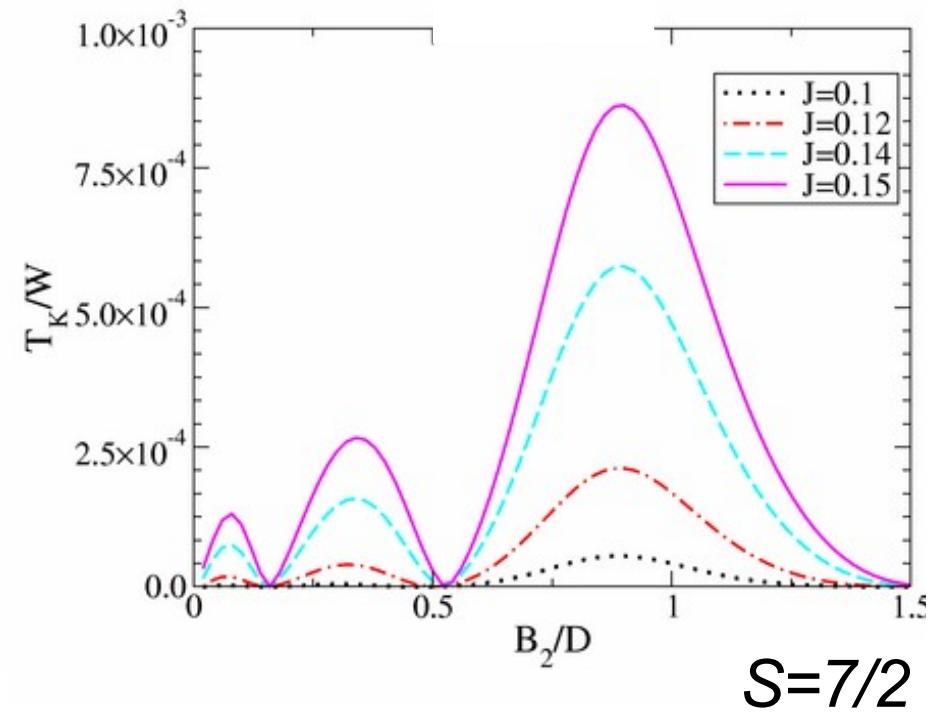


# Single spin-binding energy

Zero-bandwidth model



NRG



Different magnetic excitations of SMM involved

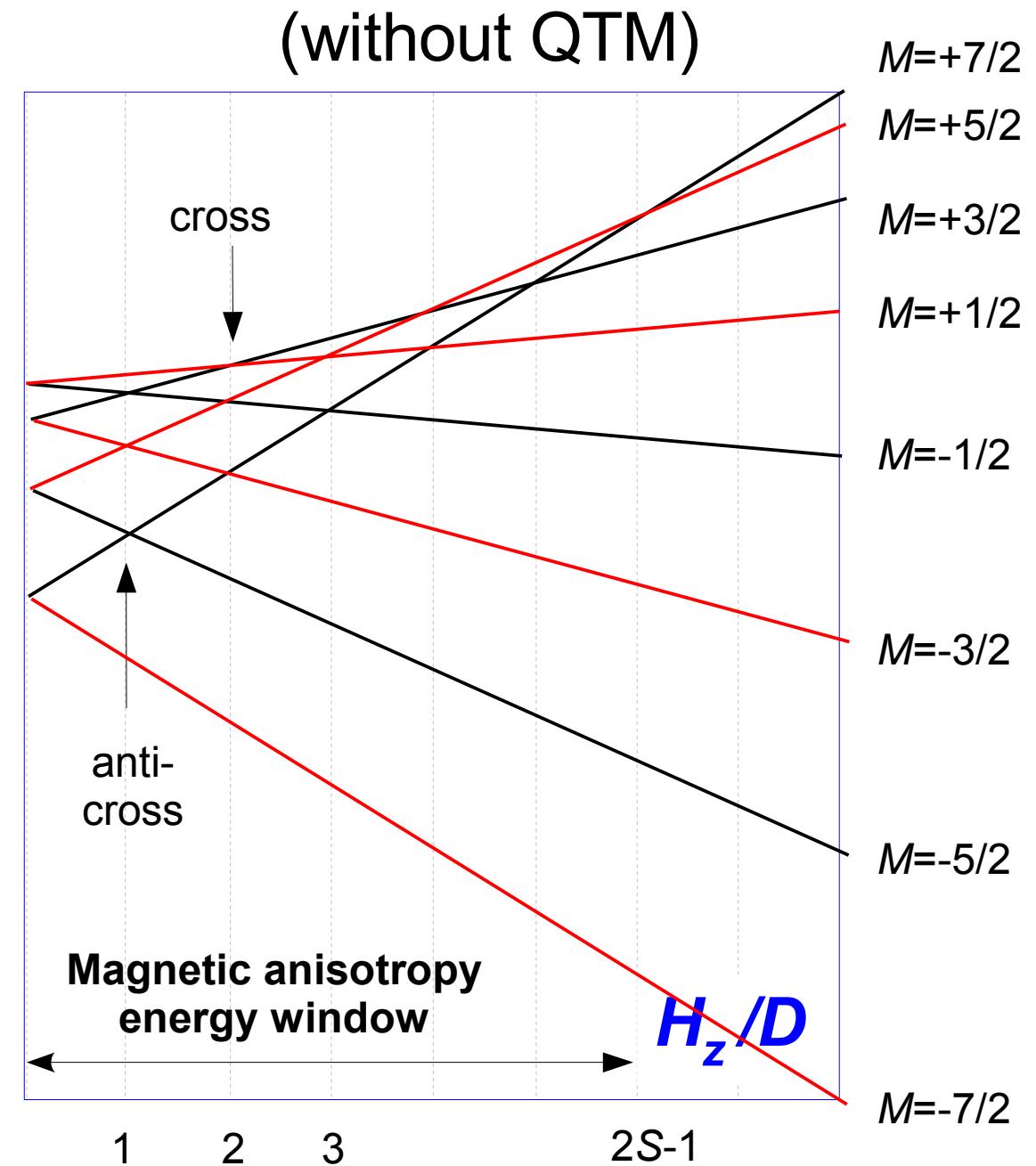
$$T_K(J, \Delta) \gg \Delta$$

