

# Introduction to electron transport in molecular systems

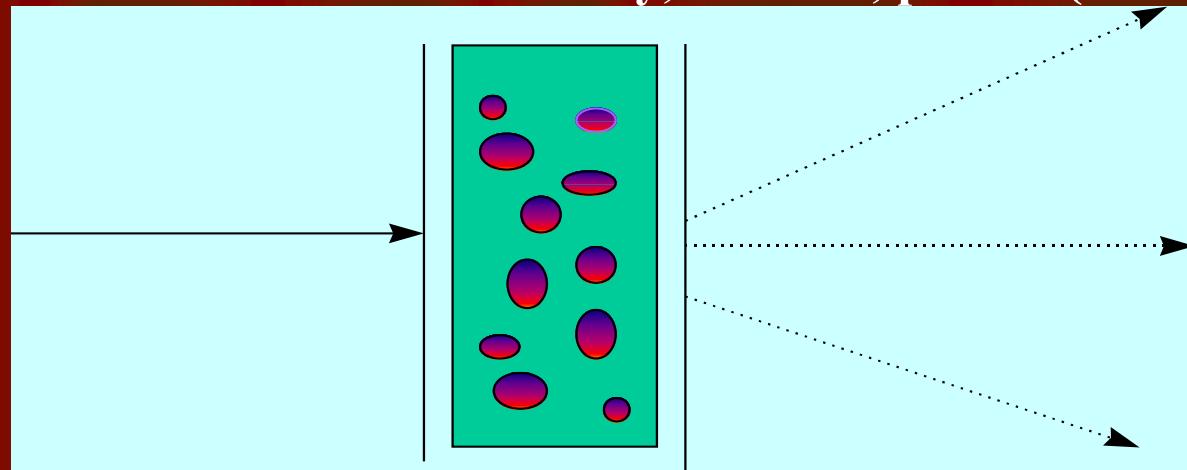
Reviews: Annu. Rev. Phys. Chem. 52, 681– 750 (2001)

[<http://atto.tau.ac.il/~nitzan/nitzanabs.html/#213>]

Science, 300, 1384-1389 (2003);

MRS Bulletin, 29, 391-395 (2004);

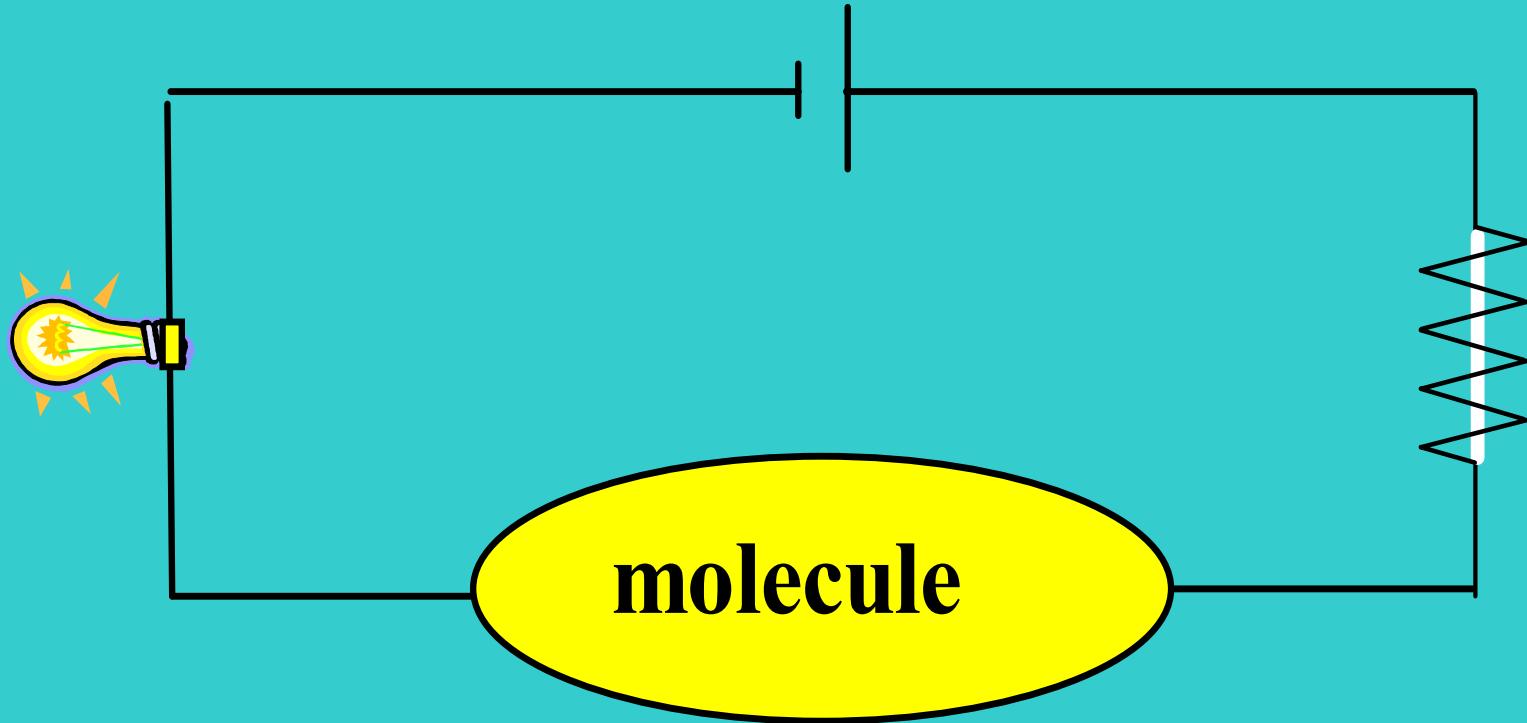
Bulletin of the Israel Chemical Society, Issue 14, p. 3-13 (Dec 2003) (Hebrew)



**Thanks**

I. Benjamin, A. Burin, G. Cuniberti, B. Davis, S. Datta, D. Evans, M. Galperin, A. Ghosh, H. Grabert, R. Gutierrez, P. Hänggi, G. Ingold, J. Jortner, S. Kohler, R. Kosloff, J. Lehmann, M. Majda, A. Mosyak, V. Mujica, R. Naaman, U. Peskin, M. Ratner, D. Segal, T. Seideman, H. Tal-Ezer

# Molecules as conductors



# **Molecular Rectifiers**

*Aviram Ratner*

**Arieh Aviram and Mark A. Ratner**

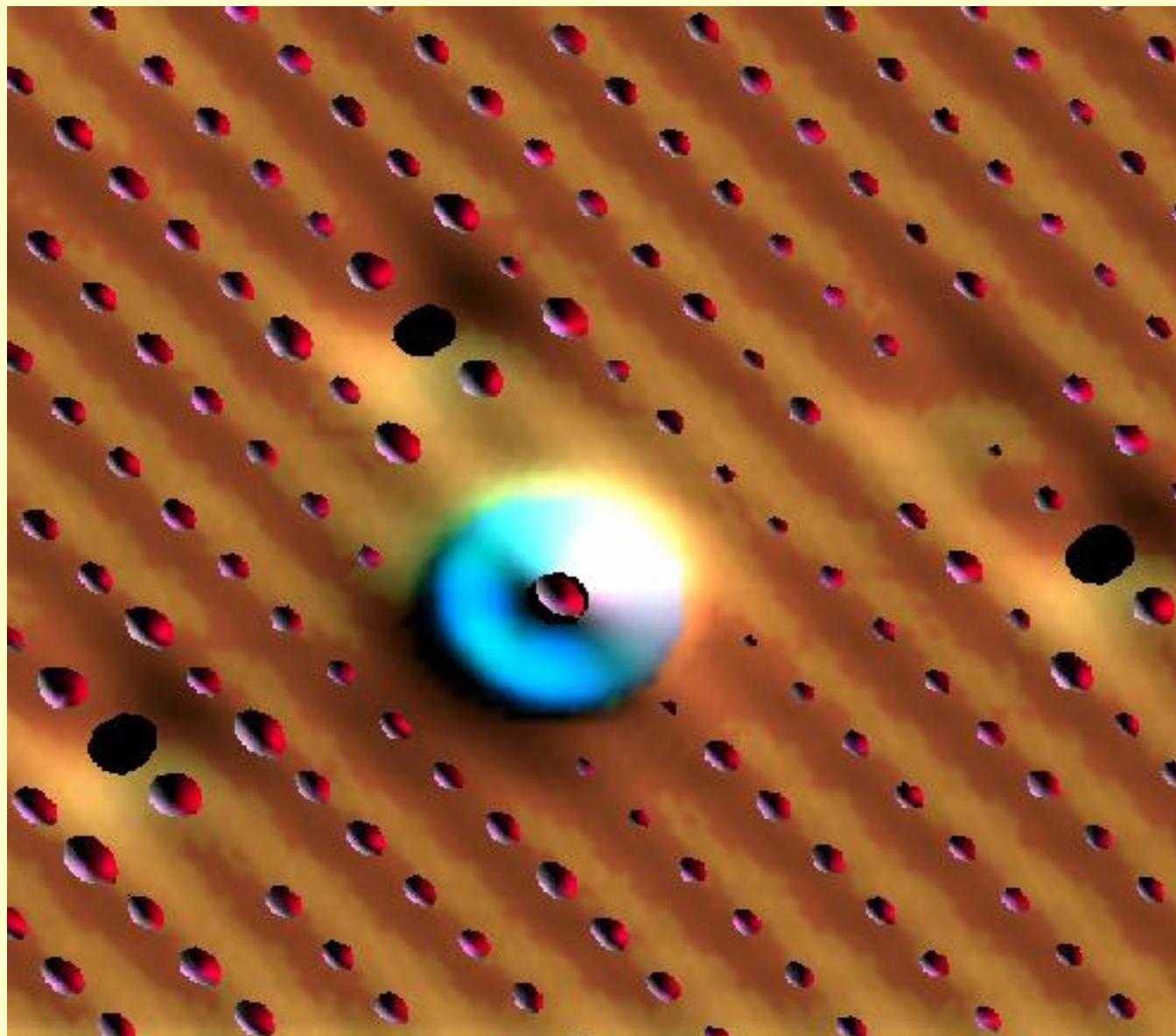
**IBM Thomas J. Watson Research Center, Yorktown Heights, New  
York 10598, USA**

**Department of Chemistry, New York New York University, New  
York 10003, USA**

**Received 10 June 1974**  
**Abstract**

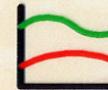
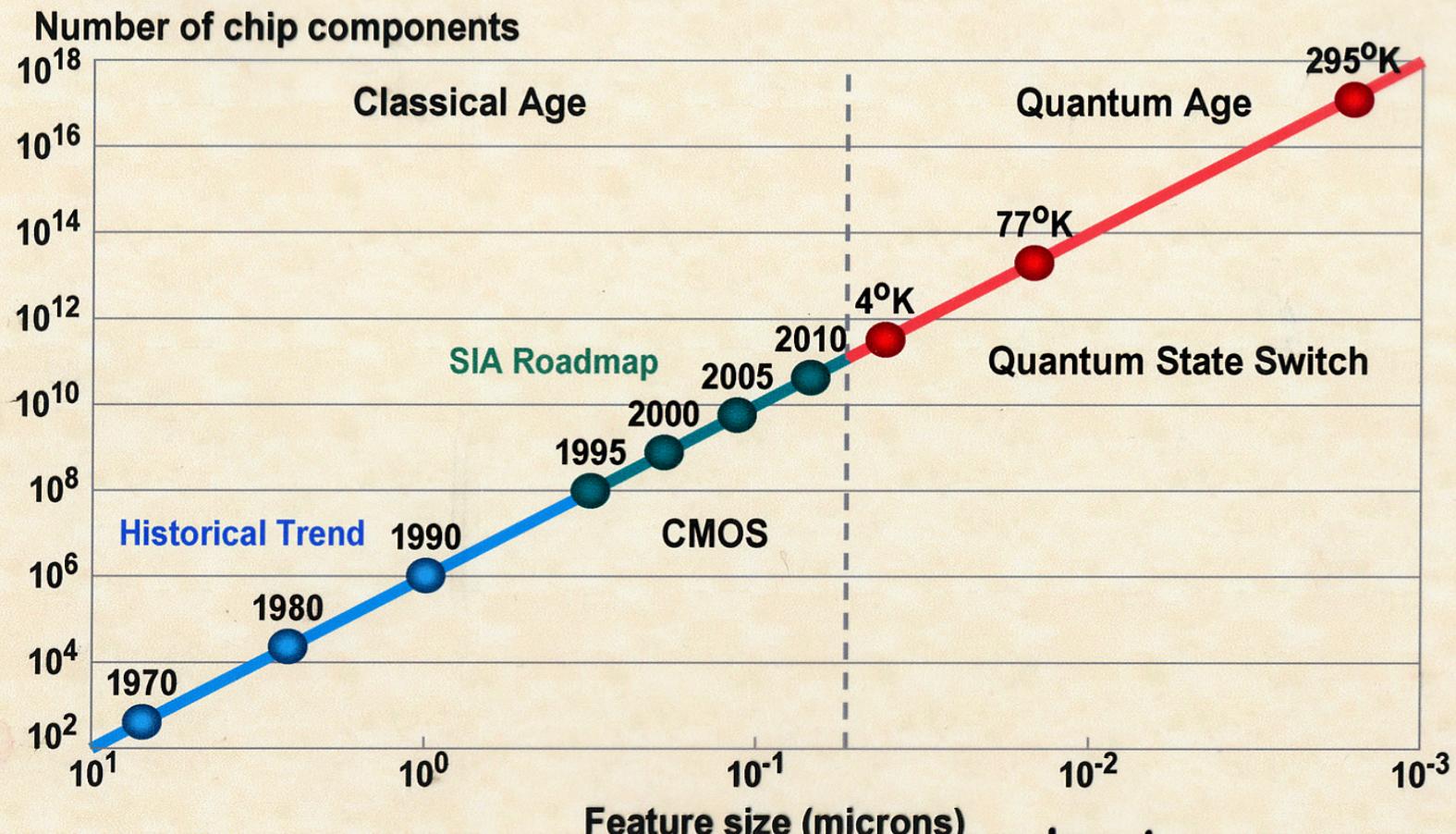
**The construction of a very simple electronic device, a rectifier, based on the use of a single organic molecule is discussed. The molecular rectifier consists of a donor pi system and an acceptor pi system, separated by a sigma-bonded (methylene) tunnelling bridge. The response of such a molecule to an applied field is calculated, and rectifier properties indeed appear.**

# Xe on Ni(110)



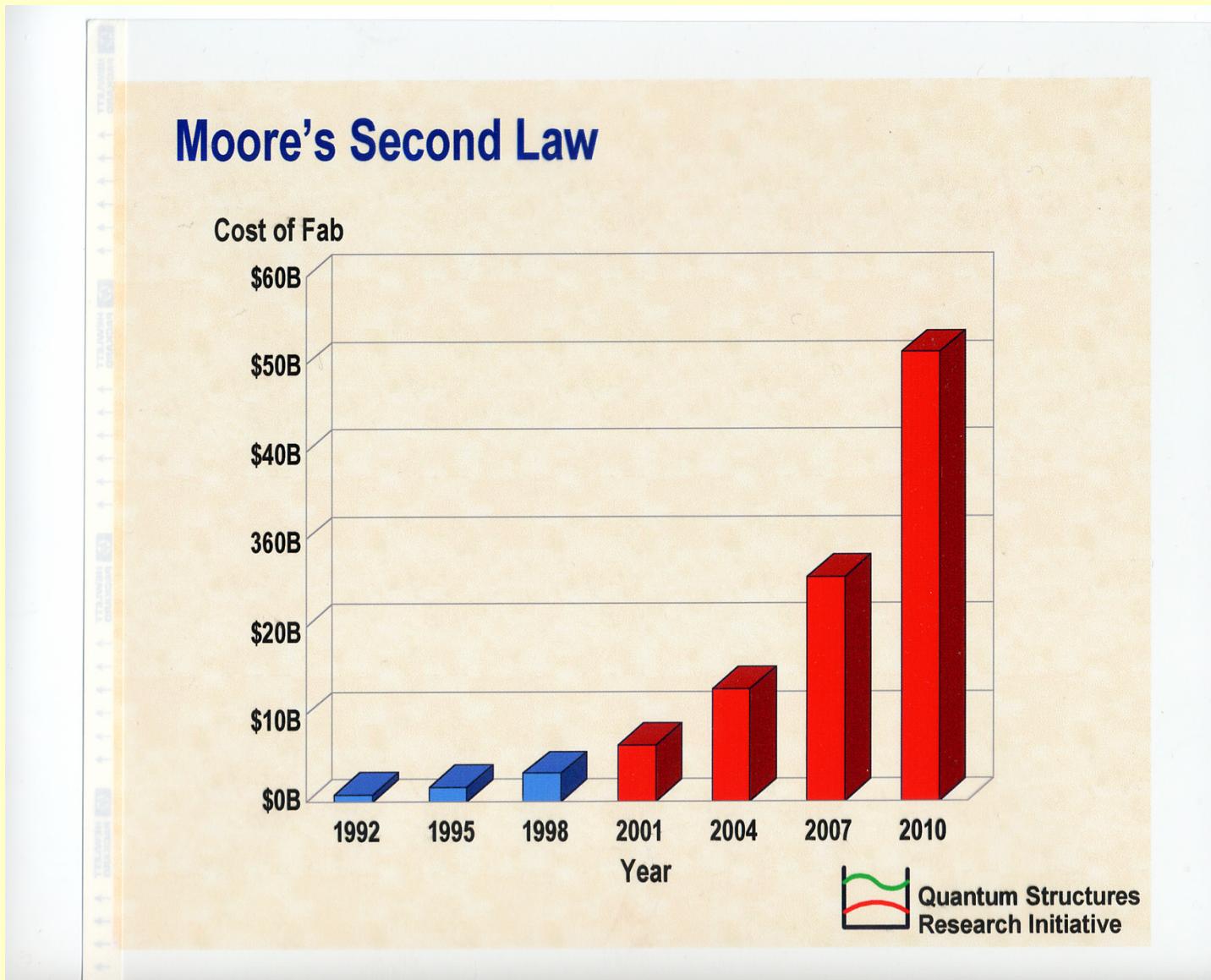
# Moore's "Law"

## Scaling of electronic devices



Quantum Structures  
Research Initiative

# Moore's 2nd law



# Molecules get wired



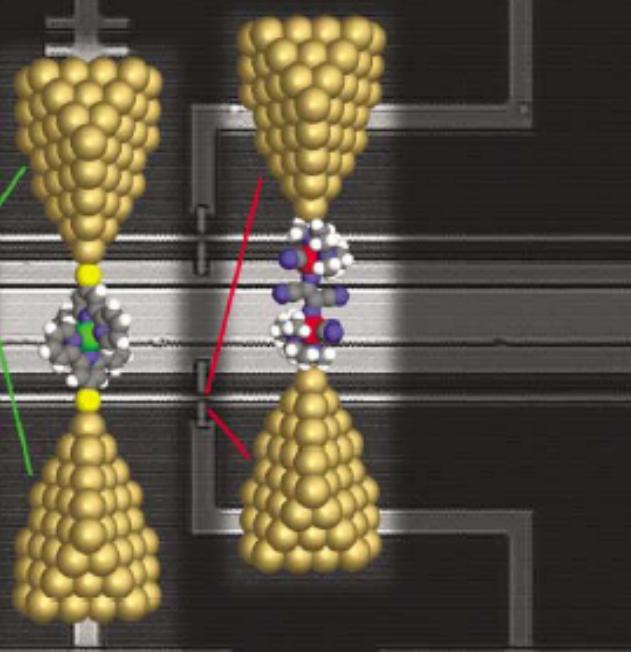
13 June 2002

International weekly journal of science

# nature

v 415

[www.nature.com/nature](http://www.nature.com/nature)



## Electronics at the atomic scale

**Antibiotic-resistant enterococci** Islands of pathogenicity

**Asteroid families** Aftermath of a recent break-up

**Non-human primates** When can experiments be justified?

**new on the market**  
microscopy

**Cornell group**

IEEE TRANSACTIONS ON ELECTRON DEVICES VOL.43  
OCTOBER 1996 1637

# Need for Critical Assessment

Rolf Landauer,*Life Fellow, IEEE*

## Abstract

**Adventurous technological proposals are subject to inadequate critical assessment. It is the proponents who organize meetings and special issues. Optical logic, mesoscopic switching devices and quantum parallelism are used to illustrate this problem.**

This editorial, disguised as a scientific paper, is obviously a plan for more honesty. We do not, in the long run, build effective public support for science and technology by promising more than we can deliver.