# Magnetic field induced anticrossings

$$H_{\text{Zeeman}} = H_z S_z$$

Red / black =  
magnetic symmetry

$2SD \sim 1 \text{ meV}$



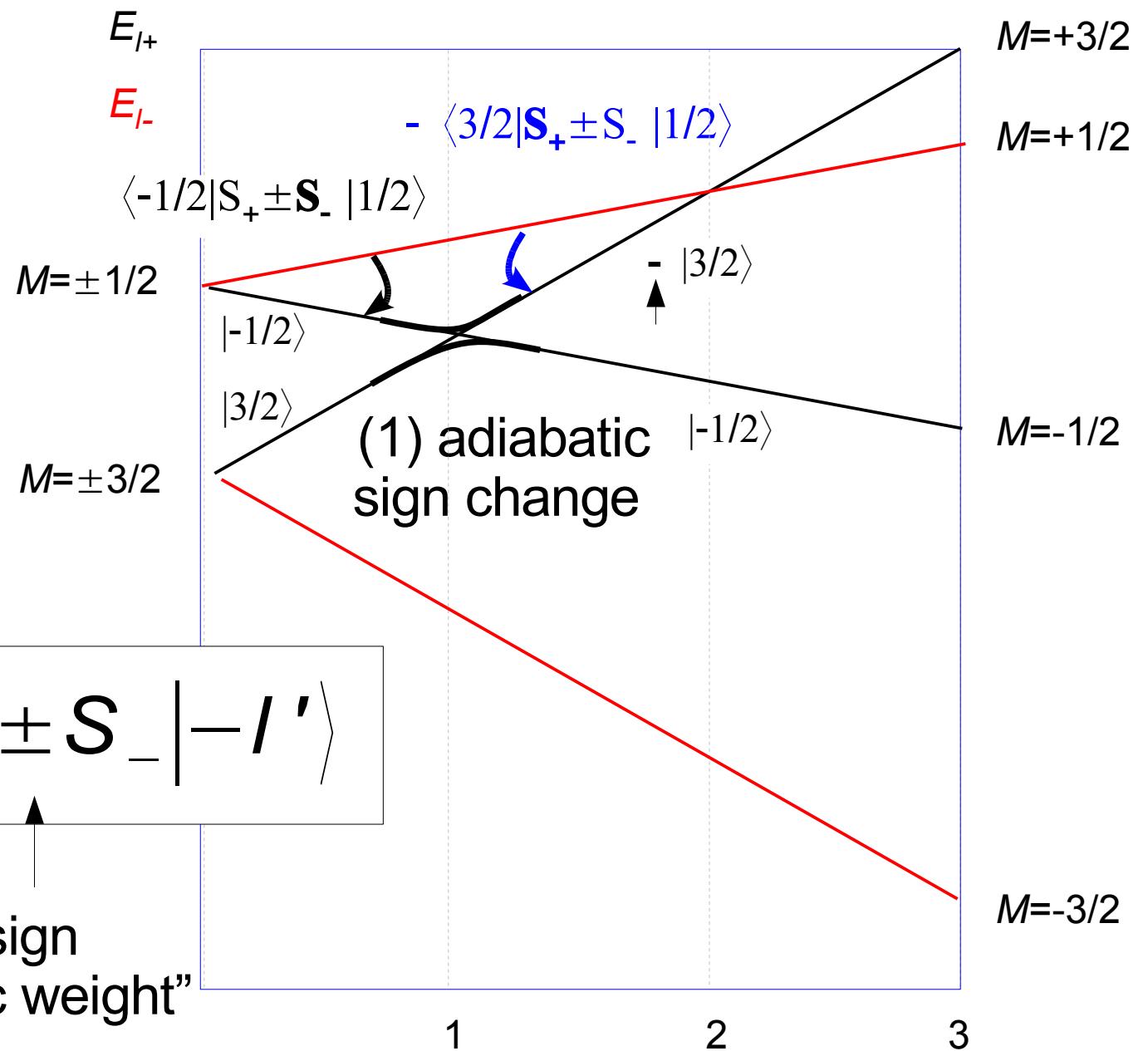
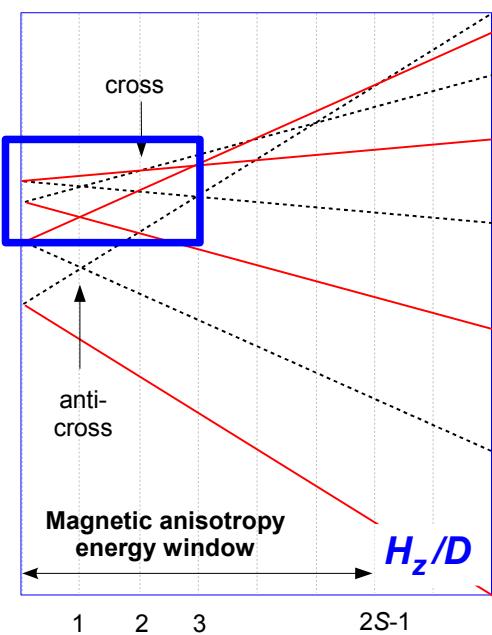
# Magnetic field induced anticrossings

$$H_{\text{ex}} = \sum_{II'} \left( \sum_{i=x,y} J_{II'}^i P_{II'}^i s_i + \sum_{\sigma=\pm} J_{II'\sigma}^z |I\sigma\rangle\langle I'\sigma| s_z \right)$$



Transverse scattering with anticrossing states  
*quenched* at anticrossing

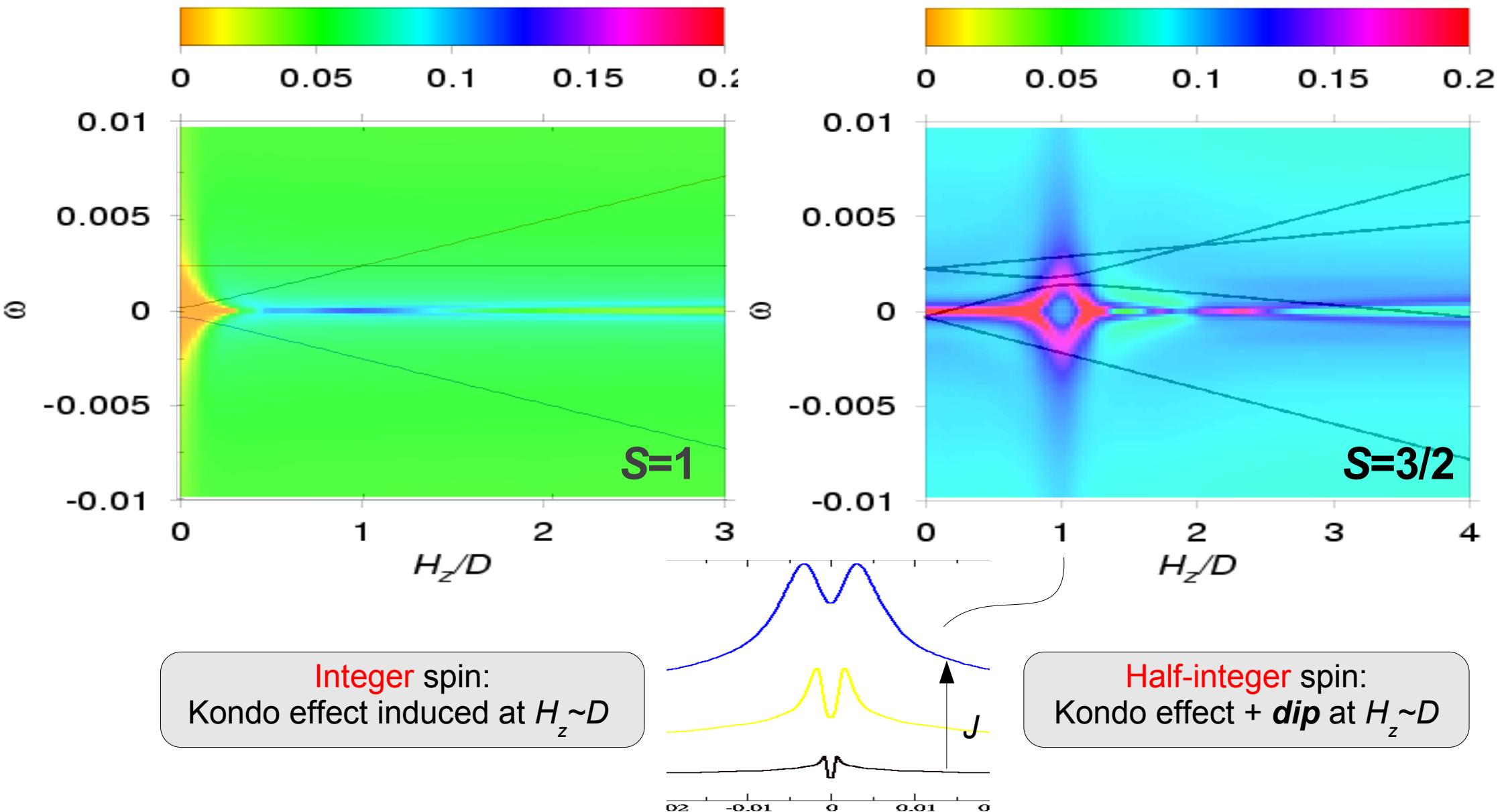
# Anticrossing: 2 sign changes



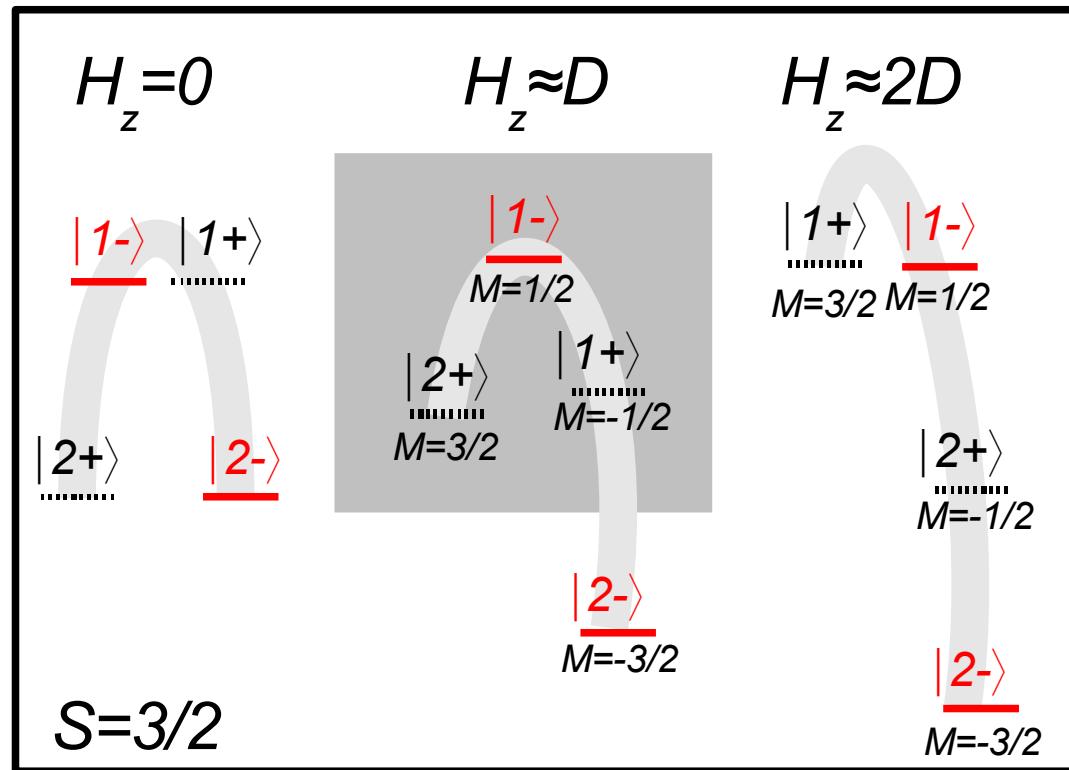
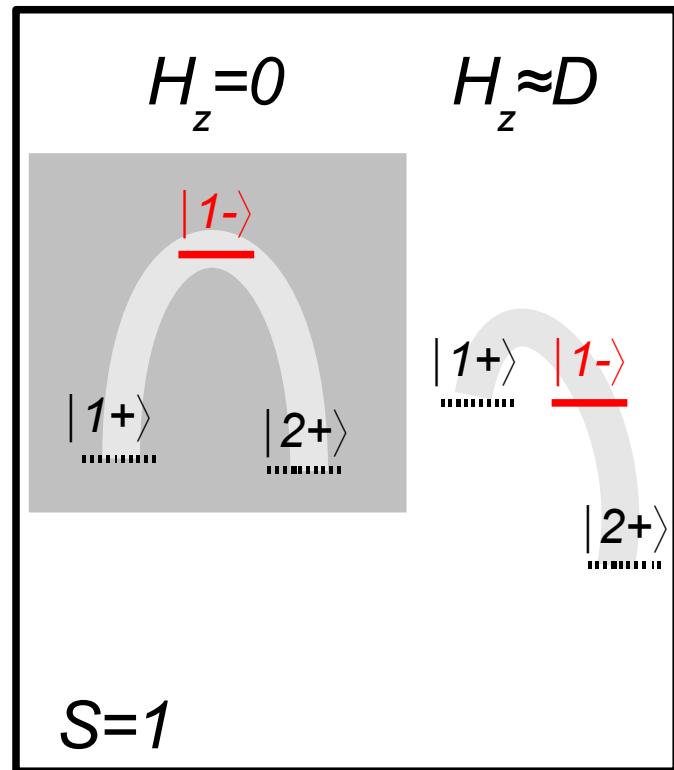
$$J_{II'}^{x,y} = J \langle +I | S_+ \pm S_- | -I' \rangle$$

(2) sign  
“magnetic weight”