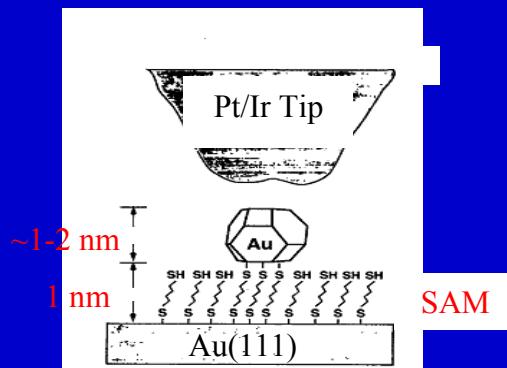
# Feynman

- For a successful Technology, reality must take precedence over public relations, for nature cannot be fooled

# First Transport Measurements through Single Molecules

Adsorbed molecule  
addressed by STM tip

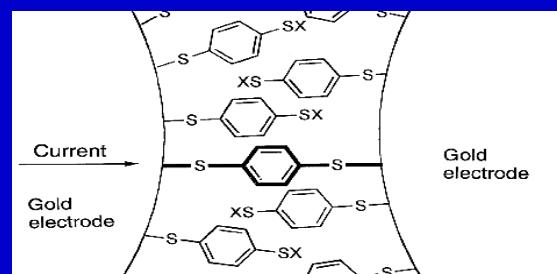
Self-assembled monolayers



Dorogi *et al.* PRB 52 (95) @  
Purdue

Molecule between  
two electrodes

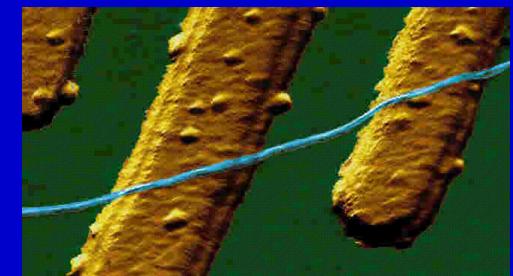
Break junction:  
dithiols between gold



Reed *et al.* Science 278 (97) @ Yale

Molecule lying  
on a surface

Single-wall carbon  
nanotube on Pt



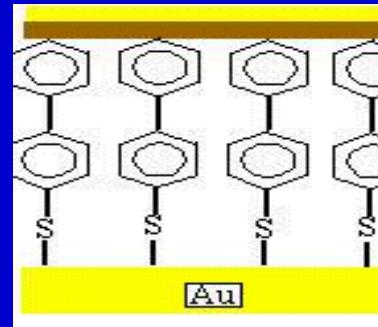
Dekker *et al.* Nature 386(97)

C<sub>60</sub> on gold

STM  
tip      Au

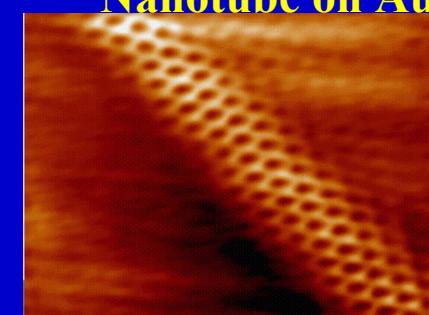
Joachim *et al.* PRL 74 (95)

Nanopore

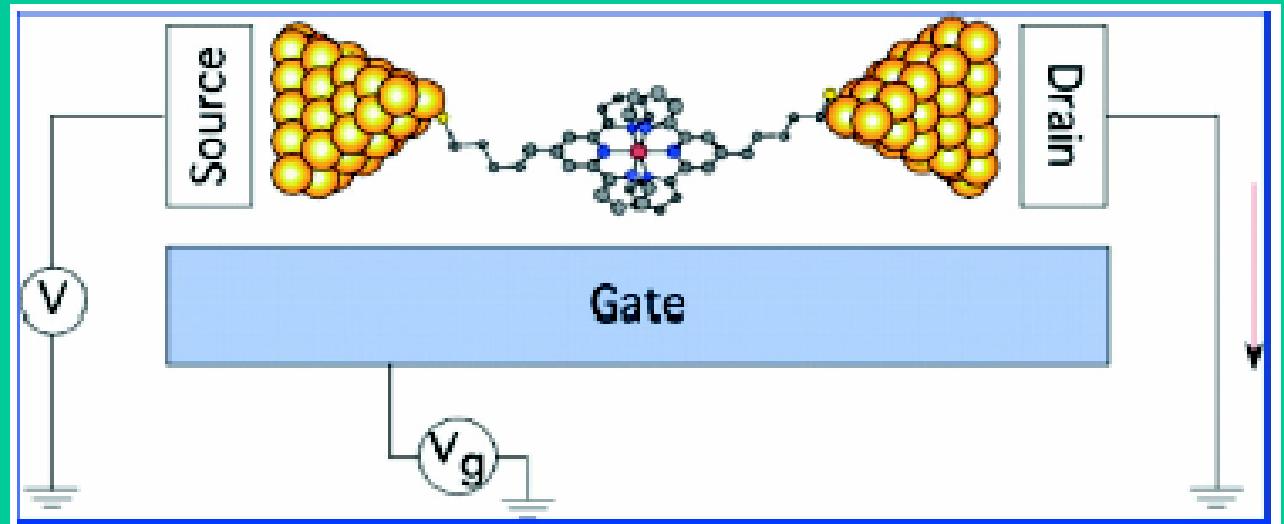
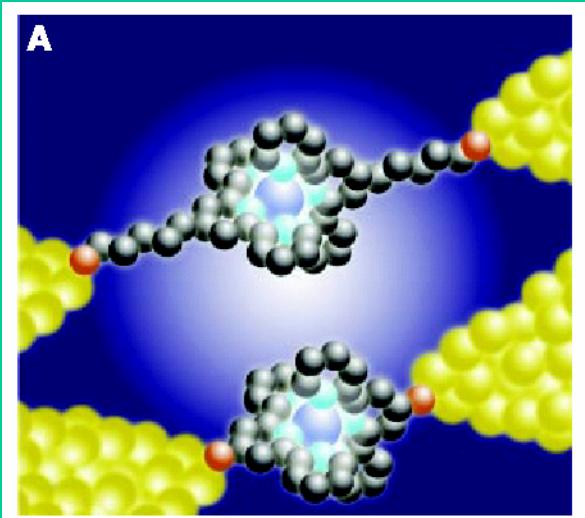


Reed *et al.* APL 71 (97)

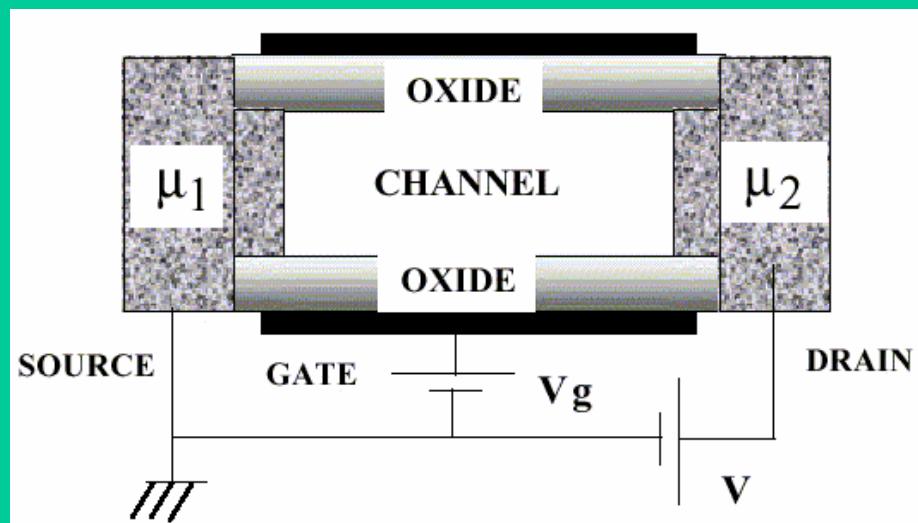
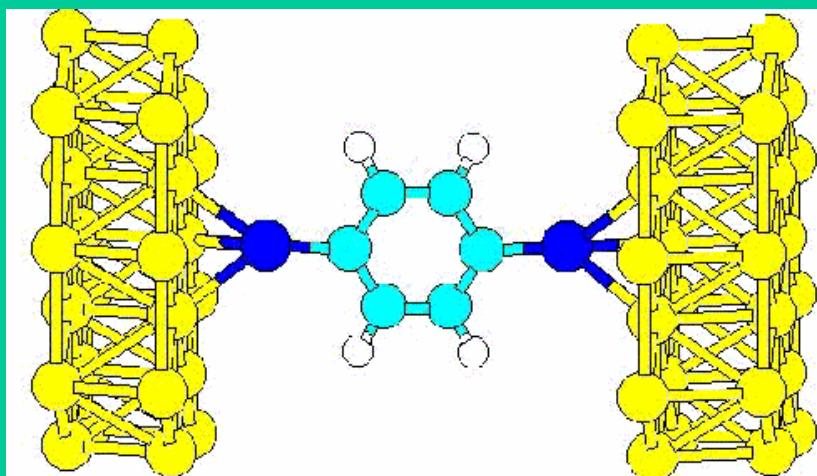
Nanotube on Au



Lieber *et al.* Nature 391 (98)

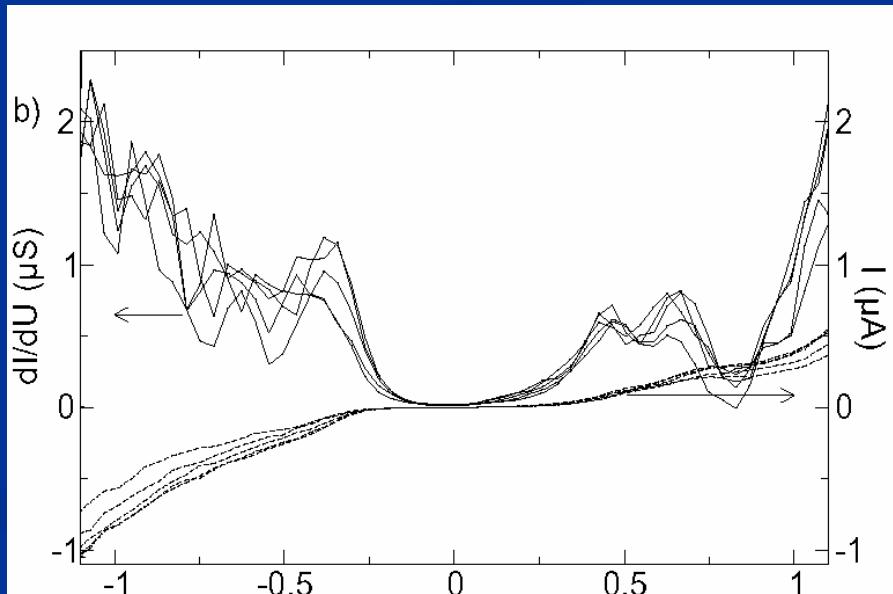
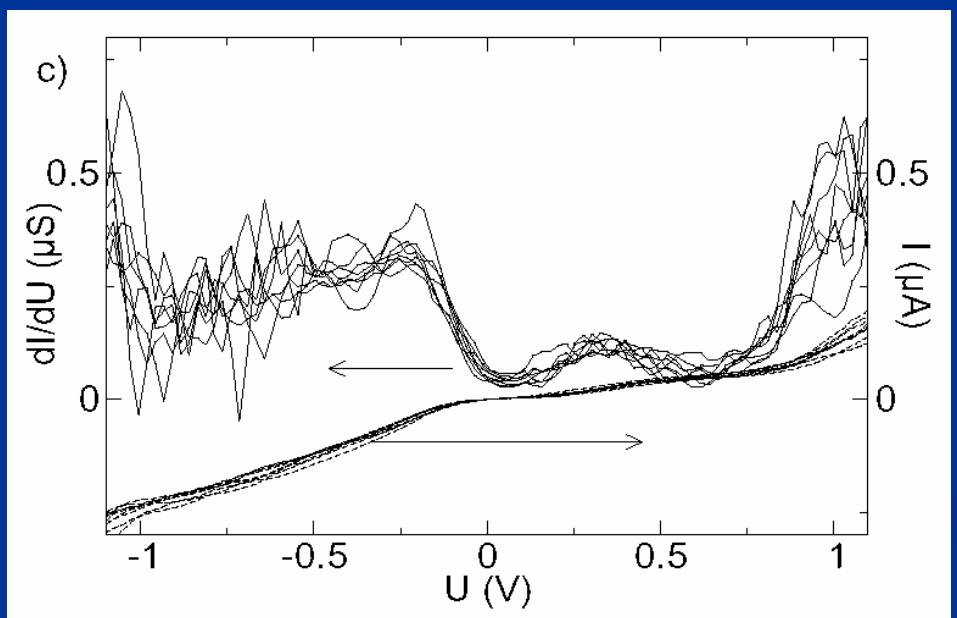
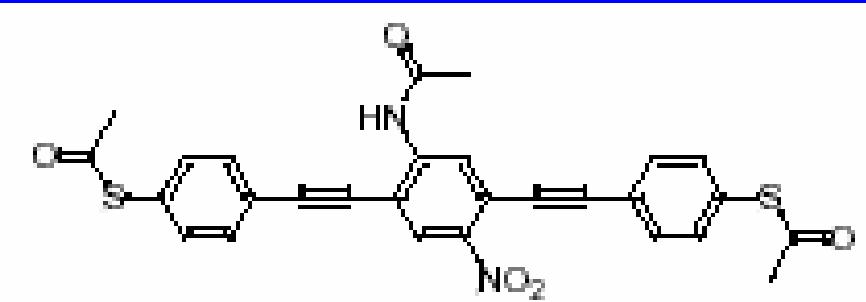
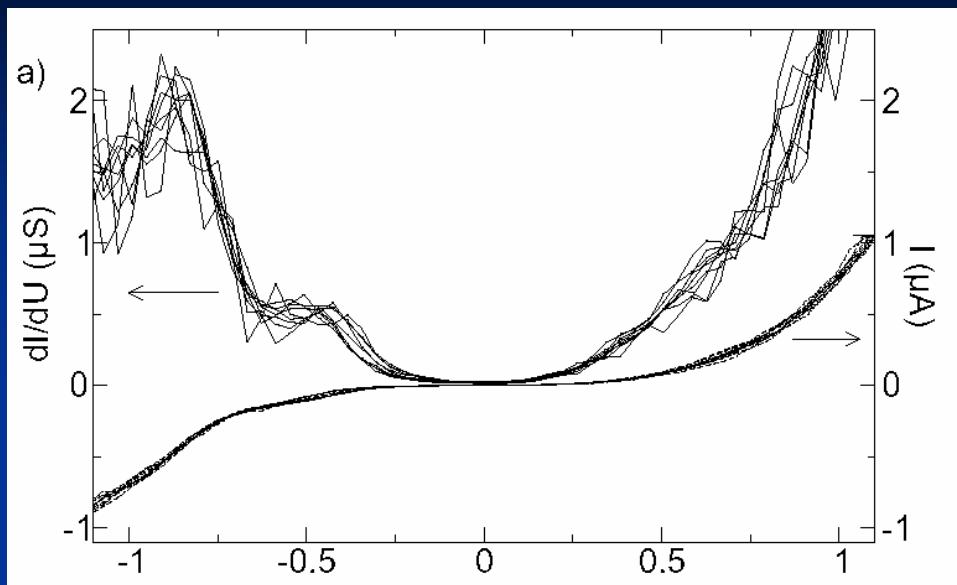


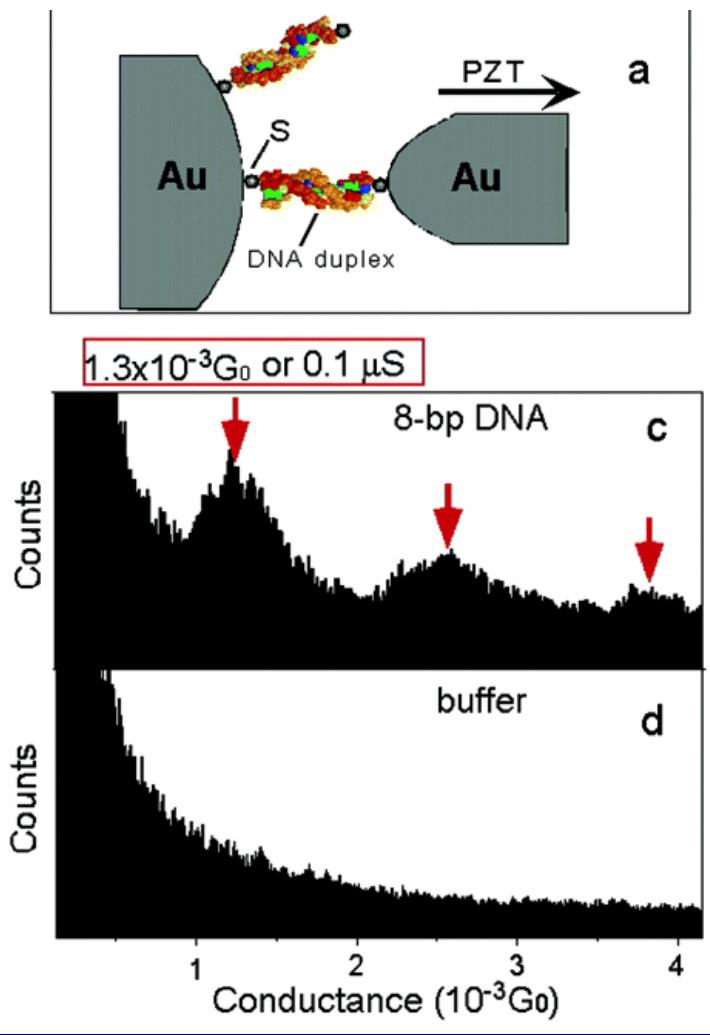
Park et. al. Nature 417,722-725 (2002)



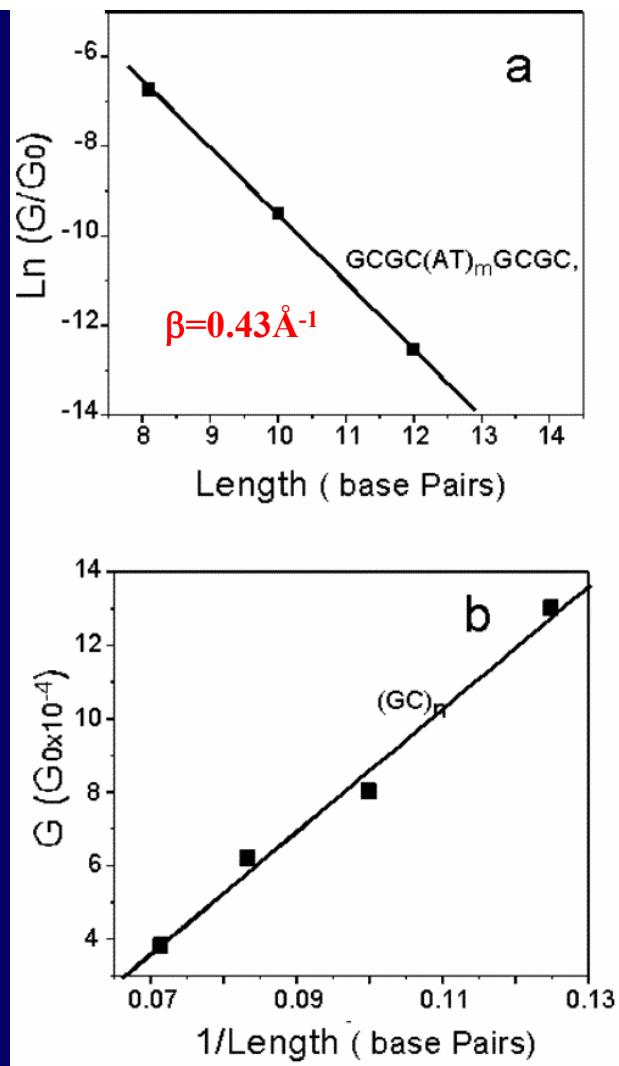
Datta et al

Weber et al, Chem. Phys. 2002





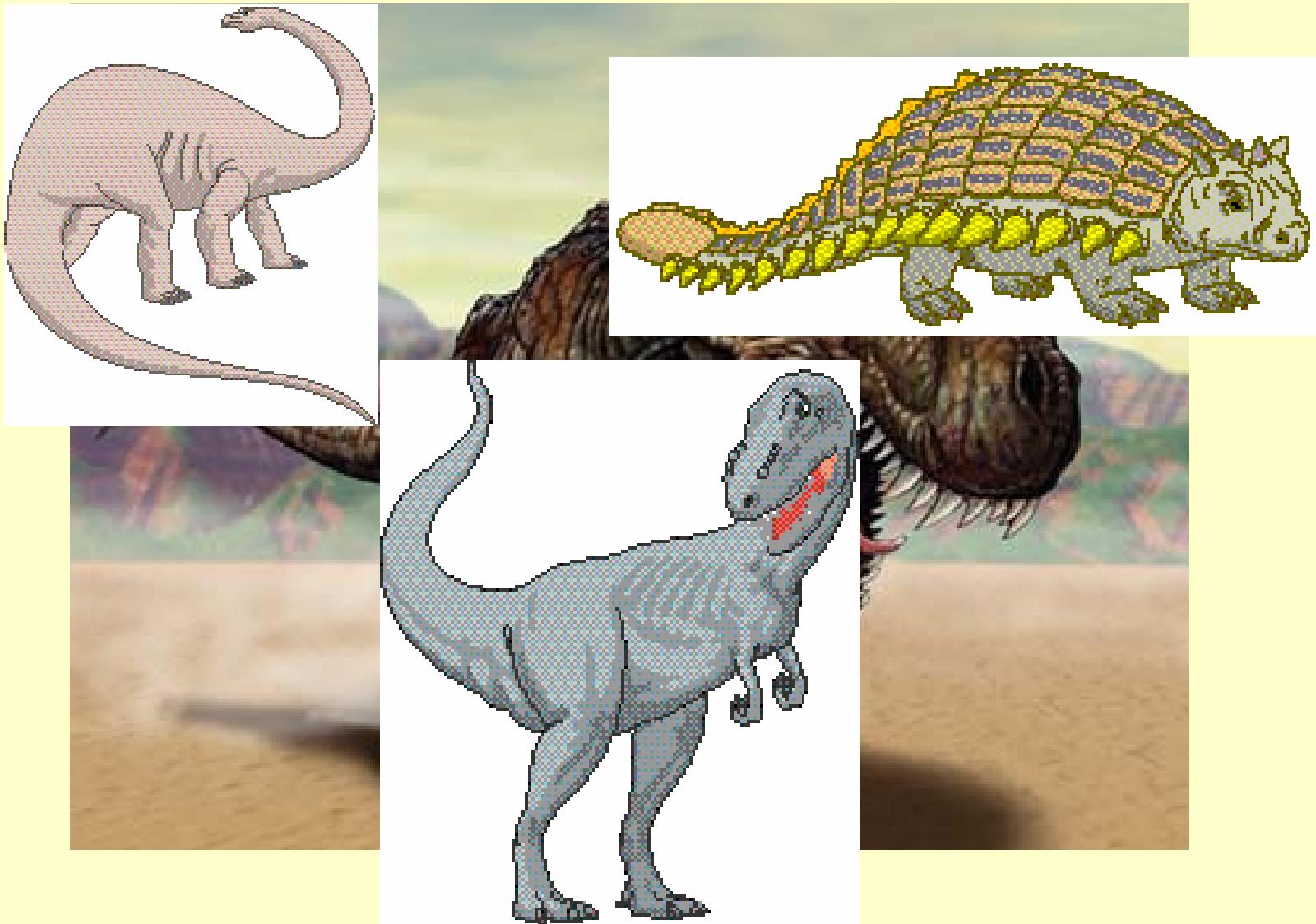
Xu et al (Tao),  
NanoLet (2004)



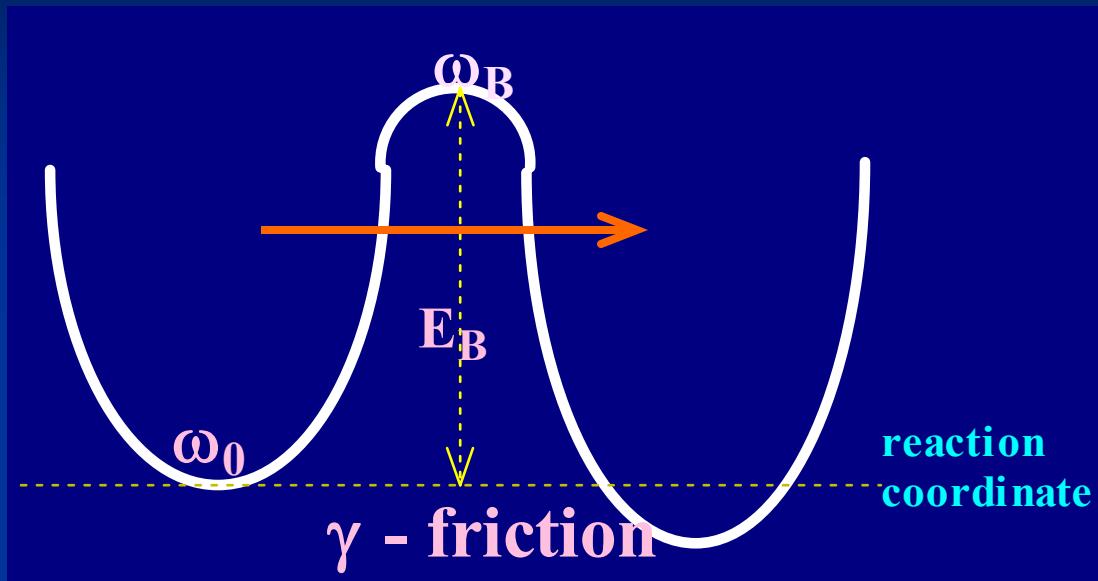
**(a)**  $\ln(G/G_0)$  vs Length (base Pairs). The data points for GCGC(AT)<sub>m</sub>GCGC show a linear decrease. A solid line is a linear fit to the data. The slope is  $\beta = 0.43 \text{\AA}^{-1}$ .

**(b)**  $G$  ( $G_0 \times 10^{-4}$ ) vs 1/Length (base Pairs). The data points for (GC)<sub>n</sub> show a linear increase, indicating a positive correlation between conductance and GC content.

# AT THE BEGINNING...



# Activated rate processes



KRAMERS THEORY:

Low friction limit →

$$k = \frac{\gamma}{k_B T} \omega_0 e^{-E_B / k_B T}$$

(action)

High friction limit →

$$k = \frac{\omega_0 \omega_B}{2\pi\gamma} e^{-E_B / k_B T} = k_{TST} \frac{\omega_B}{\gamma}$$

Transition State theory →

$$k_{TST} = \frac{\omega_0}{2\pi} e^{-E_B / k_B T}$$

Diffusion controlled rates

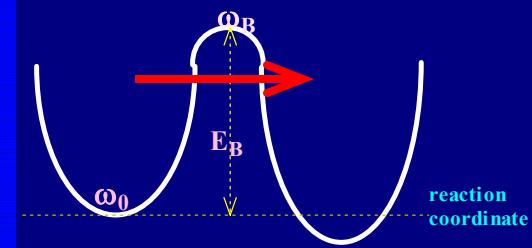
$$k = 4\pi DR$$

$$D = \frac{k_B T}{m\gamma}$$

# The physics of transition state rates

Assume:

(1) Equilibrium in the well



(2) Every trajectory on the barrier that goes out makes it

$$k_{TST} = \int_0^\infty d\mathbf{v} \mathbf{v} P(x_B, \mathbf{v}) = \langle \mathbf{v}_f \rangle P(x_B) = \frac{\omega_0}{2\pi} e^{-\beta E_B}$$

$$\frac{\int_0^\infty d\mathbf{v} \mathbf{v} e^{-\frac{1}{2}\beta m \mathbf{v}^2}}{\int_{-\infty}^\infty d\mathbf{v} e^{-\frac{1}{2}\beta m \mathbf{v}^2}} = \frac{1}{\sqrt{2\pi\beta m}}$$

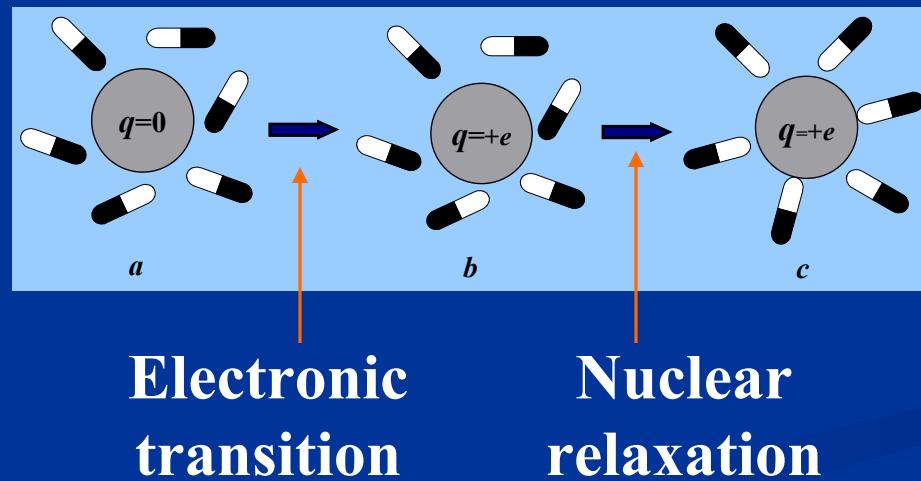
$$P(x_B) = \frac{\exp(-\beta E_B)}{\int_{-\infty}^{E_B} dx \exp(-\beta V(x))} = \sqrt{\frac{\beta m \omega_0^2}{2\pi}} e^{-\beta E_B}$$

# Theory of Electron Transfer

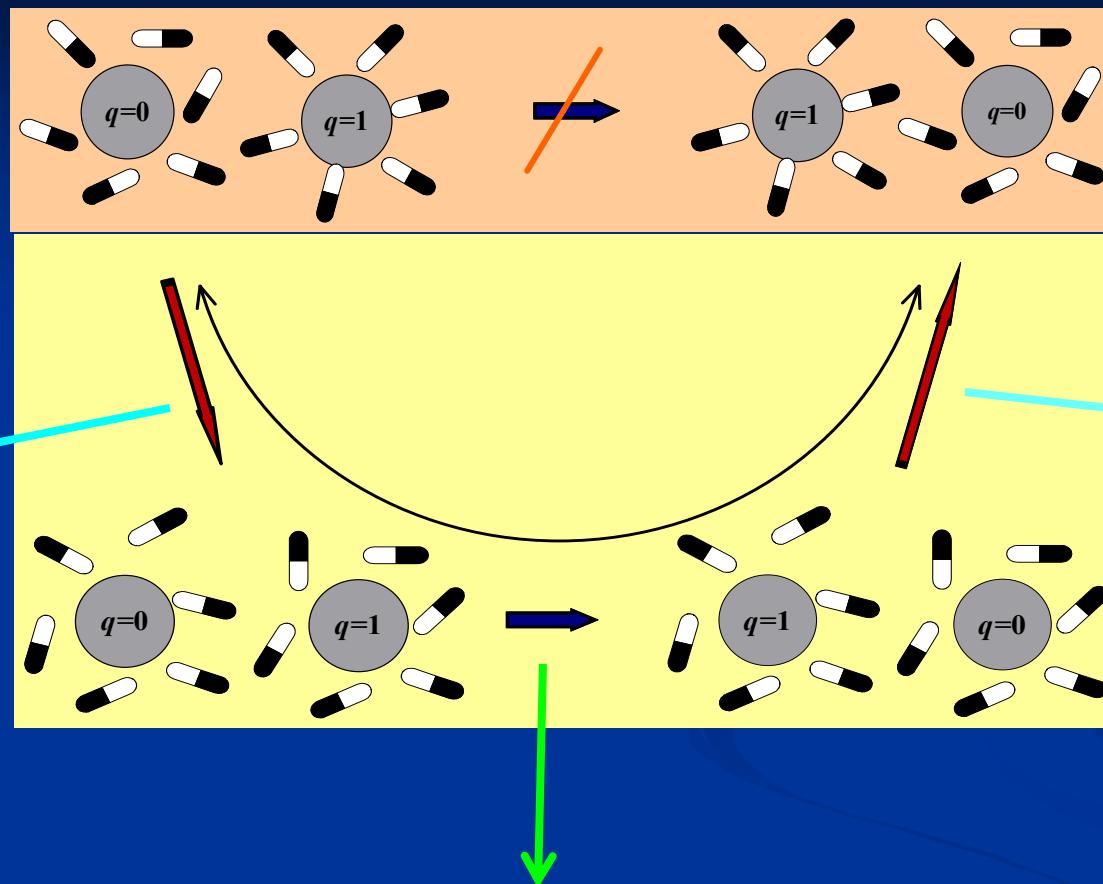
- Activation energy
- Transition probability
- Rate – Transition state theory or solvent controlled

# Electron transfer in polar media

- Electron are much faster than nuclei
- → Electronic transitions take place in fixed nuclear configurations
- → Electronic energy needs to be conserved during the change in electronic charge density

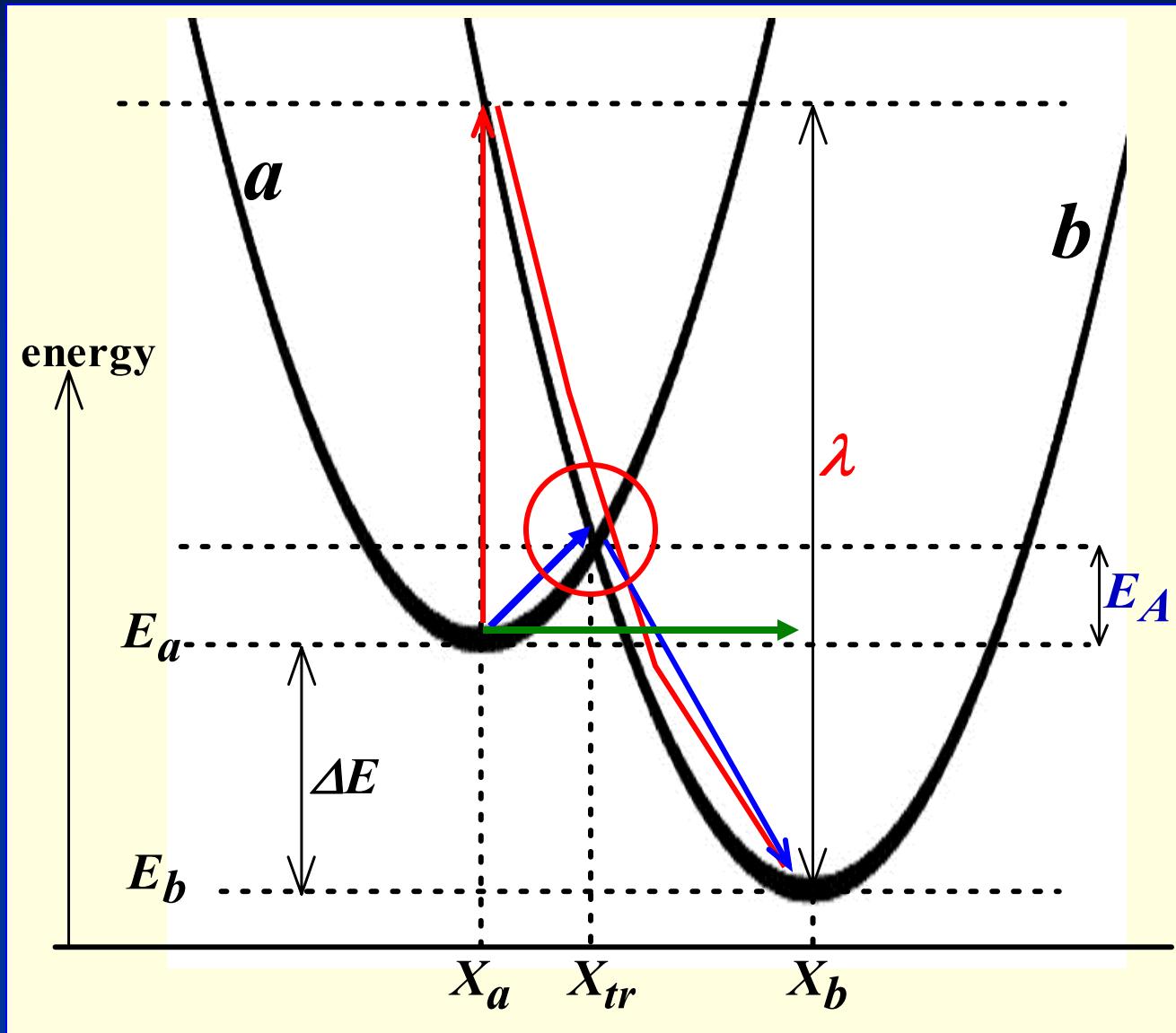


# Electron transfer



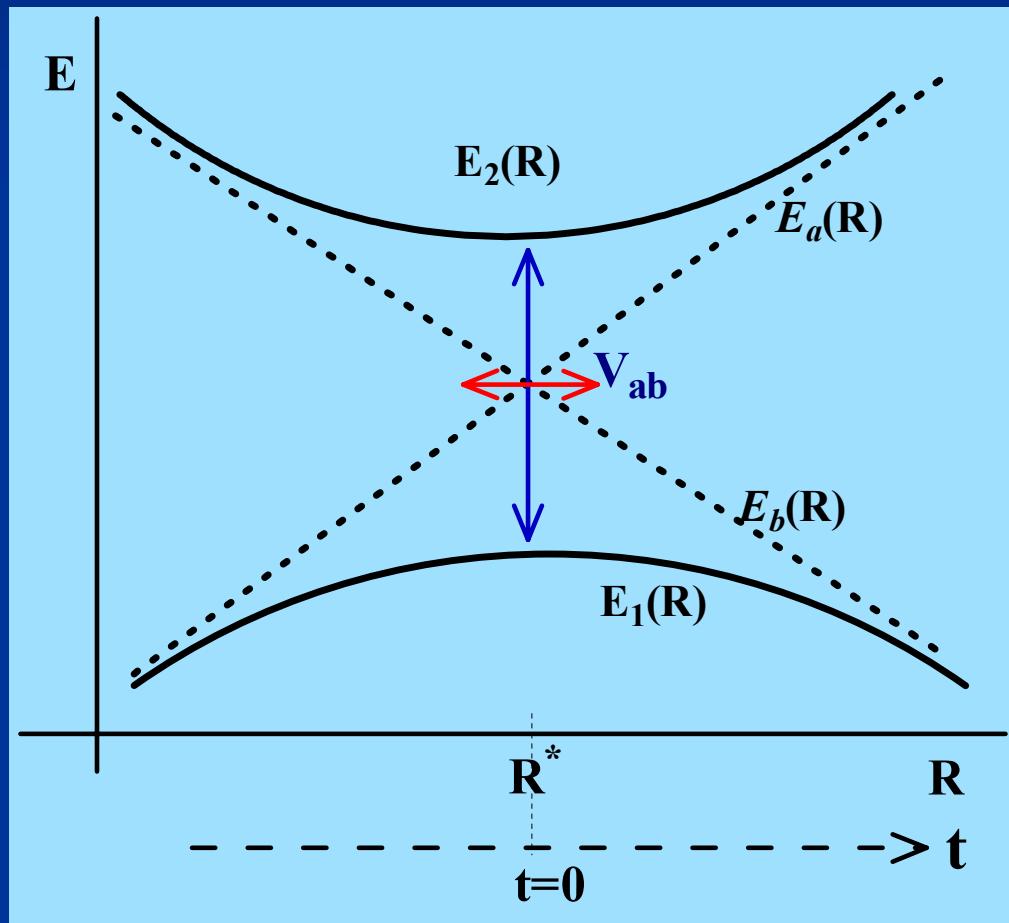
Electron transition takes place in unstable nuclear configurations obtained via thermal fluctuations

# Electron transfer



# Transition state theory of electron transfer

Alternatively –  
solvent control  
**Adiabatic and non-adiabatic ET processes**



## Landau-Zener problem

$$k = \int_0^\infty d\dot{R} \dot{R} P(R^*, \dot{R}) P_{b \leftarrow a}(\dot{R})$$

$$P_{b \leftarrow a}(\dot{R}) = 1 - \exp \left\{ -\frac{2\pi |V_{a,b}|^2}{\hbar |\dot{R} \Delta F|} \right\}_{R=R^*}$$

$$k_{NA} = \sqrt{\frac{\pi \beta K}{2}} \frac{|V_{a,b}|^2}{\hbar |\Delta F|_{R=R^*}}$$

# Electron transfer: Marcus theory

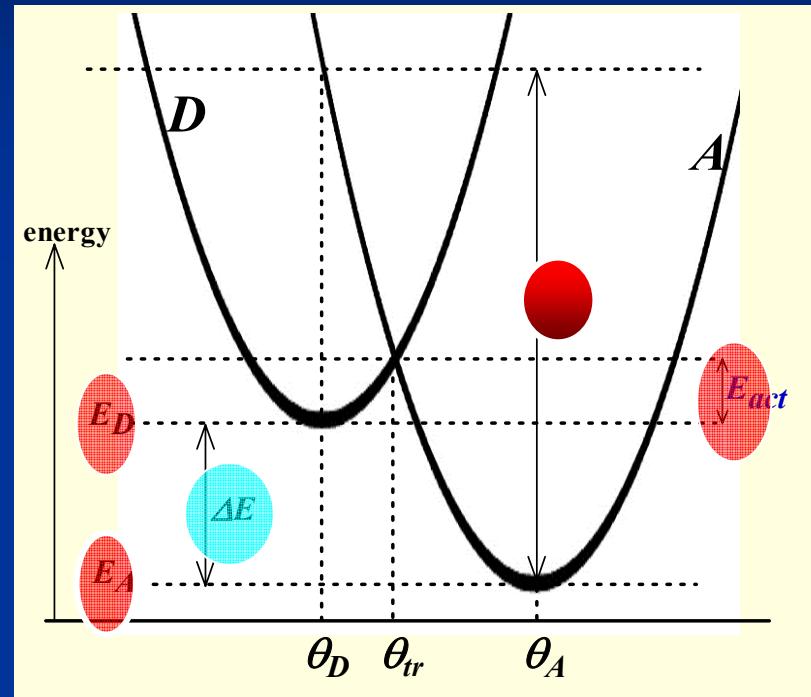
$$W_0(\theta) = E_0 + \lambda\theta^2$$

$$W_1(\theta) = E_1 + \lambda(1-\theta)^2$$

$$k_{DA} \sim \mathcal{F}(E_{AD}) = \frac{e^{-(\lambda+E_{AD})^2/4\lambda k_B T}}{\sqrt{4\pi\lambda k_B T}}$$