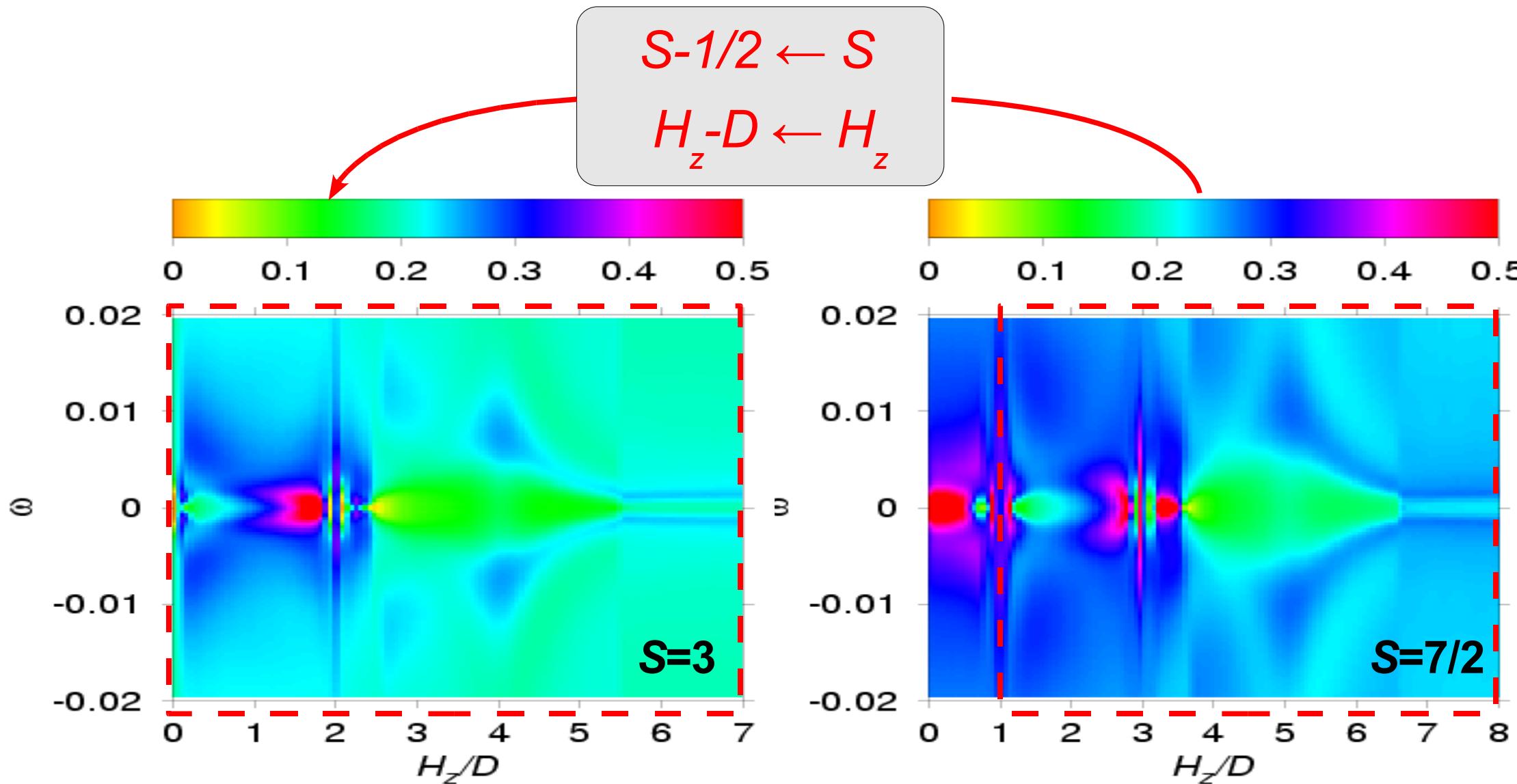
# Field induced/modulated Kondo effect



# Relation integer / half-integer spin

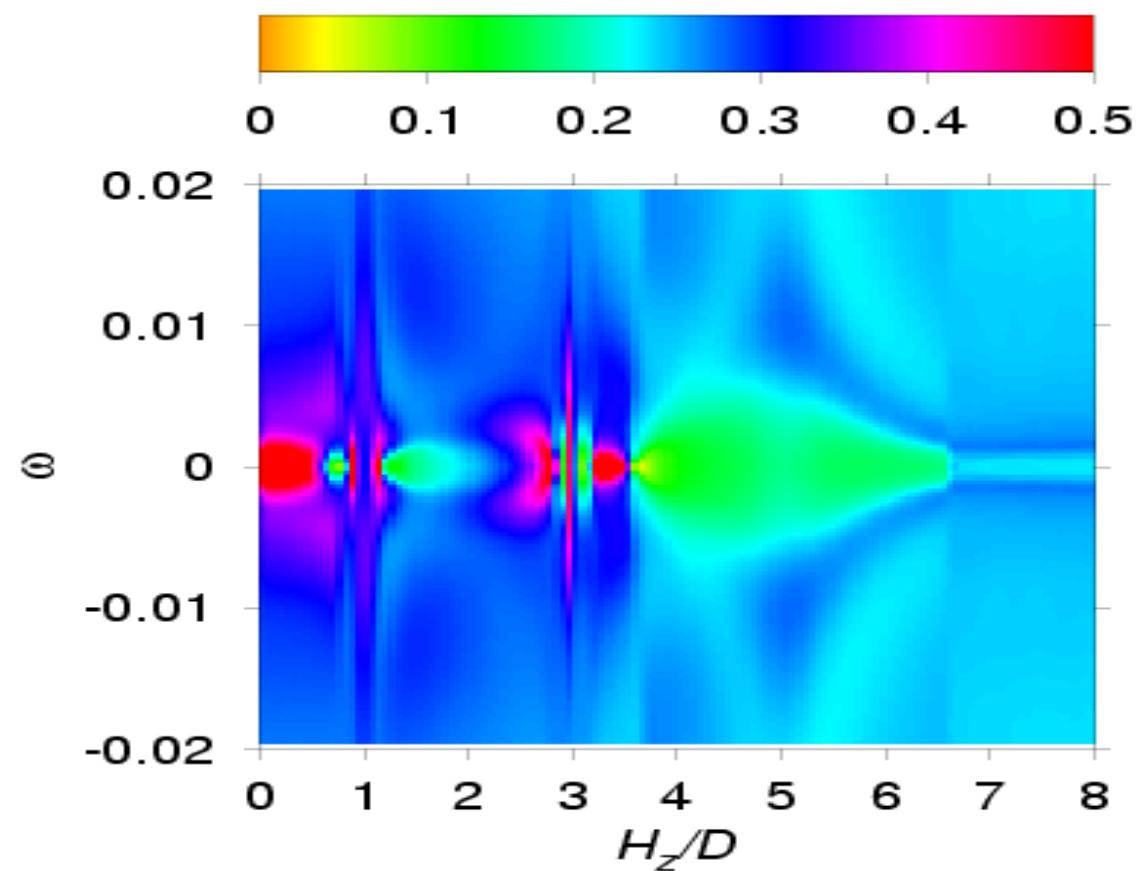