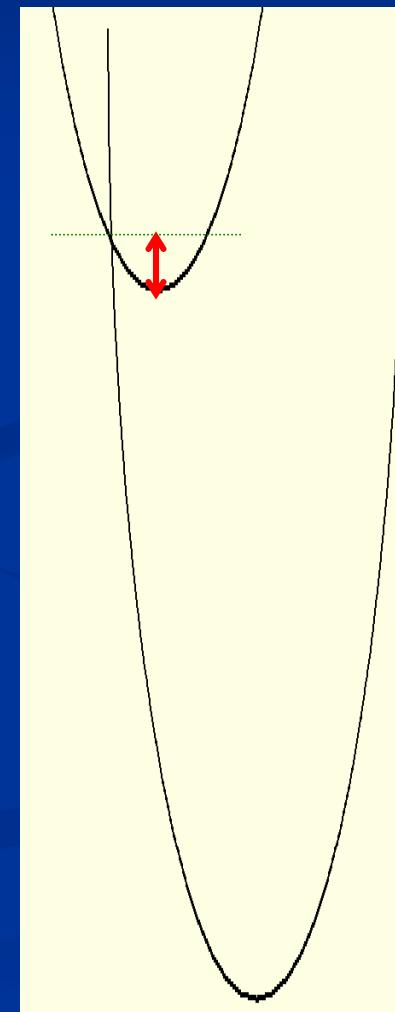
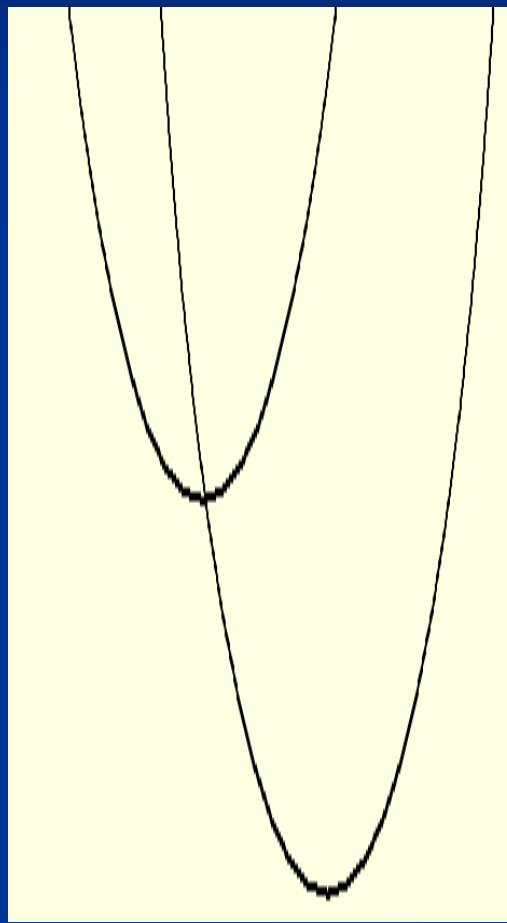
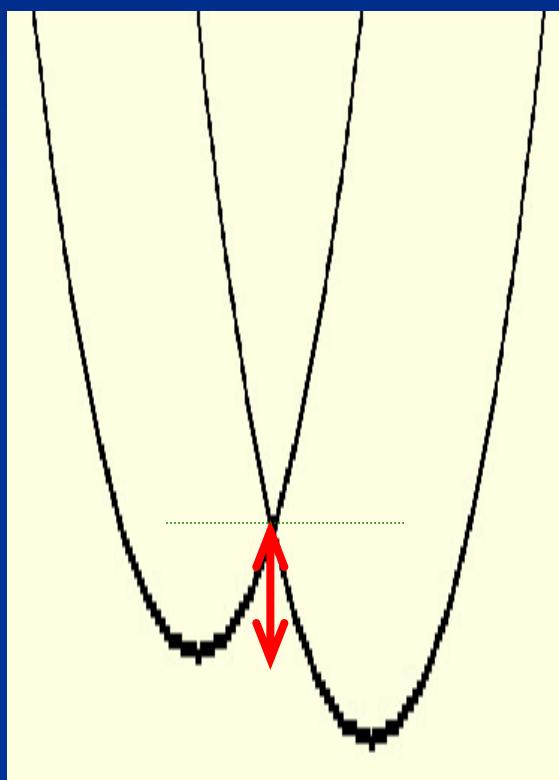
$$E_{AD} = \Delta E = E_A - E_D$$

$$E_A = \frac{[(E_A - E_D) + \lambda]^2}{4\lambda}$$

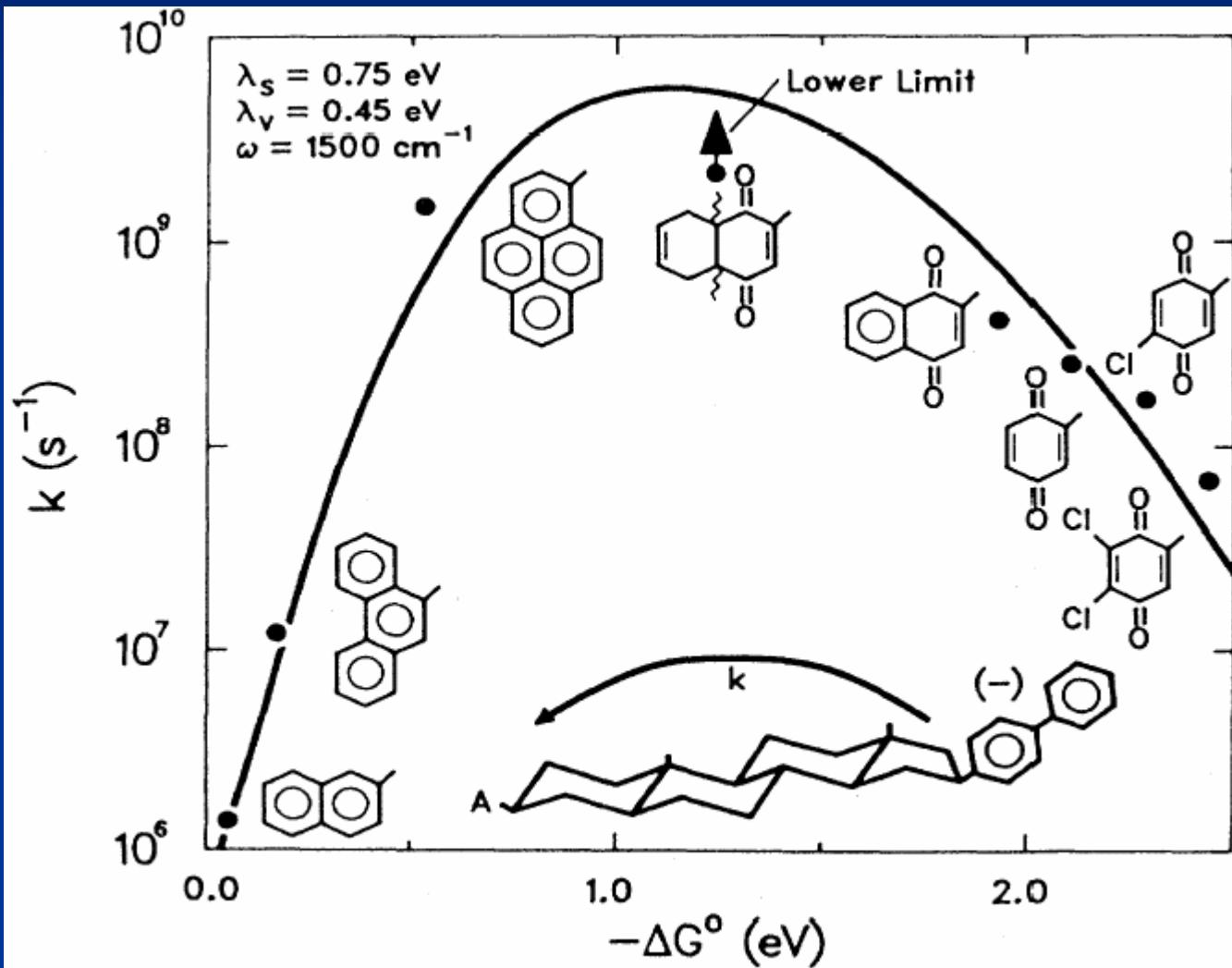


$$\lambda = \left( \frac{1}{\epsilon_e} - \frac{1}{\epsilon_s} \right) \left( \frac{1}{2R_A} + \frac{1}{2R_B} - \frac{1}{R_{AB}} \right) \Delta q^2$$

# Electron transfer: Effect of Driving (=energy gap)



# Experimental confirmation of the inverted regime



Miller et al,  
JACS(1984)

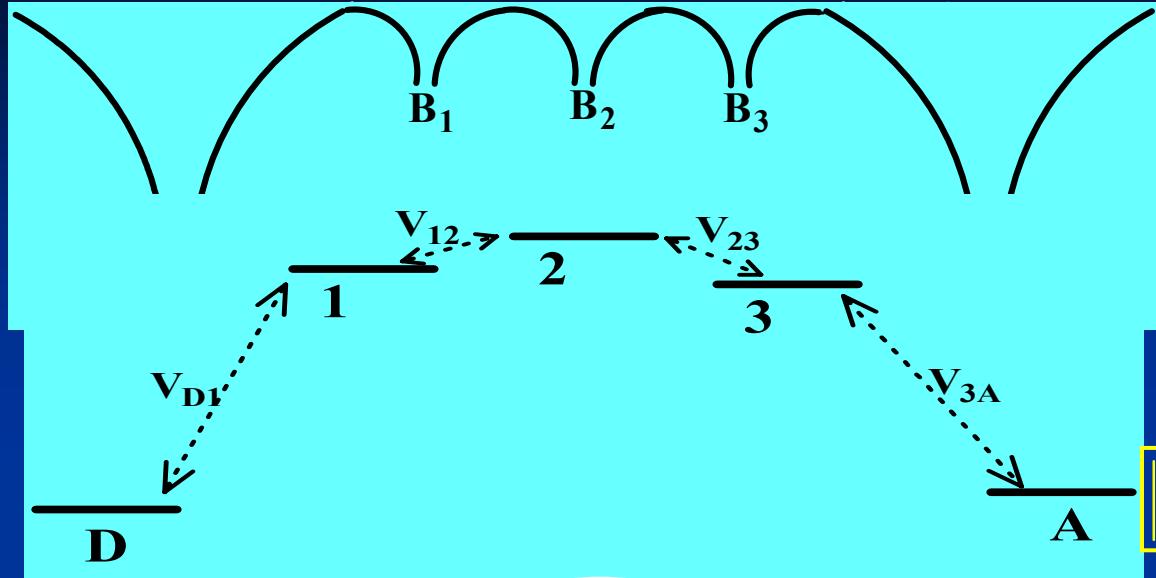
Marcus Nobel  
Prize: 1992

# Electron transfer – the coupling

- From Quantum Chemical Calculations
- The Mulliken-Hush formula

$$| H_{DA} | = \frac{\hbar \omega_{\max} |\mu_{12}|}{eR_{DA}}$$

- Bridge mediated electron transfer



on transfer

$$|E_j - E_B|, |V_{j,j+1}| \ll |E_B - E_{D/A}|$$

$$\begin{aligned} \hat{H} = & E_D |\mathbf{D}\rangle\langle\mathbf{D}| + \sum_{j=1}^N E_j |j\rangle\langle j| + E_A |A\rangle\langle A| \\ & + V_{D1} |\mathbf{D}\rangle\langle 1| + V_{1D} |1\rangle\langle \mathbf{D}| + V_{AN} |A\rangle\langle N| + V_{NA} |N\rangle\langle A| \\ & + \sum_{j=1}^{N-1} (V_{j,j+1} |j\rangle\langle j+1| + V_{j+1,j} |j+1\rangle\langle j|) \end{aligned}$$

$$\tilde{V}_{DA} = \frac{V_{D1} V_{NA}}{V_B} \left( \frac{V_B}{(E_{D/A} - E_B)} \right)^N = V_0 e^{-(1/2)Nb\beta'}$$

# Marcus expressions for non-adiabatic ET rates

$$k_{D \rightarrow A} = \frac{2\pi}{\hbar} |V_{DA}|^2 \mathcal{F}(E_{AD})$$
$$= \frac{2\pi}{\hbar} |V_{D1} V_{NA}|^2 |G_{1N}^{(B)}(E_D)|^2 \mathcal{F}(E_{AD})$$

Donor-to-Bridge/  
Acceptor-to-bridge

Bridge Green's  
Function

$$\mathcal{F}(E) = \frac{e^{-(\lambda+E)^2/4\lambda k_B T}}{\sqrt{4\pi\lambda k_B T}}$$

Franck-Condon-  
weighted DOS

Reorganization energy

# Bridge mediated ET rate

$$k_{ET} \sim \mathcal{F}(E_{AD}, T) \exp(-\beta' R_{DA})$$

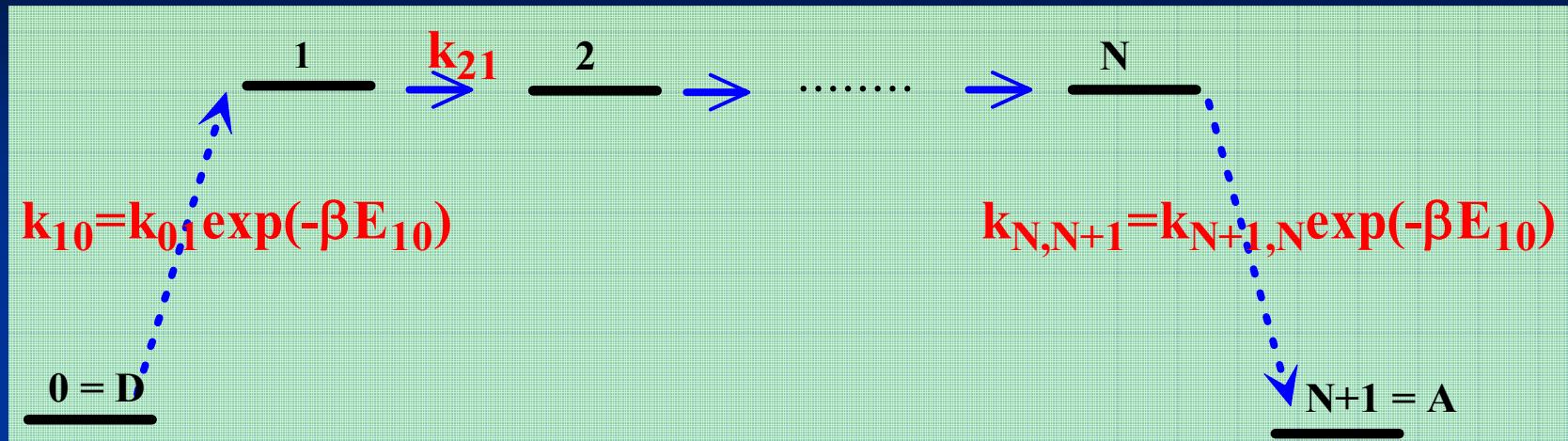
$\beta'$  ( $\text{\AA}^{-1}$ ) =

**0.2-0.6** for highly conjugated chains

**0.9-1.2** for saturated hydrocarbons

**$\sim 2$**  for vacuum

# Incoherent hopping



$$\dot{P}_0 = -k_{1,0}P_0 + k_{0,1}P_1$$

$$\dot{P}_1 = -(k_{0,1} + k_{2,1})P_1 + k_{1,0}P_0 + k_{1,2}P_2$$

⋮

$$\dot{P}_N = -(k_{N-1,N} + k_{N+1,N})P_N + k_{N,N-1}P_{N-1} + k_{N,N+1}P_{N+1}$$

$$\dot{P}_{N+1} = -k_{N,N+1}P_{N+1} + k_{N+1,N}P_N$$

**STEADY STATE  
SOLUTION**

# ET rate from steady state hopping

$$0 = -(k_{0,1} + k_{2,1})P_1 + k_{1,0}P_0 + k_{1,2}P_2$$

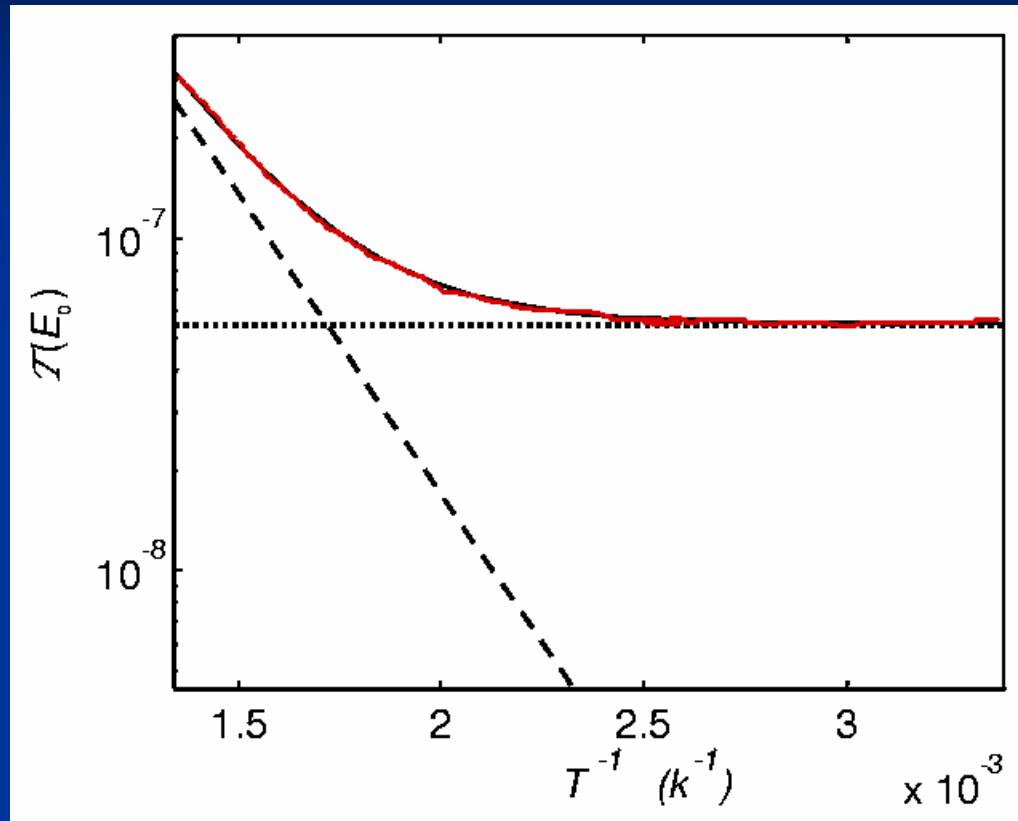
•  
•  
•

$$0 = -(k_{N-1,N} + k_{N+1,N})P_N + k_{N,N-1}P_{N-1}$$

$$\dot{P}_{N+1} = k_{N+1,N}P_N = k_{D \rightarrow A}P_0$$

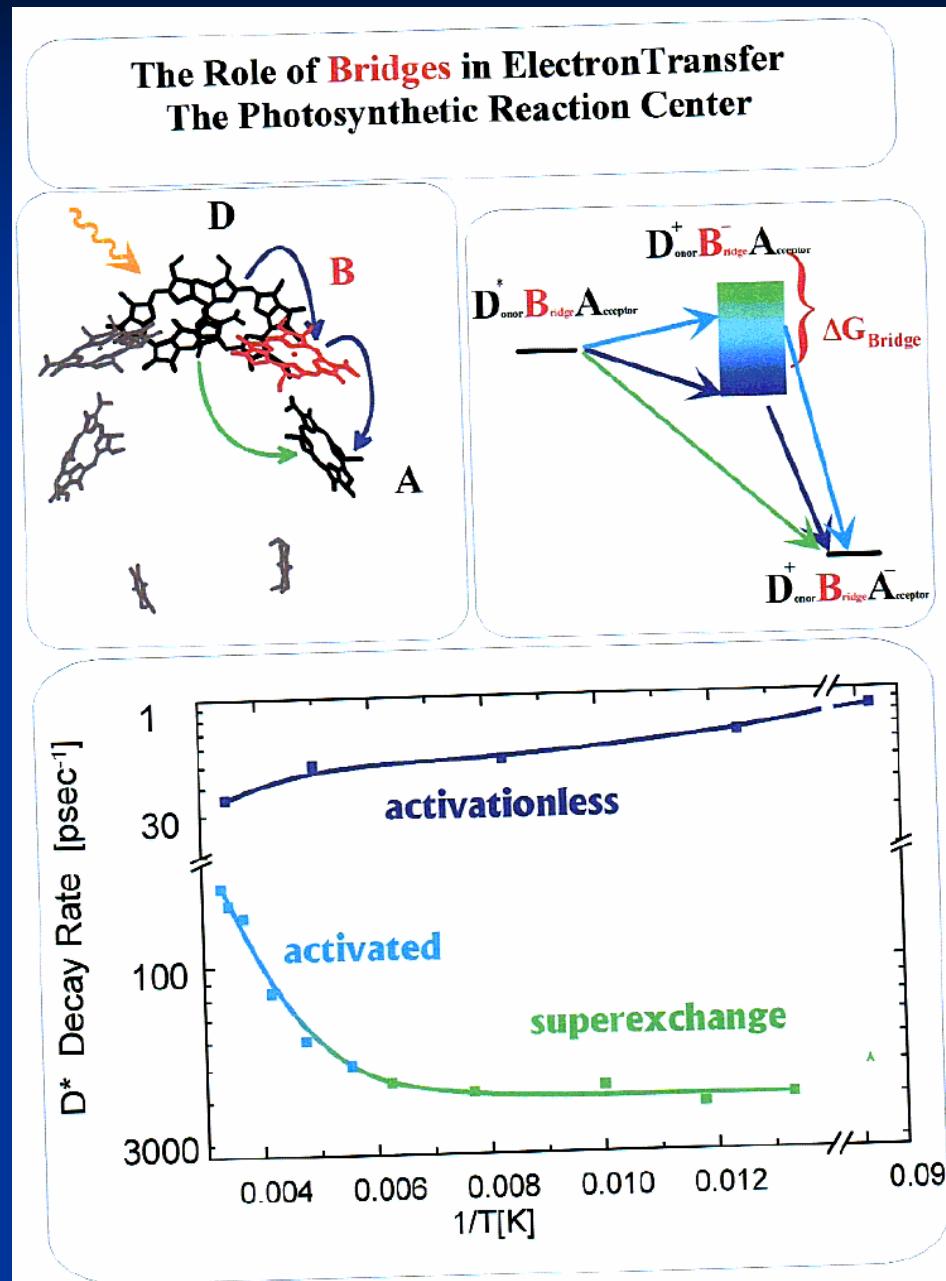
$$k_{D \rightarrow A} \equiv k_{N+1,0} = \frac{k e^{-(E_B/k_B T)}}{\left[ \frac{k}{k_{N \rightarrow A}} + \frac{k}{k_{1 \rightarrow D}} - 1 \right] + N}$$

# Dependence on temperature



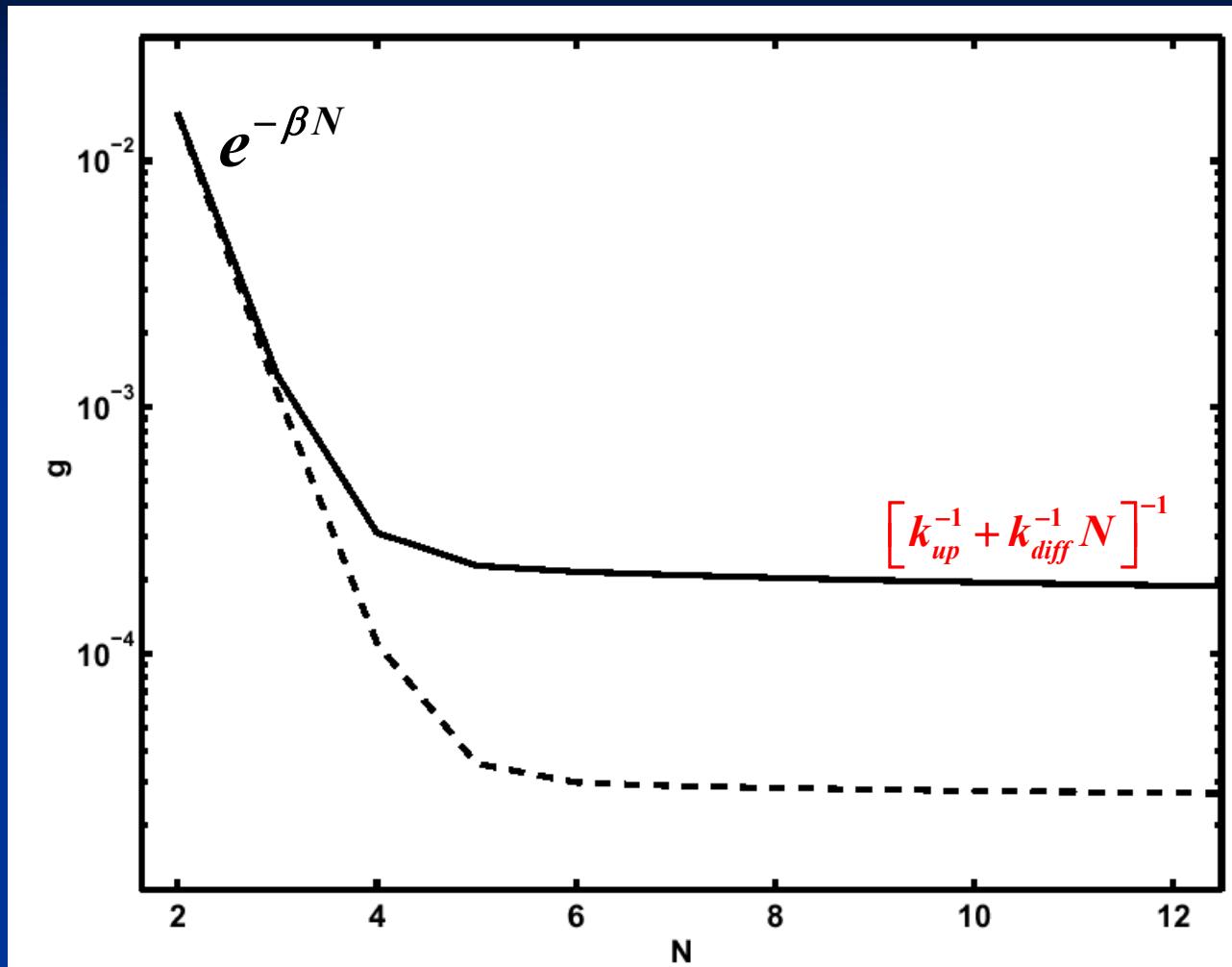
The integrated elastic (dotted line) and activated (dashed line) components of the transmission, and the total transmission probability (full line) displayed as function of inverse temperature. Parameters are as in Fig. 3.

# The photosynthetic reaction center

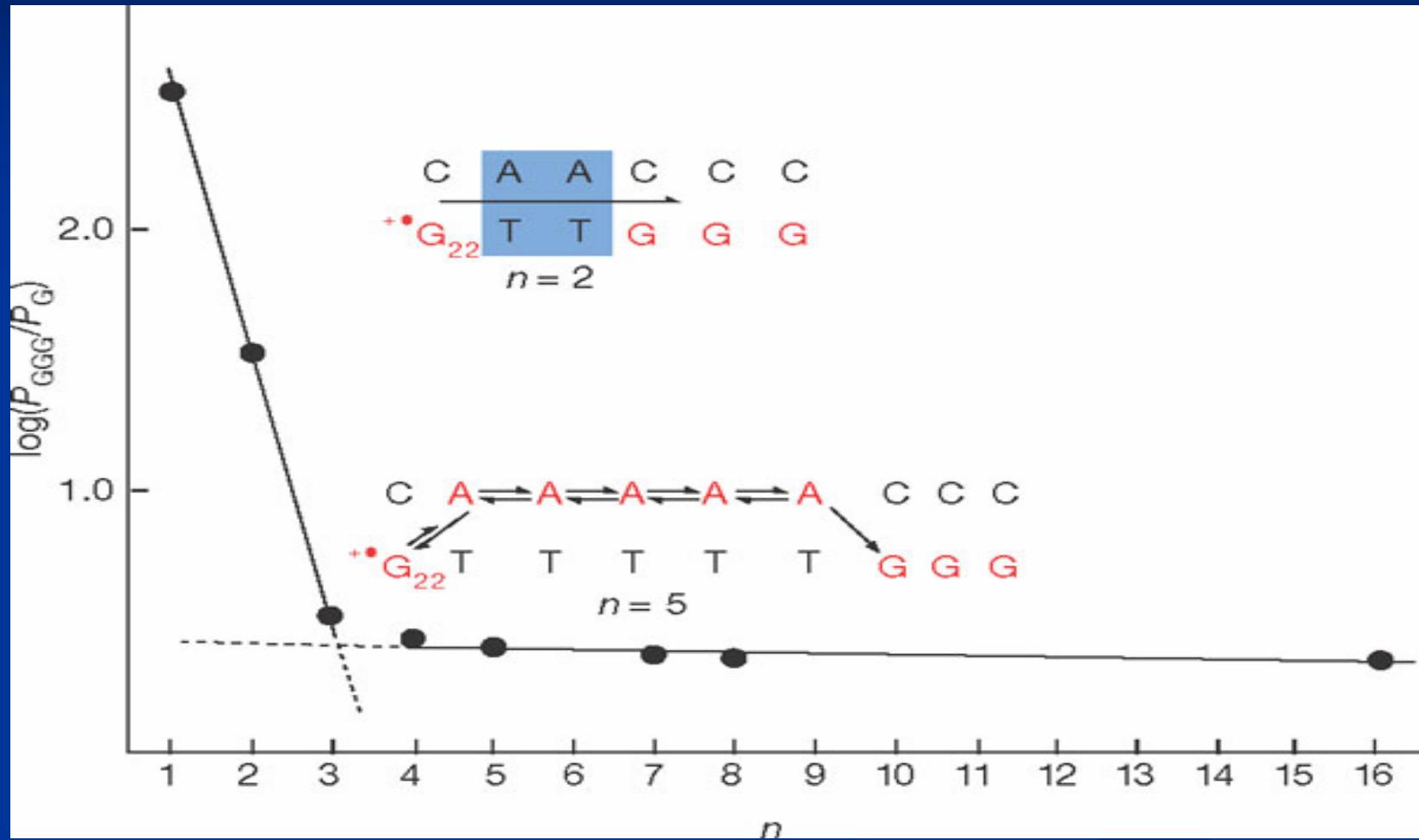


Michel - Beyerle et al

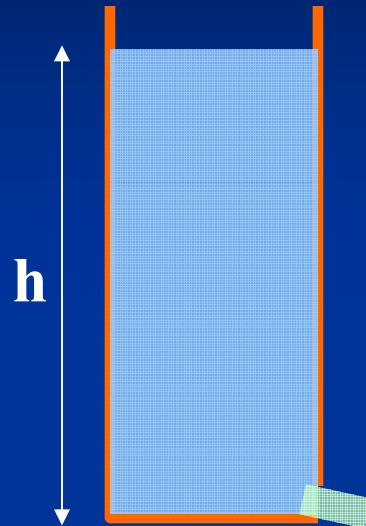
# Dependence on bridge length



# DNA (Giese et al 2001)



# Steady state evaluation of rates

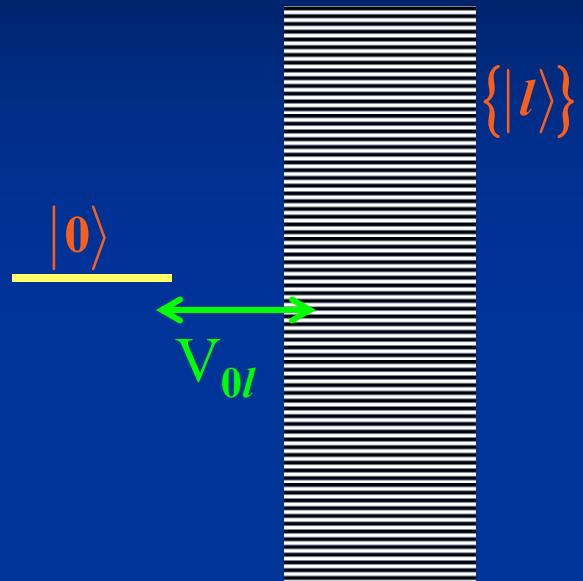


Rate of water flow depends linearly on water height in the cylinder

Two ways to get the rate of water flowing out:

- (1) Measure  $h(t)$  and get the rate coefficient from  $k = (1/h)dh/dt$
- (2) Keep  $h$  constant and measure the steady state outwards water flux  $J$ . Get the rate from  $k = J/h$  -- Steady state rate

# Steady state quantum mechanics



Starting from state 0 at  $t=0$ :

$$P_0 = \exp(-\Gamma_0 t)$$

$$\Gamma_0 = 2\pi|V_{0l}|^2\rho_L \text{ (Golden Rule)}$$

Steady state derivation:

$$\psi(t) = C_0(t)|0\rangle + \sum_l C_l(t)|l\rangle$$

$$\cancel{C_0 \not\propto \frac{d}{dt} C_0 \cancel{\bar{C}_0 = -iE_0 t C_0 - i \sum_l V_{sl} C_l}}$$

$$\hbar \frac{d}{dt} C_l = -iE_l C_l - iV_{l0} C_0 \quad ; \text{ all } l$$

$$C_0 = c_0 e^{-(i/\hbar)E_0 t} \quad ; \quad \begin{aligned} \hbar \frac{d}{dt} C_l &= -i E_l C_l - i V_{l0} C_0 - (1/2) \eta C_l \quad ; \quad \text{all } l \\ &\qquad\qquad\qquad \text{pumping} \qquad\qquad\qquad \text{damping} \end{aligned}$$

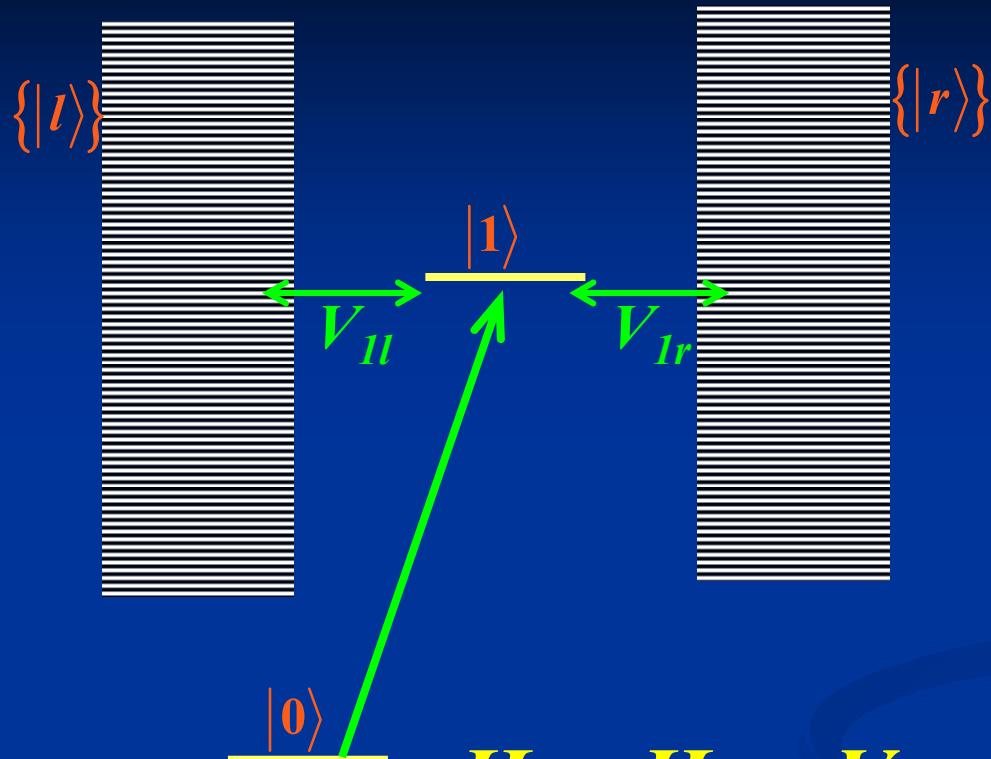
$$C_l(t) = c_l e^{-(i/\hbar)E_0 t} \quad ; \quad c_l = \frac{V_{ls} c_0}{E_0 - E_l + i\eta/2}$$

$$J = (\eta/\hbar) \sum_l |C_l|^2 = |C_0|^2 \sum_l |V_{l0}|^2 \frac{\eta/\hbar}{(E_0 - E_l)^2 + (\eta/2)^2}$$

$$\xrightarrow{\eta \rightarrow 0} |C_0|^2 \frac{2\pi}{\hbar} \sum_l |V_{l0}|^2 \delta(E_0 - E_l)$$

$$k = \frac{J}{|C_0|^2} = \frac{2\pi}{\hbar} \sum_l |V_{l0}|^2 \delta(E_0 - E_l) = \frac{2\pi}{\hbar} \left( |V_{l0}|^2 \rho_L \right)_{E_l=E_0} = \Gamma_0 / \hbar$$

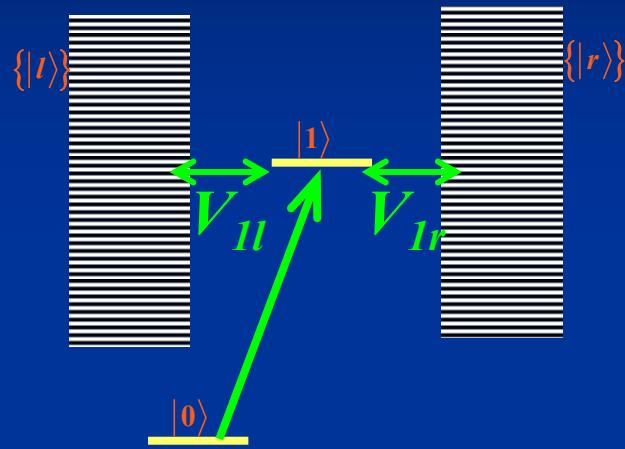
# Resonance scattering



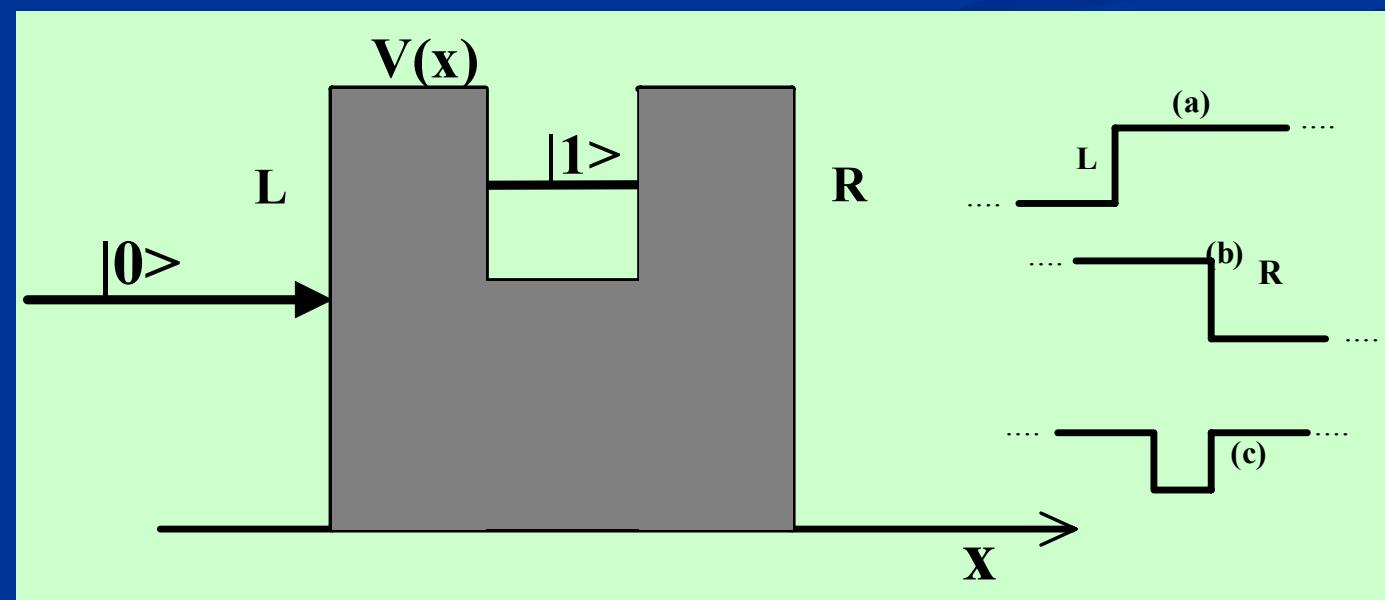
$$H_0 = E_0 |0\rangle\langle 0| + E_1 |1\rangle\langle 1| + \sum_{l \neq 0} E_l |l\rangle\langle l| + \sum_r E_r |r\rangle\langle r|$$

$$V = V_{0,1} |0\rangle\langle 1| + V_{1,0} |1\rangle\langle 0| + \sum_l (V_{l,1} |l\rangle\langle 1| + V_{1,l} |1\rangle\langle l|) + \sum_r (V_{r,1} |r\rangle\langle 1| + V_{1,r} |1\rangle\langle r|)$$

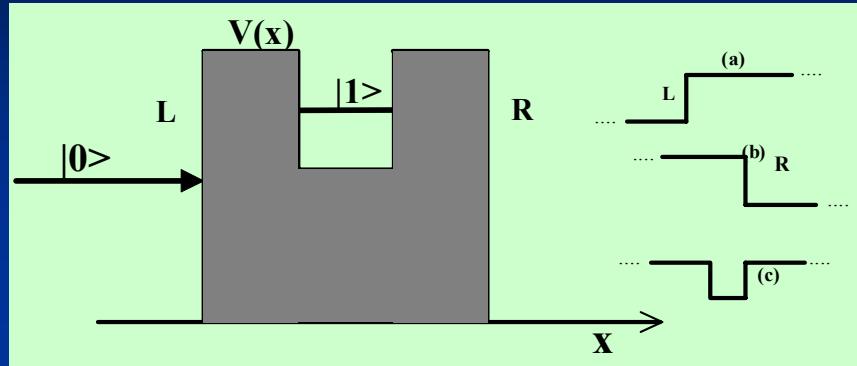
# Resonant tunneling



$$J_{0 \rightarrow R} = \frac{|V_{1,0}|^2}{(E_0 - E_1)^2 + (\Gamma_1/2)^2} \frac{\Gamma_{1R}}{\hbar} |c_0|^2$$



# Resonant Tunneling



$$J_{0 \rightarrow R} = \frac{|V_{1,0}|^2}{(E_0 - E_1)^2 + (\Gamma_1/2)^2} \frac{\Gamma_{1R}}{\hbar} |c_0|^2$$

Transmission Coefficient

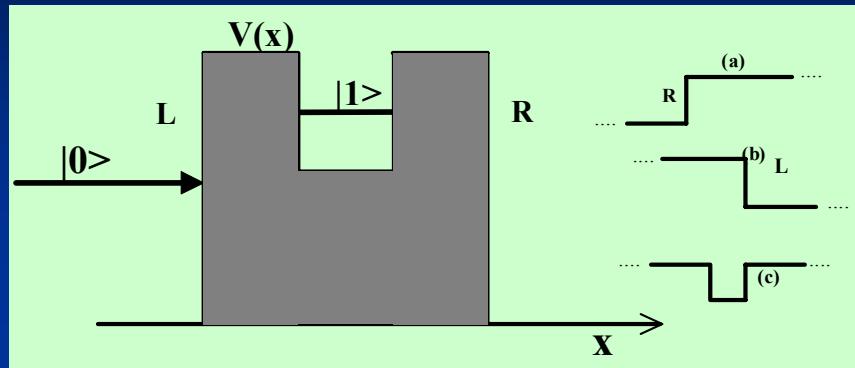
$$J_{0 \rightarrow R} = (\text{incident flux}) \times \mathcal{T}(E_0) = |c_0|^2 \frac{p_0}{mL} \mathcal{T}(E_0)$$

$$(2\pi\hbar\rho_L(E_0))^{-1}$$

$$\mathcal{T}(E_0) = \frac{\Gamma_{1L}(E_0)\Gamma_{1R}(E_0)}{(E_0 - \tilde{E}_1)^2 + (\Gamma_1(E_0)/2)^2}$$

$$\Gamma_1 = \Gamma_{1R} + \Gamma_{1L}$$

# Resonant Transmission – 3d



$$\mathcal{T}(E_0) = \frac{\Gamma_{1L}(E_0)\Gamma_{1R}(E_0)}{(E_0 - \tilde{E}_1)^2 + (\Gamma_1(E_0)/2)^2}$$

$$\Gamma_1 = \Gamma_{1R} + \Gamma_{1L}$$

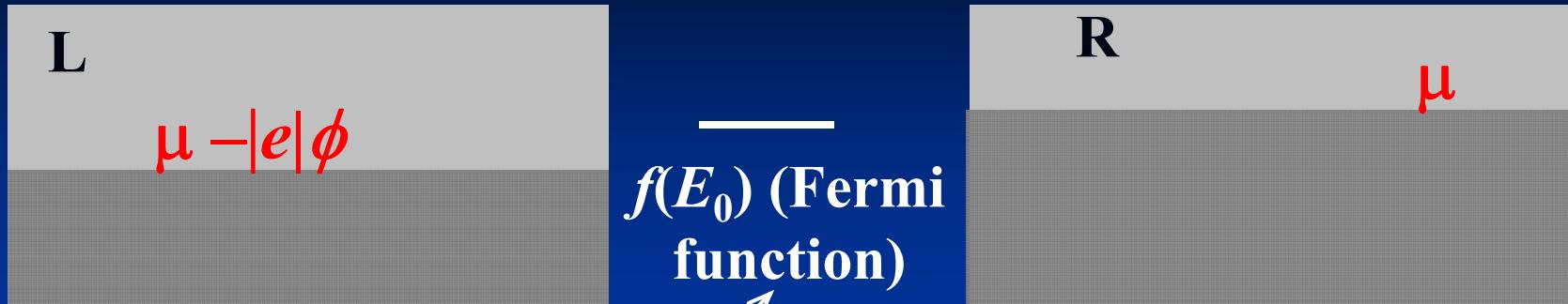
1d

3d: Total flux from L to R at energy  $E_0$ :

$$\left( \frac{dJ_{L \rightarrow R}(E)}{dE} \right)_{E=E_0} = \frac{1}{(2\pi\hbar)} \frac{\Gamma_{1L}(E_0)\Gamma_{1R}(E_0)}{(E_0 - \tilde{E}_1)^2 + (\Gamma_1(E_0)/2)^2} |c_0|^2$$