# Relation integer / half-integer spin



Parameters:  $W=1$ ,  $D=5*10^{-5}W$ ,  $B_2=0.1D$ ,  $J=0.15W$

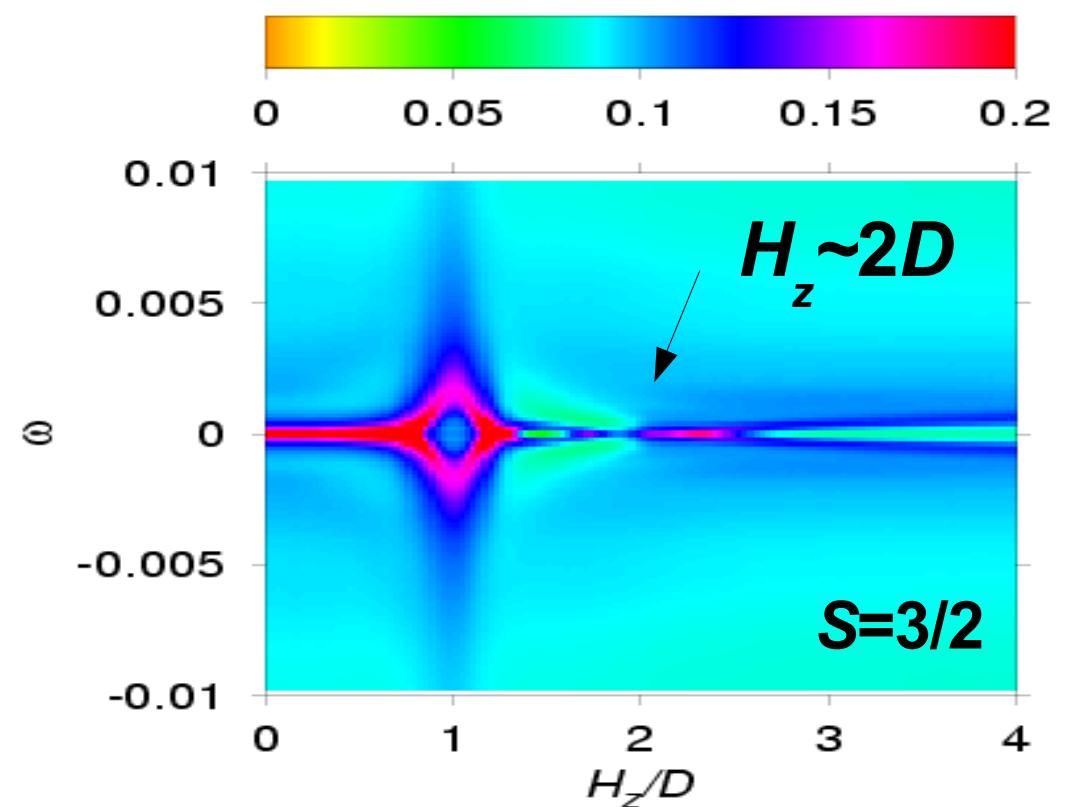
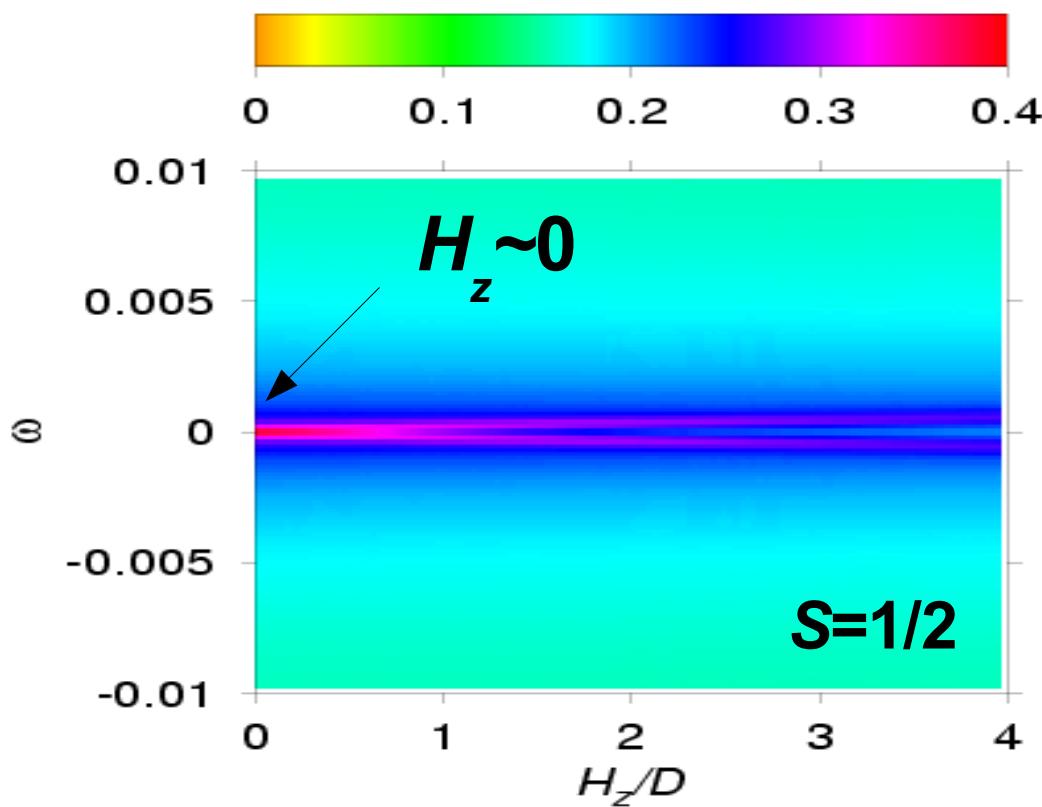
# Entertainment break