If the continua are associated with a metal electrode at thermal equilibrium than  $|c_0|^2 = f(E_0) = \left[ \exp((E_0 - \mu)/k_B T) + 1 \right]^{-1}$   
 (Fermi-Dirac distribution)

# CONDUCTION



$$\left( \frac{dJ_{L \rightarrow R}(E)}{dE} \right)_{E=E_0} = \frac{1}{(2\pi\hbar)} \mathcal{T}(E_0) |c_0|^2$$

$$\mathcal{T}(E) = \frac{\Gamma_{1L}(E)\Gamma_{1R}(E)}{(E - \tilde{E}_1)^2 + (\Gamma_1(E)/2)^2}$$

$$I = \frac{|e|}{2\pi\hbar} \int_{-\infty}^{\infty} dE (f_L(E) - f_R(E)) \mathcal{T}(E)$$

$$f(E + |e| \phi) - f(E) = |e| \phi \delta(E - \mu)$$

$$I = \frac{e^2}{2\pi\hbar} \mathcal{T}(E = \mu) \times \phi \xrightarrow{\text{2 spin states}} I = \frac{e^2}{\pi\hbar} \mathcal{T}(E = \mu) \times \phi$$

## Zero bias conduction $g(\phi = 0)$

# Landauer formula

$$g(\phi = 0) = \frac{e^2}{\pi \hbar} \mathcal{T}(E = \mu) ; \quad \mu - \text{Fermi energy}$$

$$I = \frac{|e|}{\pi \hbar} \int_{-\infty}^{\infty} dE (f_L(E) - f_R(E)) \mathcal{T}(E)$$

$$g(\phi) = \frac{dI}{d\phi}$$

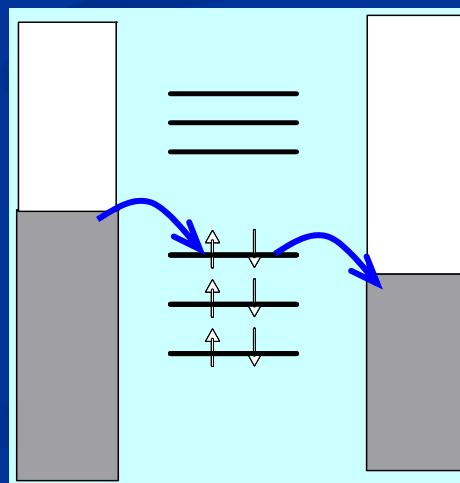
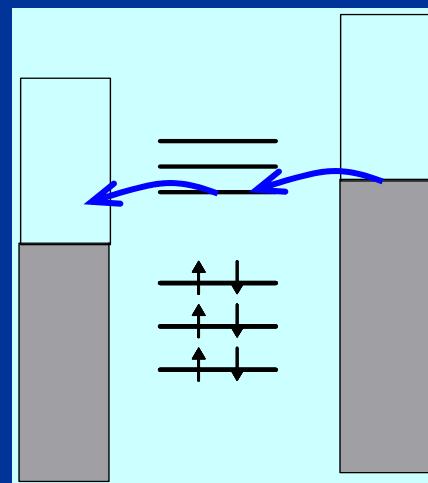
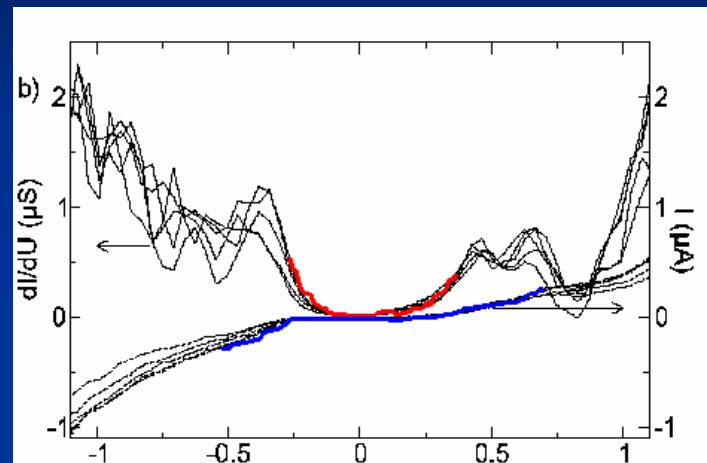
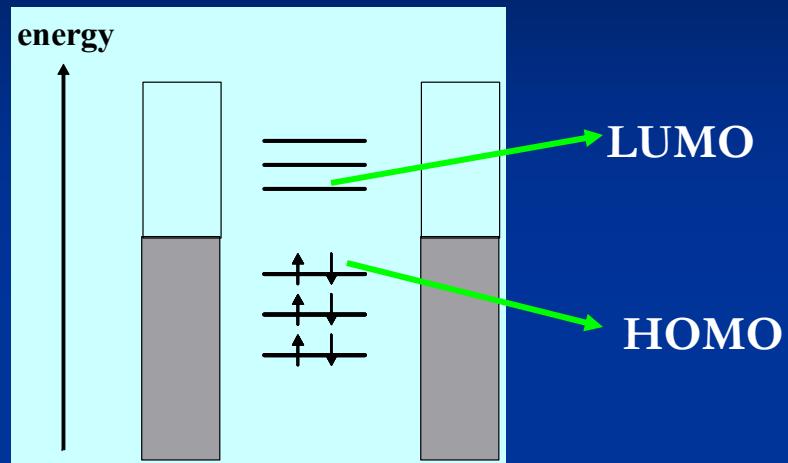
For a single “channel”:

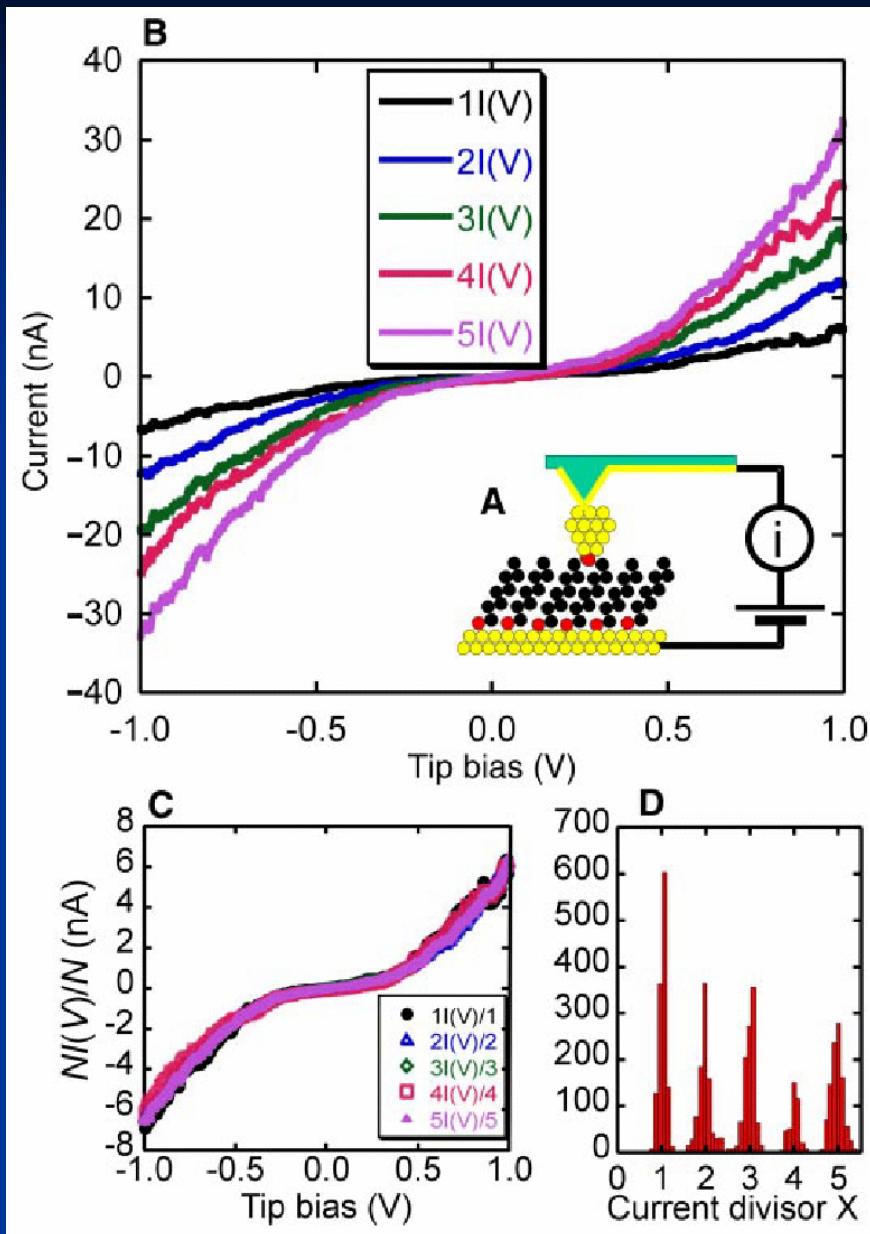
$$\mathcal{T}(E) = \frac{\Gamma_{1L}(E)\Gamma_{1R}(E)}{(E - \tilde{E}_1)^2 + (\Gamma_1(E)/2)^2} \quad (\text{maximum}=1)$$

Maximum conductance per channel

$$g = \frac{e^2}{\pi \hbar} = (12.9 K\Omega)^{-1}$$

# Molecular level structure between electrodes





Cui et al (Lindsay),  
Science 294, 571 (2001)

“The resistance of a single octanedithiol molecule was  $900 \pm 50$  megaohms, based on measurements on more than 1000 single molecules. In contrast, nonbonded contacts to octanethiol monolayers were at least four orders of magnitude more resistive, less reproducible, and had a different voltage dependence, demonstrating that the measurement of intrinsic molecular properties requires chemically bonded contacts”.

# General case

$$I = \frac{|e|}{\pi \hbar} \int_{-\infty}^{\infty} dE (f_L(E) - f_R(E)) \mathcal{T}(E)$$

$$\mathcal{T}_{\mathcal{T}(E)} = \text{Tr}_B \left[ \hat{\Gamma}_{1L}(E) \hat{G}^{(B)\dagger}(E) \hat{\Gamma}_{1L}(E) \hat{G}^{(R)}(E) \right]$$

$\frac{(E - E_1)^2 + (\Gamma_1(E)/2)^2}{|E - E_1 - (1/2)i\Gamma|^2}$

$$G^{(B)}(E) = \left( E \Gamma^{(B)} - \hat{H}^{(B)} \right)^{-1}$$

Unit matrix in  
the bridge space

$$H_{n,n'}^{(B)} = H_{n,n'} + \boxed{B_{n,n'}}$$

Bridge Hamiltonian

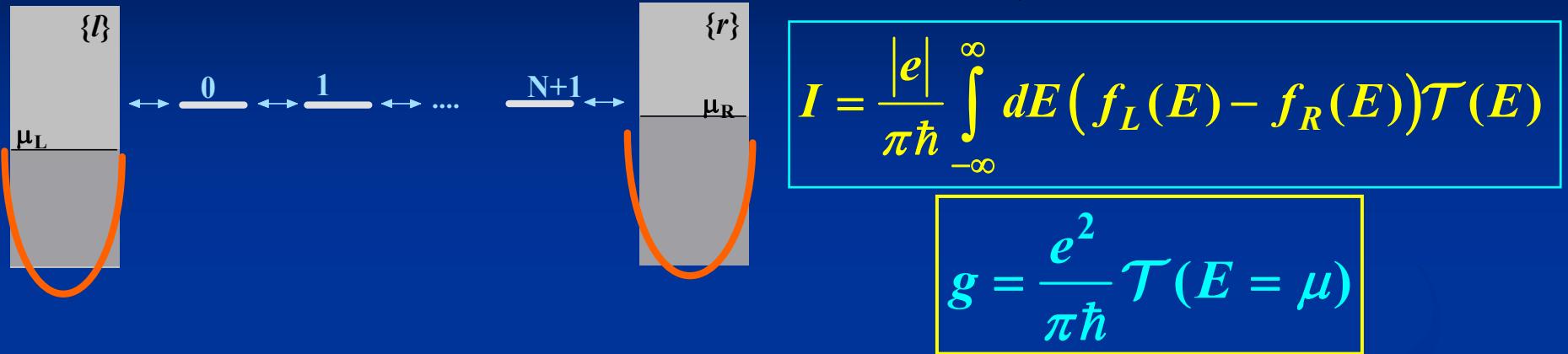
$$B^{(R)}(E) = -(1/2)i\Gamma^{(R)}$$

$$\Gamma_{n,n'}^{(R)} = 2\pi H_{n,R} H_{R,n'} \rho_R$$

$B^{(R)} + B^{(L)} -$  Self energy

Wide band approximation

# The N-level bridge (n.n. interactions)



$$\mathcal{T}(E) = |G_{0,N+1}(E)|^2 \Gamma_0^{(L)}(E) \Gamma_{N+1}^{(R)}(E)$$

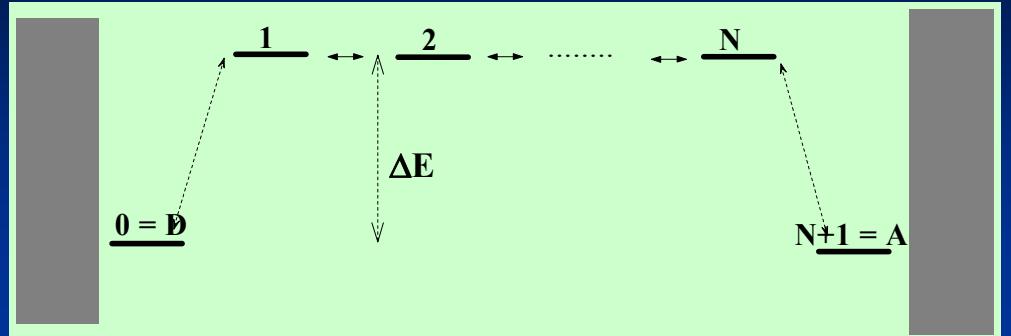
$$\left(\hat{G}_B(E)\right)_{0,N+1} = \frac{1}{(E - E_0)} V_0 \cdot \frac{1}{(E - E_1)} V_{12} \cdots \frac{1}{(E - E_N)} V_{N,N+1} \frac{1}{(E - E_{N+1})}$$

$G_{1N}(E)$

$$\left( E - E_0 + \frac{1}{2} i \Gamma_{0L} \right)$$

$$\left( E - E_{N+1} + \frac{1}{2} i \Gamma_{N+1,R} \right)$$

# ET vs Conduction



$$g = \frac{e^2}{\pi \hbar} |G_{0,N+1}(E)|^2 \Gamma_0^{(L)}(E) \Gamma_{N+1}^{(R)}(E)$$

$$= \frac{e^2}{\pi \hbar} \left| \frac{V_{01} V_{N,N+1}}{\left( E - E_B + \frac{1}{2} i \Gamma_0^{(L)} \right) \left( E - E_A + \frac{1}{2} i \Gamma_{N+1}^{(R)} \right)} \right|^2 |G_{1N}^{(B)}(E)|^2 \Gamma_0^{(L)}(E) \Gamma_{N+1}^{(R)}(E)$$

$$k_{D \rightarrow A} = \frac{2\pi}{\hbar} |V_{DA}|^2 \mathcal{F}(E_{AD})$$

$$= \frac{2\pi}{\hbar} |V_{01} V_{N,N+1}|^2 |G_{1N}^{(B)}(E_D)|^2 \mathcal{F}(E_{AD})$$

# A relation between g and k

$$g \approx \frac{8 e^2}{\pi^2 \Gamma_D^{(L)} \Gamma_A^{(R)} \mathcal{F}} k_{D \rightarrow A}$$

Diagram illustrating the components of the equation:

- Electron charge**: Represented by a yellow box at the top with a downward arrow pointing to the equation.
- conduction**: Represented by a red label with an upward arrow pointing to the term  $\Gamma_D^{(L)}$ .
- Decay into electrodes**: Represented by a yellow box with two upward arrows pointing to the terms  $\Gamma_D^{(L)}$  and  $\Gamma_A^{(R)}$ .
- Marcus**: Represented by a yellow box with an upward arrow pointing to the term  $\mathcal{F}$ .
- Electron transfer rate**: Represented by a red label with an upward arrow pointing to the term  $k_{D \rightarrow A}$ .

# A relation between g and k

$$g \approx \frac{8e^2}{\pi^2 \Gamma_D^{(L)} \Gamma_A^{(R)} \mathcal{F}} k_{D \rightarrow A}$$

$$\mathcal{F} = \left( \sqrt{4\pi\lambda k_B T} \right)^{-1} \exp(-\lambda / 4k_B T)$$

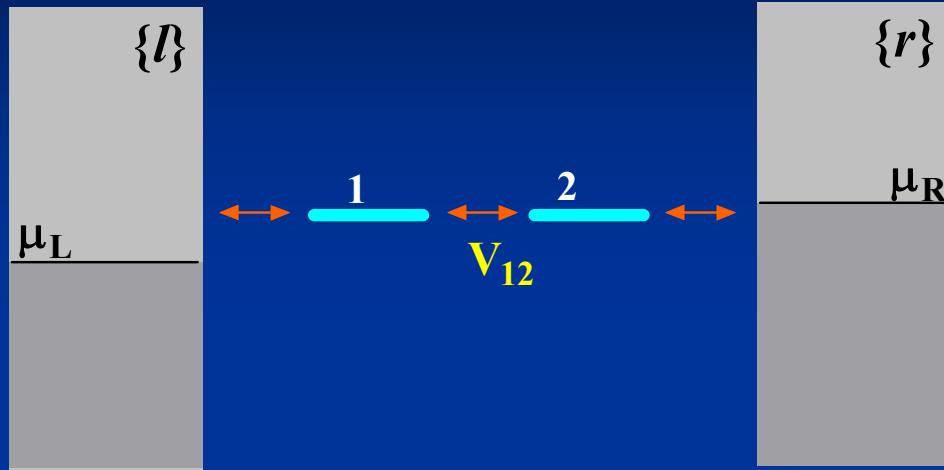
$$\lambda \approx 0.5 \text{ eV} \quad \Gamma_D^{(L)} = \Gamma_A^{(R)} \approx 0.5 eV$$

$$\begin{aligned} g &\sim \left( e^2 / \pi \hbar \right) \left( 10^{-13} k_{D \rightarrow A} (s^{-1}) \right) \\ &\cong \left[ 10^{-17} k_{D \rightarrow A} (s^{-1}) \right] \Omega^{-1} \end{aligned}$$

# Comparing conduction to rates (M. Newton, 2003)

alkane bridge <sup>a</sup> $(X(CH_2)_{n-2})$	$g(\Omega^{1-})$	$5 \times 10^{-19} k_t / \text{DOS}$ (eq 2.23)
$n = 8$	$(10.3 \pm 0.5) \times 10^{-10}$	$2 \times 10^{-8}$
$n = 10$	$(3.5 \pm 0.2) \times 10^{-10}$	$(2 \pm 1) \times 10^{-9}$
$n = 12$	$(1.2 \pm 0.1) \times 10^{-10}$	$(2 \pm 1) \times 10^{-10}$