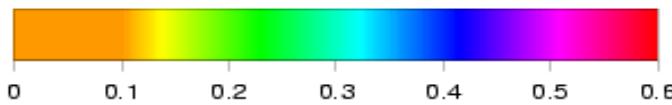
# Relation integer / half-integer spin

Iteration  
 $n=1,2,\dots,2S-1$

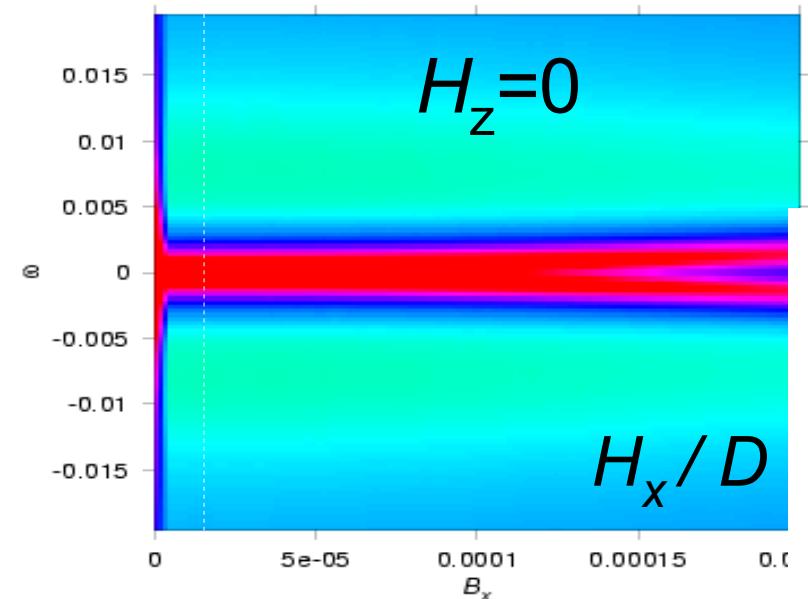
$$S-n/2, H_z \sim 0 \leftarrow S, H_z \sim nD$$



# Transverse field effect

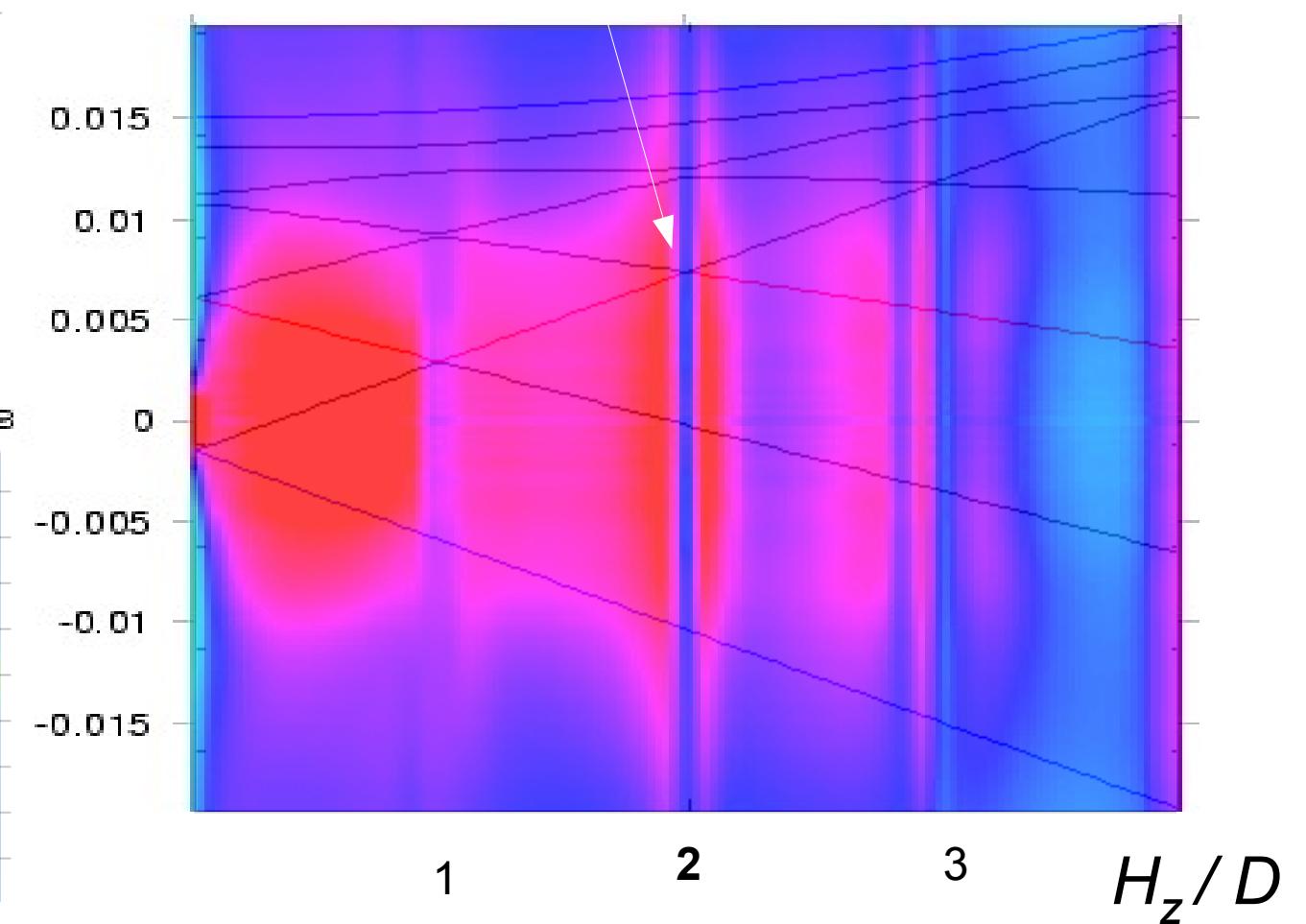
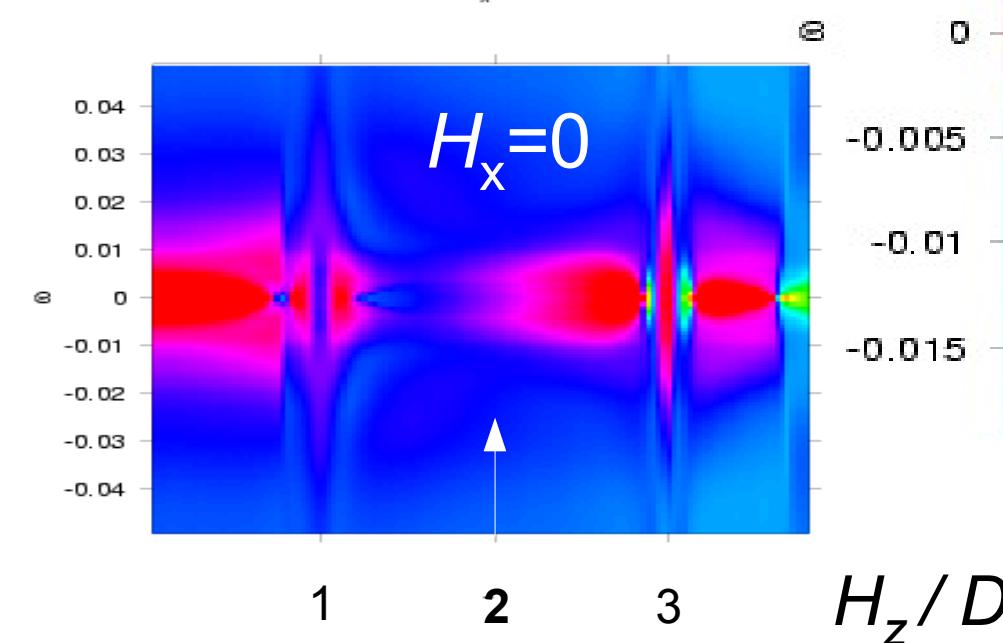


$$H_{\text{Zeeman}} = H_z S_z + H_x S_x \quad \text{easy + hard axis}$$



*Field ( $H_x$ ) induced QTM  
detected by sweeping  $H_z$*

crossing  
for  $H_x=0$



$$D=5e-5=10B2=5Bx, J=0.2$$

# Magnetic field Kondo spectroscopy

- Magnetic parameters of SMM in electrical circuit
- Magnetic field energies  $< 2 D S \sim 1 \text{ meV}$   
*no complete Zeeman splitting required*
- Temperatures  $\sim T_K \gg 2 D S \sim 1 \text{ meV}$   
*no mK required*
- Control  $J$ : tunneling distance (STM) or gate (3-terminal)
- 3-terminal transport:  
“Weak” & “strong” Kondo  $\sim$  gate-tunable  
Kondo in subsequent charge and *spin* states