# 2-level bridge (local representation)

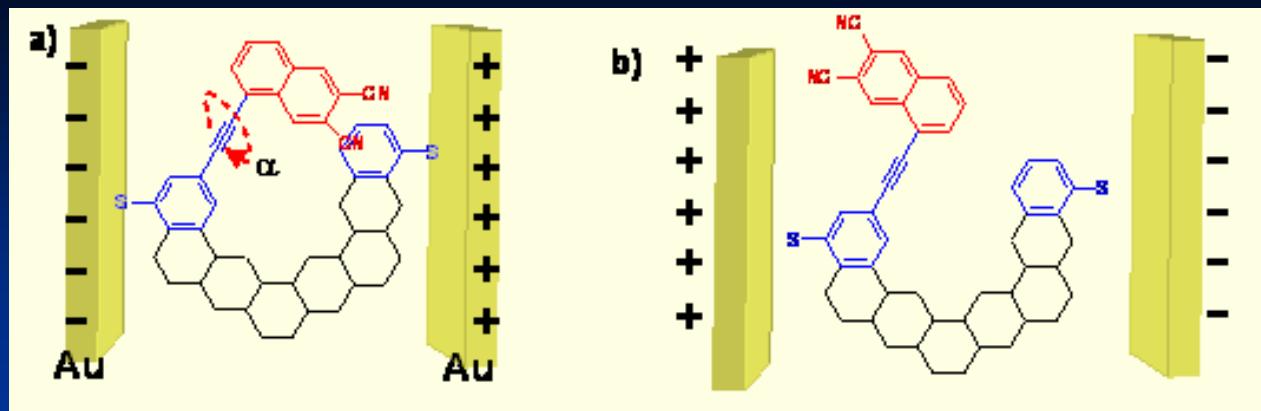


$$g(E) = \frac{\frac{e^2}{\pi \hbar} \Gamma_1^{(L)}(E) \Gamma_2^{(R)}(E) |V_{1,2}|^2}{\left( E - (\tilde{E}_1 + (1/2)i\Gamma_1^{(L)}(E)) \right) \left( E - (\tilde{E}_2 + (1/2)i\Gamma_2^{(R)}(E)) - |V_{1,2}|^2 \right)}$$

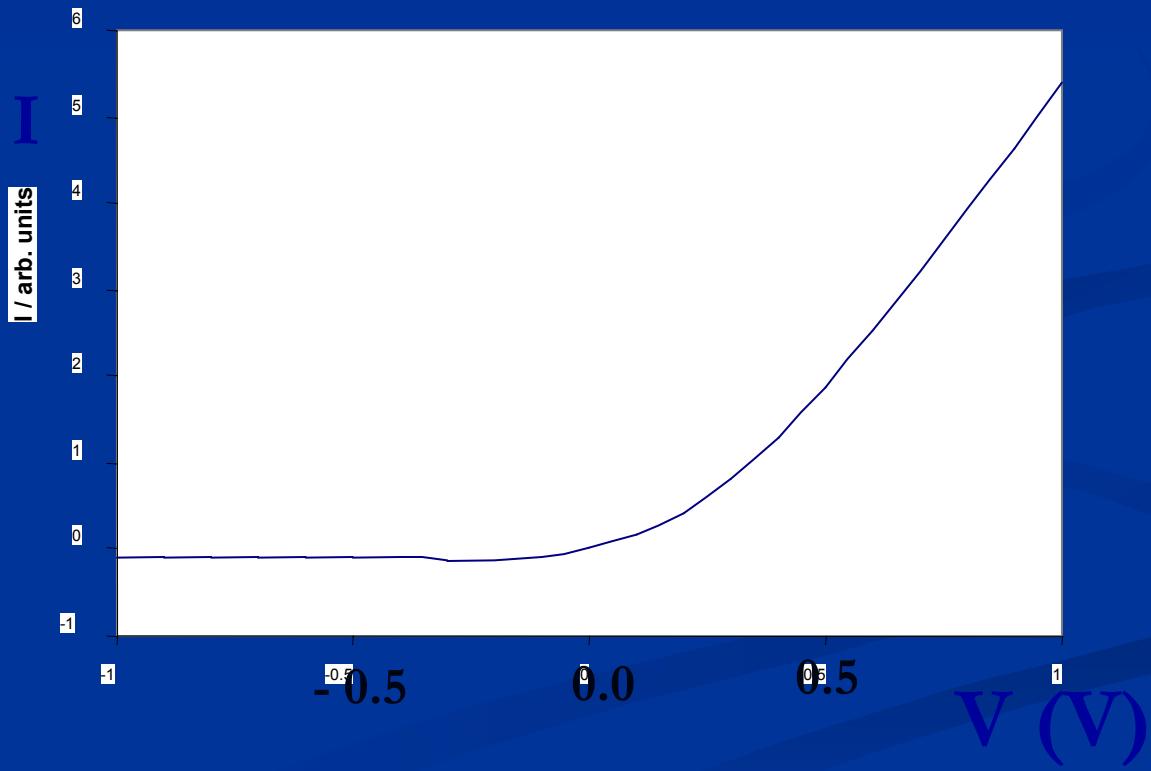
- Dependence on:

- Molecule-electrode coupling  $\Gamma_L, \Gamma_R$
- Molecular energetics  $E_1, E_2$
- Intramolecular coupling  $V_{1,2}$

e-e coupling  
Spin



Ratner and  
Troisi, 2004



# “Switching”

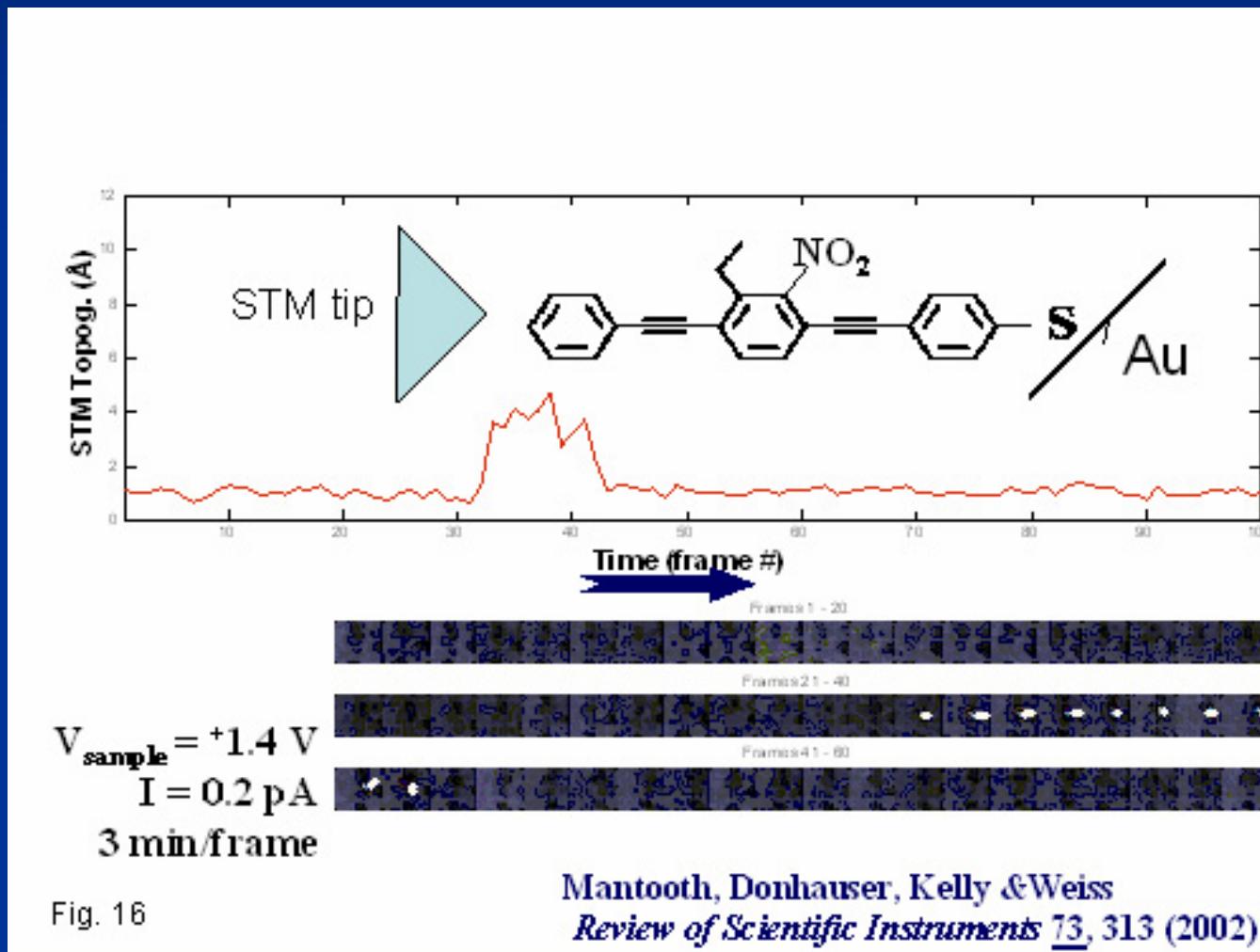
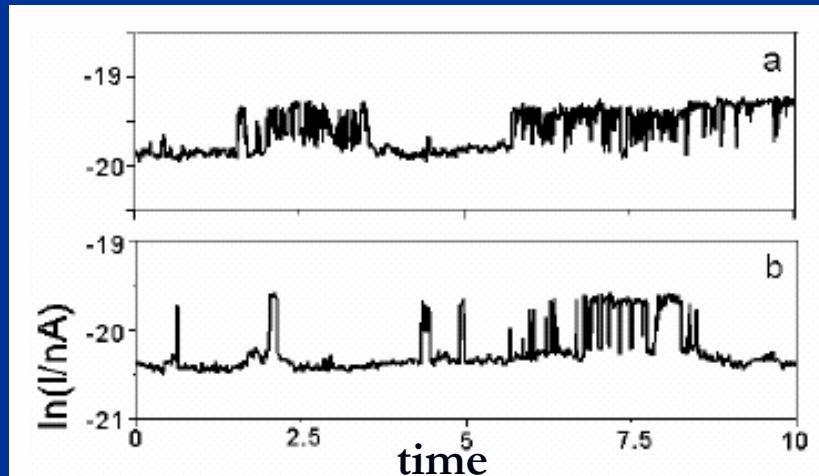


Fig. 16

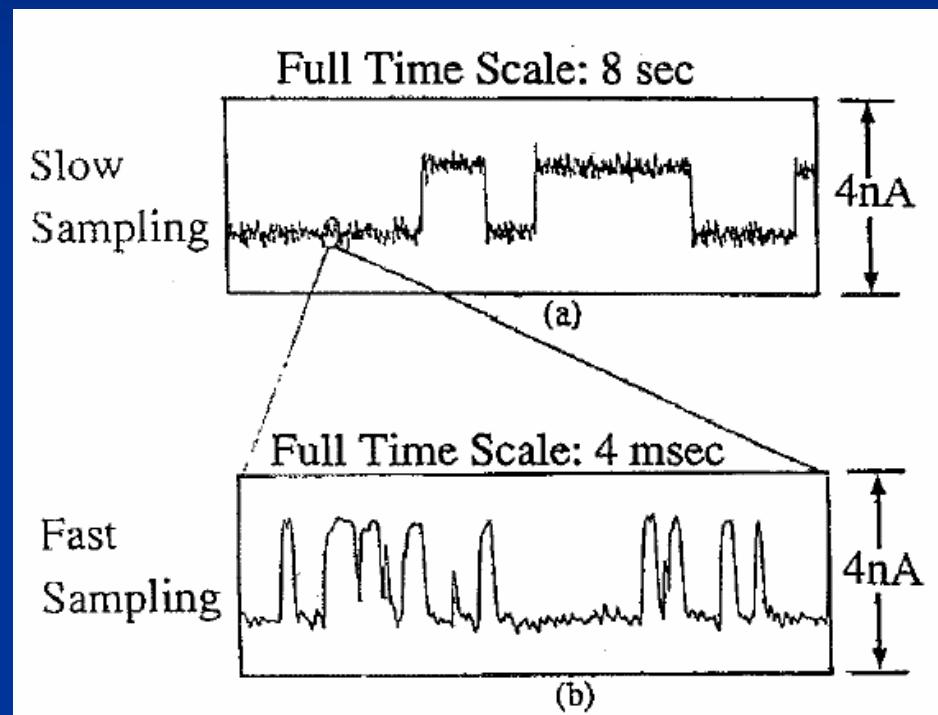
# Reasons for switching

- Conformational changes

- Transient charging

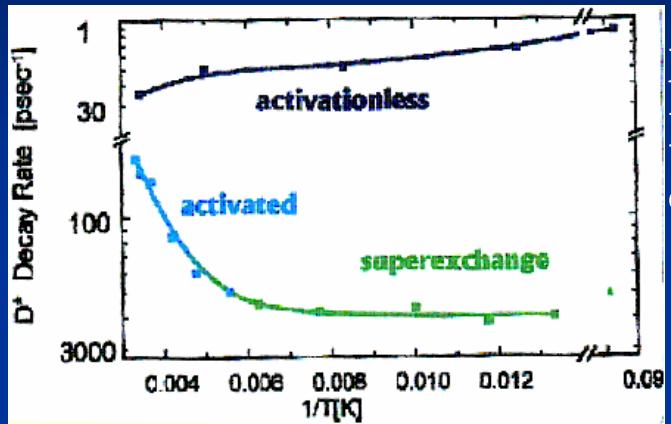


STM under water  
S.Boussaad et. al. JCP (2003)

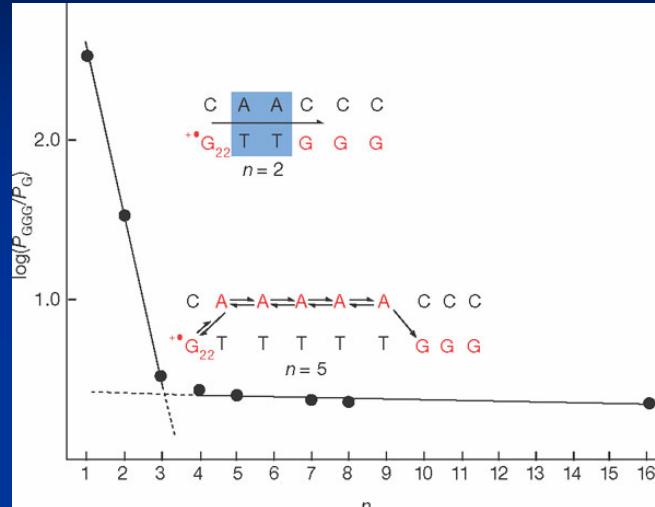


Tsai et. al. PRL 1992: RTS in  
Me-SiO<sub>2</sub>-Si junctions

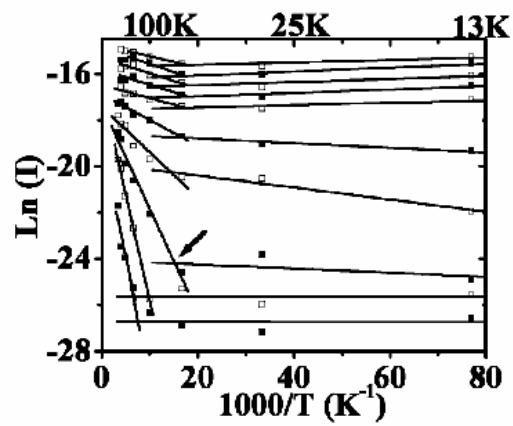
# Temperature and chain length dependence



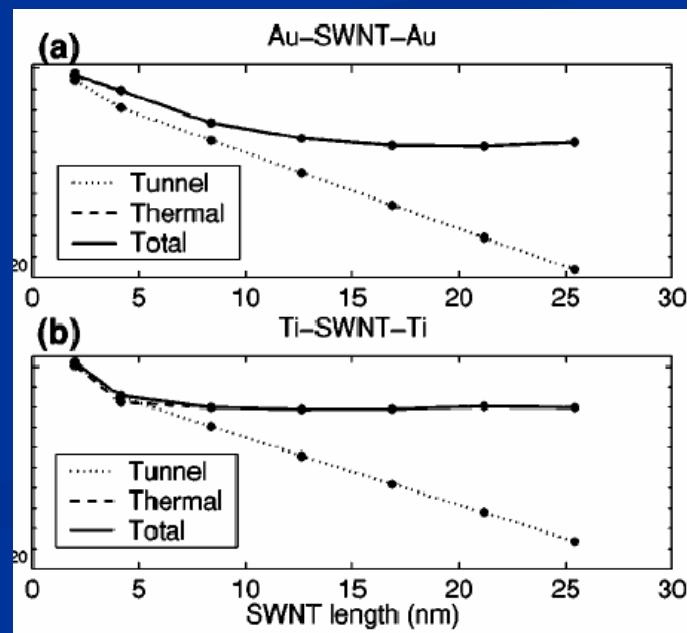
Michel-Beyerle et al



Giese et al, 2002



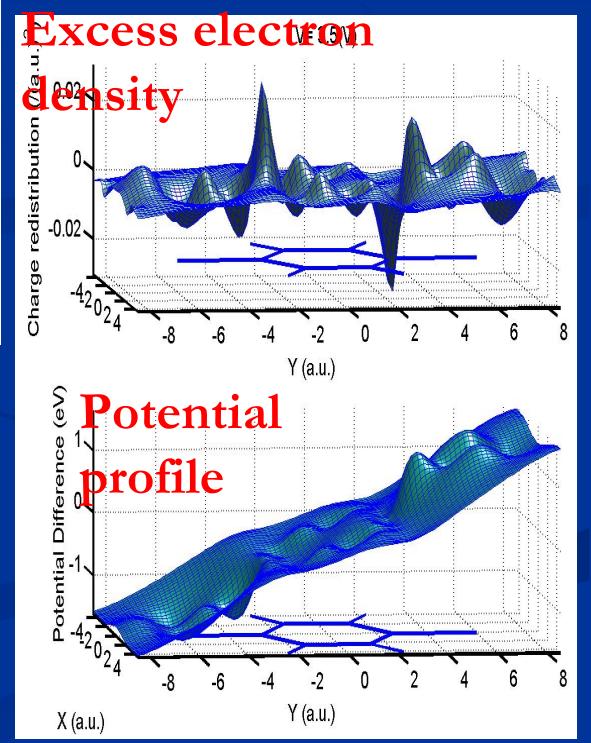
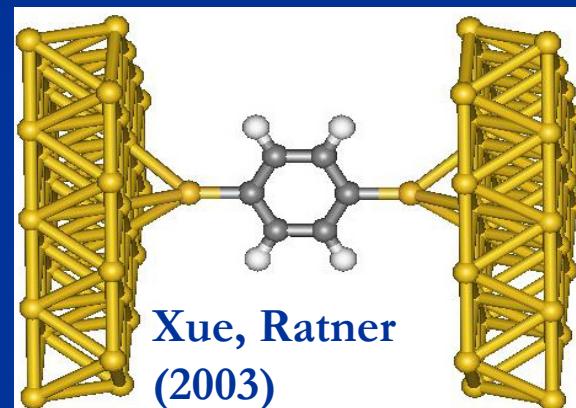
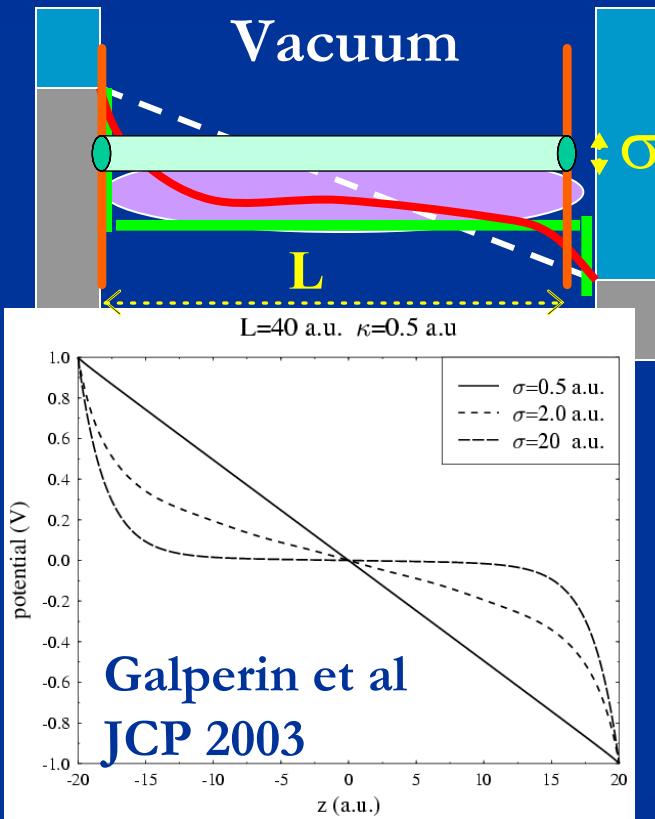
Selzer et al 2004



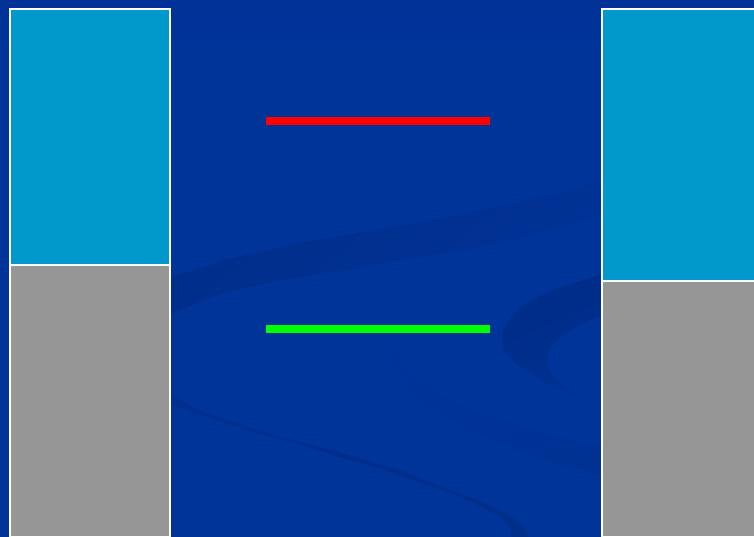
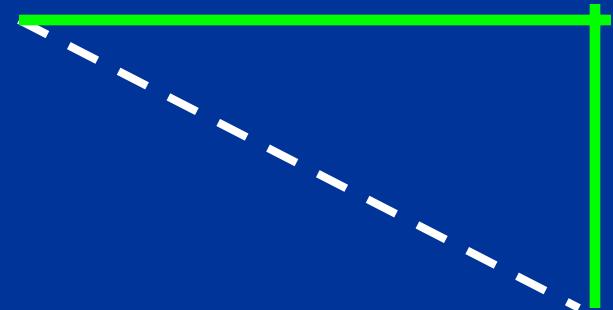
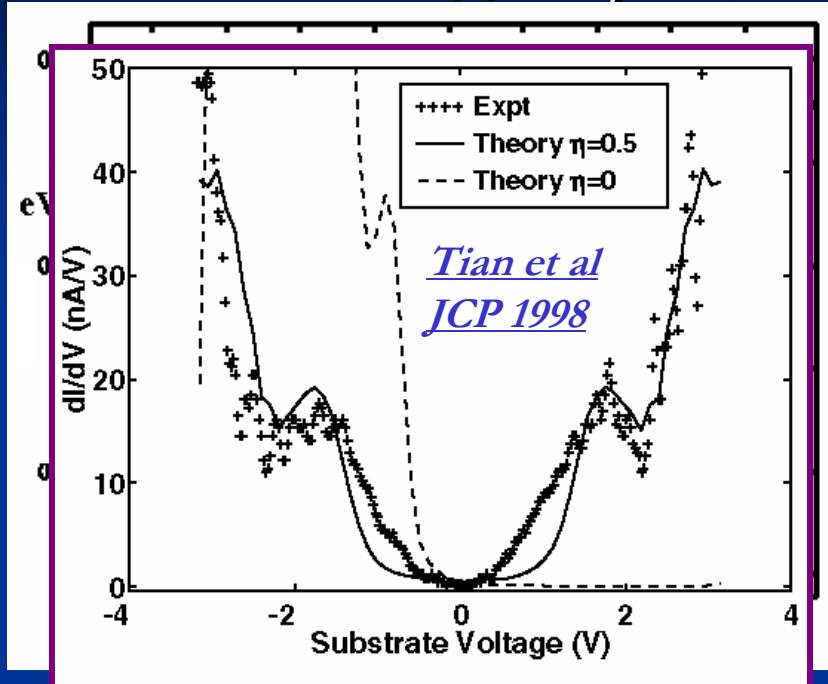
Xue and Ratner 2003

# Where does the potential bias falls, and how?

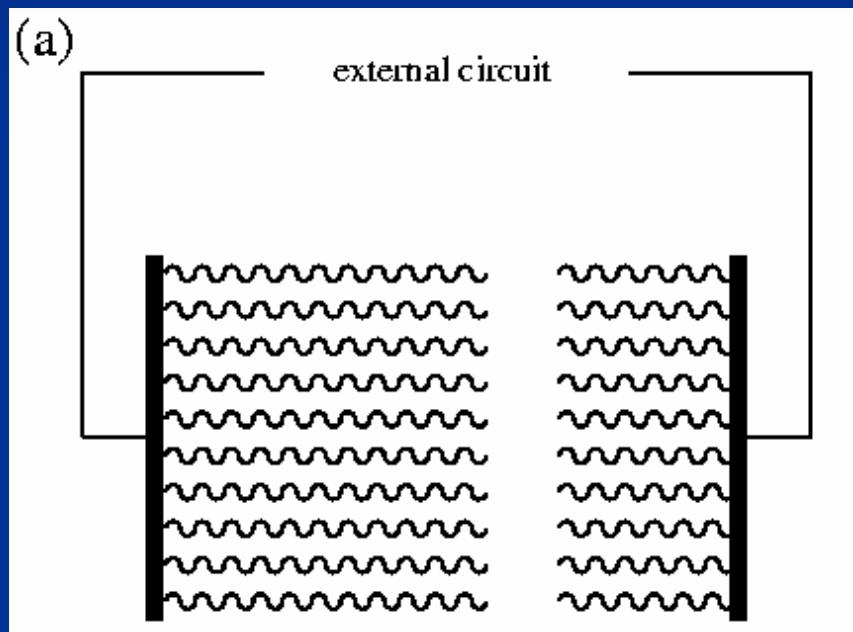
- Image effect
- Electron-electron interaction (on the Hartree level)



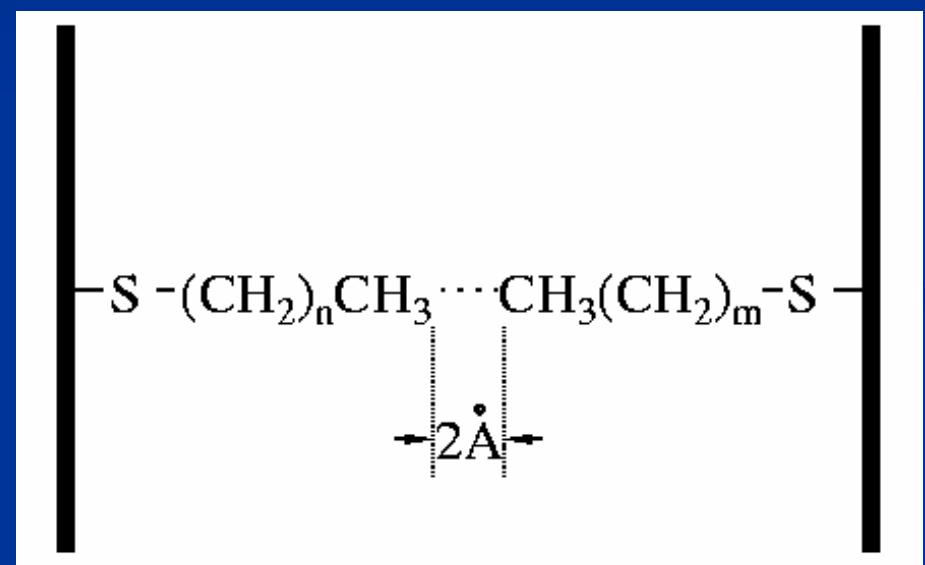
# Why is it important?



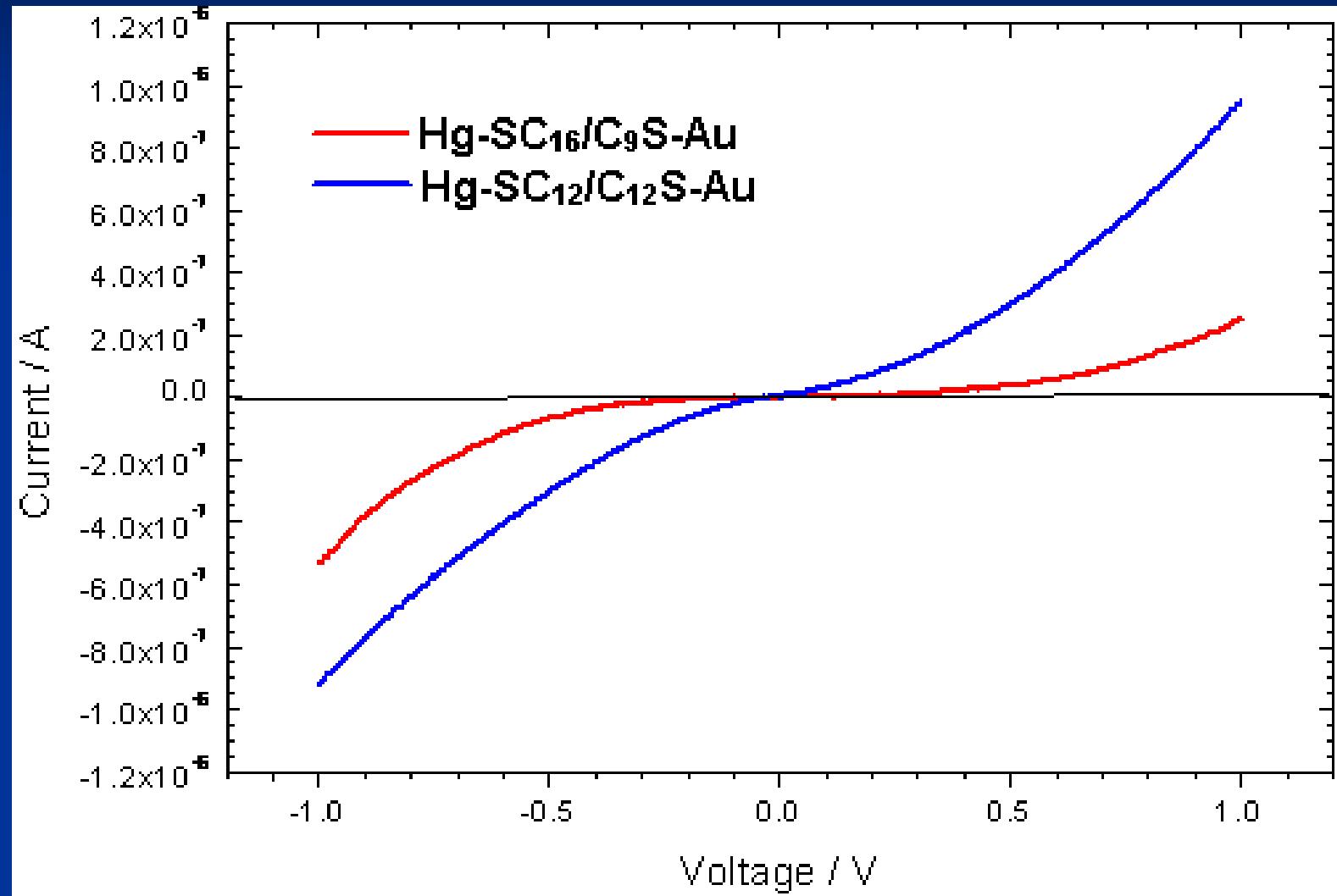
# Experiment



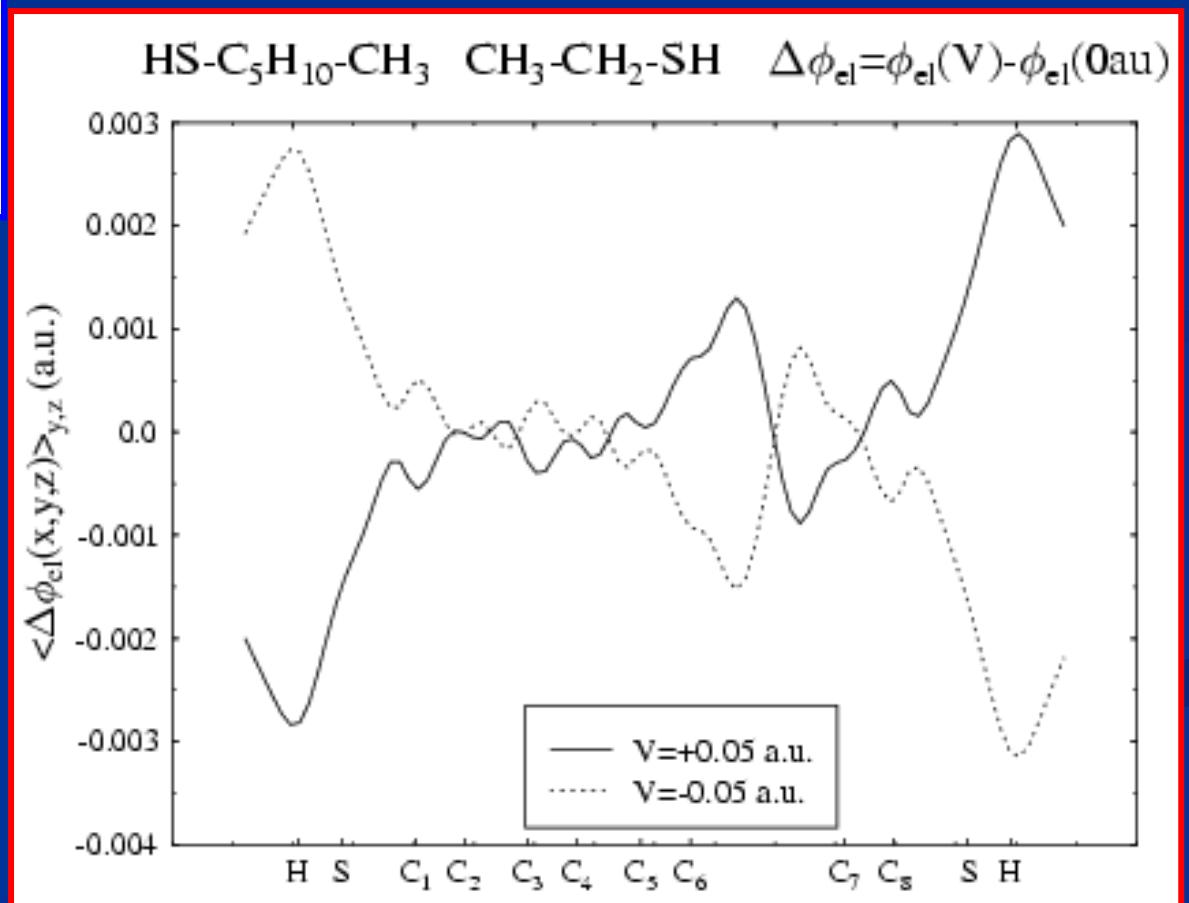
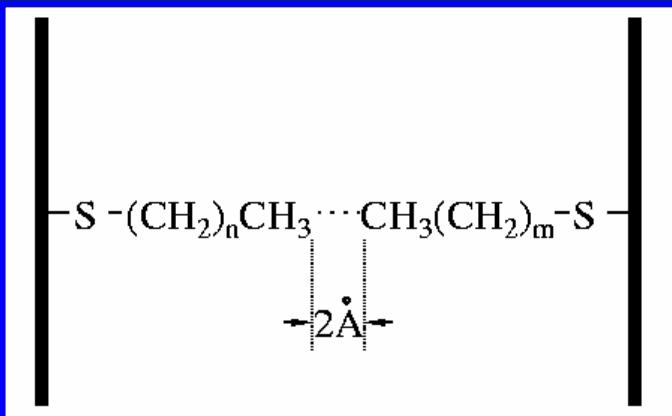
# Theoretical Model



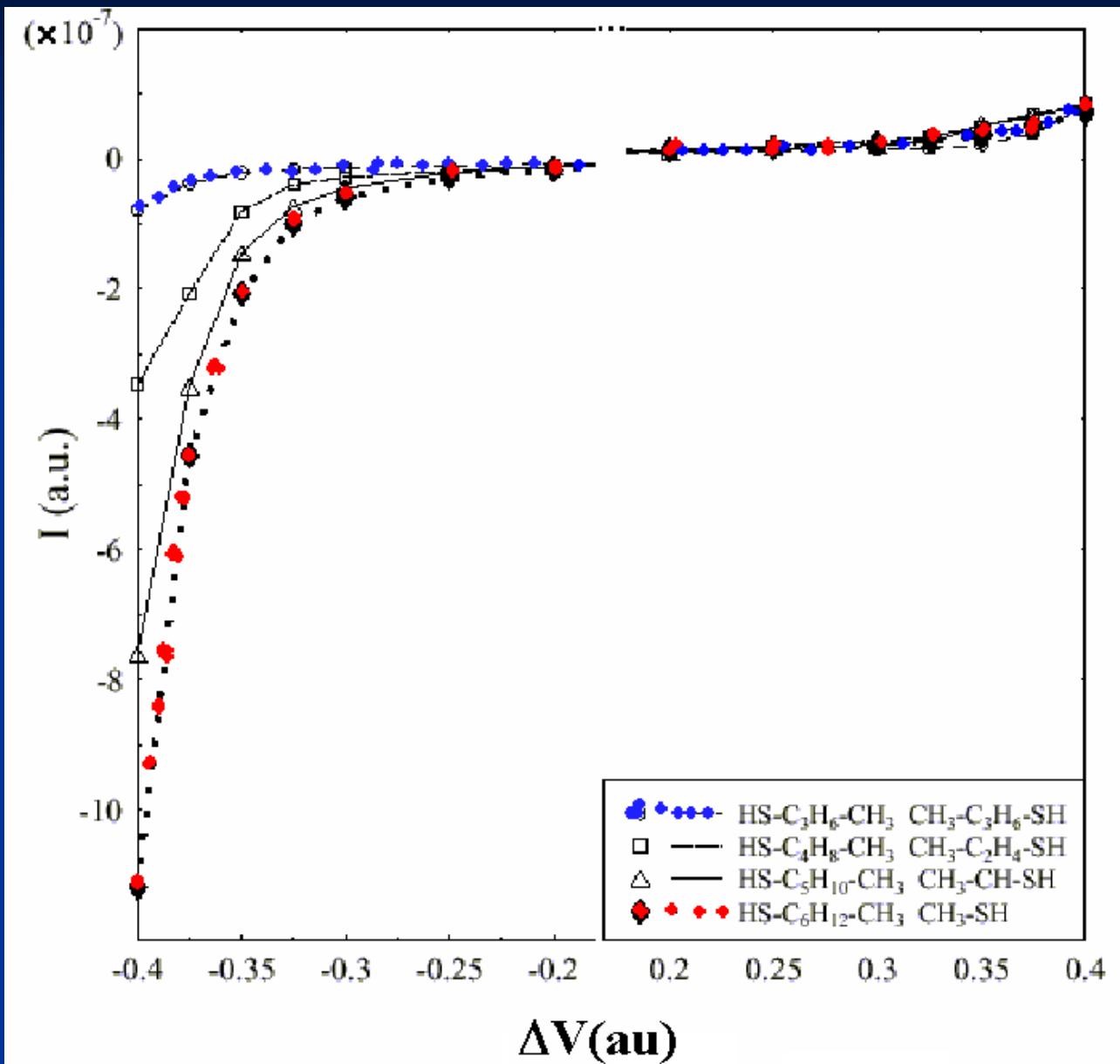
# Experimental i/V behavior

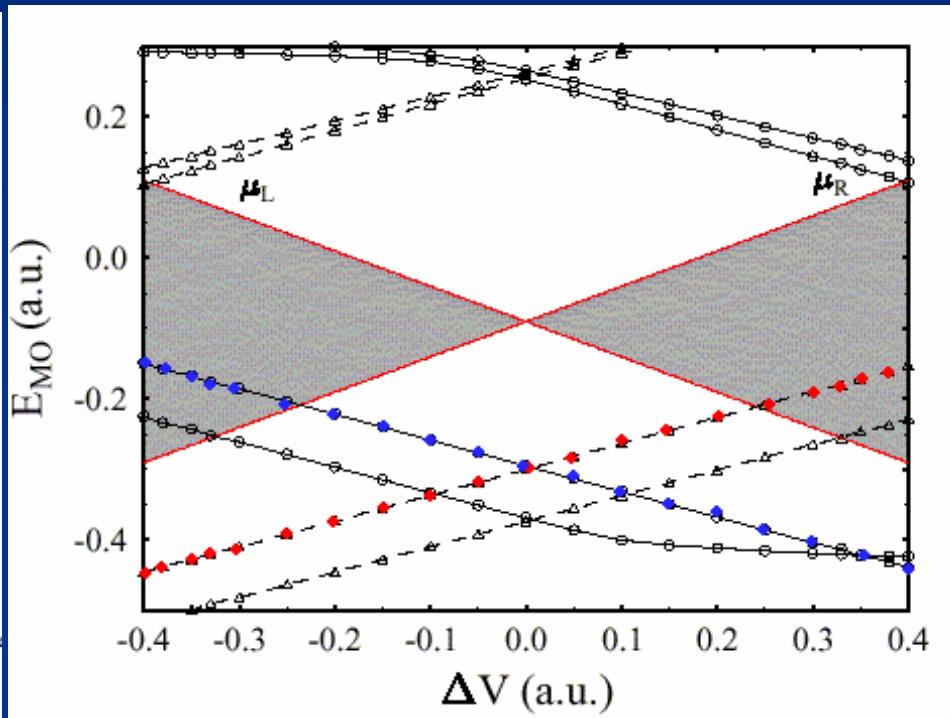
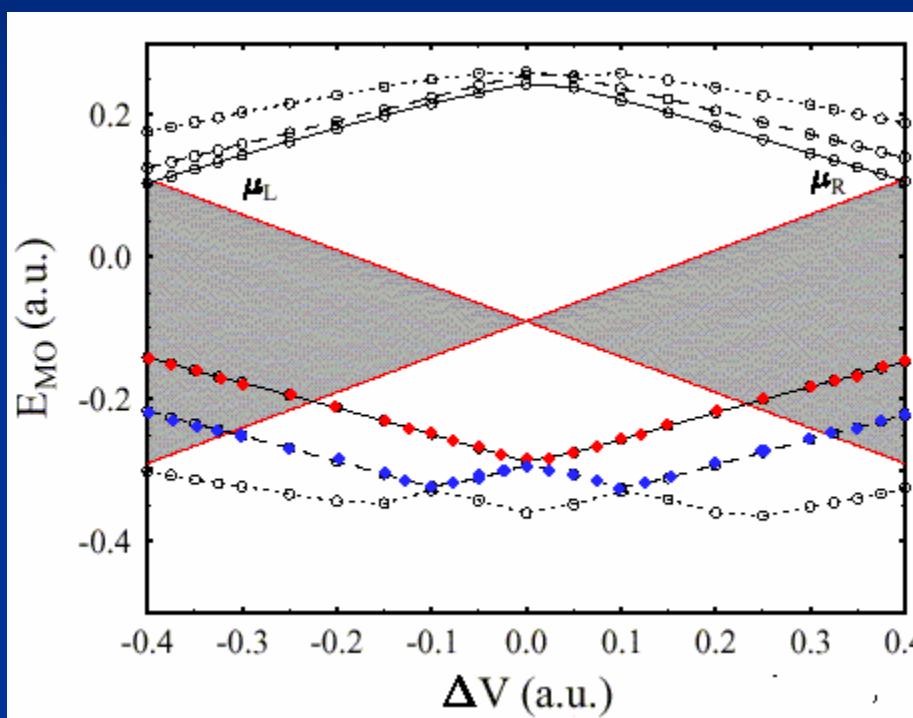


# Potential distribution



# NEGF - HF calculation





MO

Segment  
Orbital