



A microscopic approach to spin dynamics: about the meaning of spin relaxation times

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Outline

- Motivation
- Spin relaxation in semiconductors
- The concept of Bloch equations
- The spin-dependent Bloch equations
 - ▶ An extension of the optical Bloch equations
 - ▶ Comparison with experimental observables
- Conclusion

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- Reaching limits of conventional semiconductor technologies (e.g. transistors)
 - leakage currents
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 - ⇒ *Usage of the spin degree-of-freedom of carriers* (not only electronic devices, also optical devices)

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- Reaching limits of conventional semiconductor technologies (e.g. transistors)
 - leakage currents
 - heat
- Possible solution: **Spintronics**
 - ⇒ *Usage of the spin degree-of-freedom of carriers* (not only electronic devices, also optical devices)
- Limits of spintronics:
 - spin injection
 - ⇒ **spin relaxation and spin dephasing**

D'yakonov Perel' (DP) mechanism

- Origin: spin-orbit (SO) interaction in systems without **inversion-symmetry**
→ band splitting: $E_{\uparrow}(\mathbf{k}) \neq E_{\downarrow}(\mathbf{k})$

Structure of SO interaction: $\mathcal{H}_{SO} \sim \sigma \cdot \mathbf{B}(\mathbf{k})$

→ splitting corresponds to an effective **k-dependent** magnetic field $\mathbf{B}(\mathbf{k})$
⇒ **precession** of the spins around $\mathbf{B}(\mathbf{k})$

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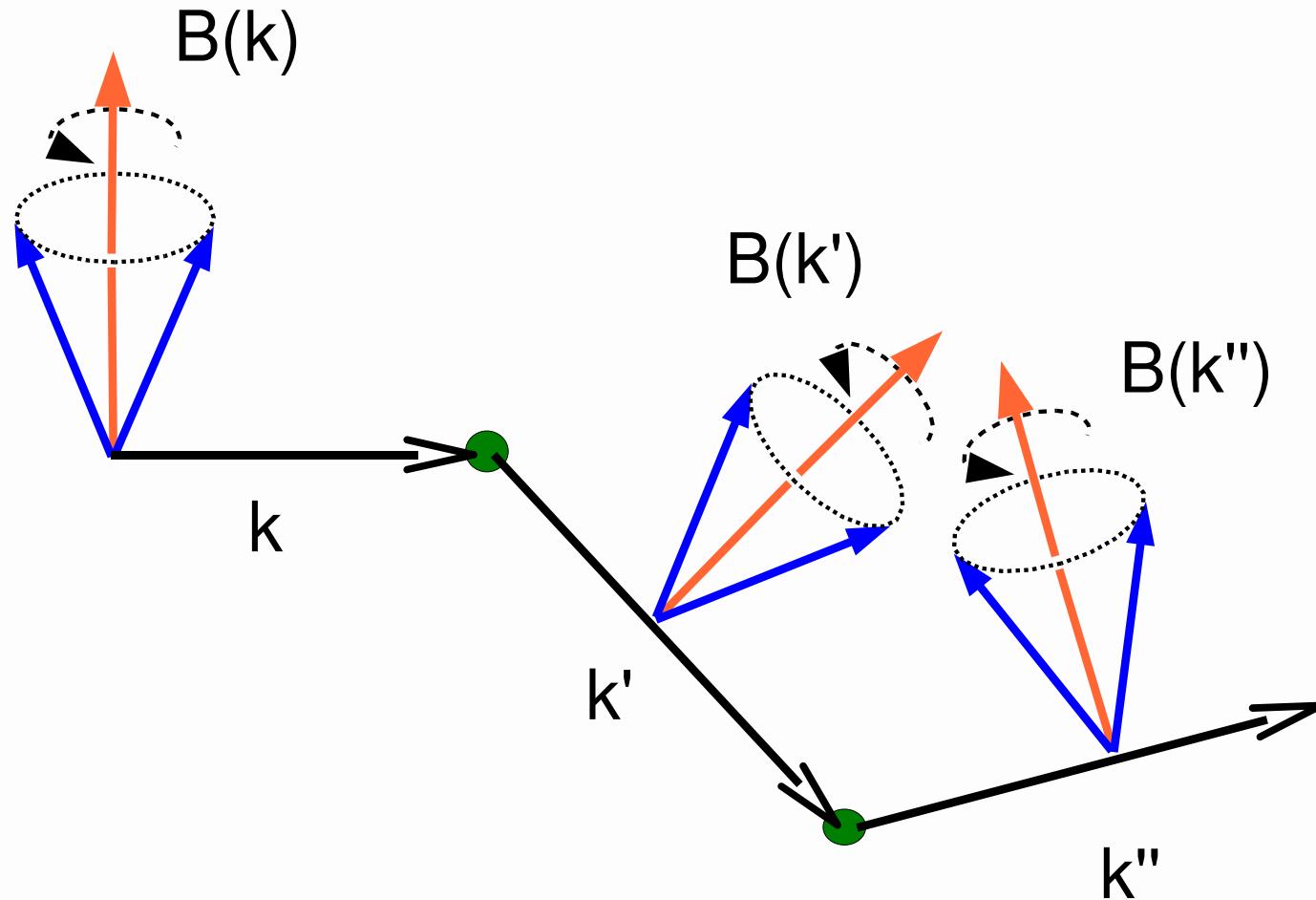
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- In addition: **scattering**
→ change of the k-vector of the electrons
→ change of the magnetic field $\mathbf{B}(\mathbf{k})$

Spin relaxation DP II





Spin relaxation DP III

⇒ Spin relaxation

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- Characteristics:

spin relaxation time \leftrightarrow scattering time
(motional narrowing)

$$\tau_s \sim \tau_p^{-1}$$

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- Sources of inversions-asymmetry:
bulk inversion-asymmetry (BIA/Dresselhaus)

$$B(k) \sim k^3$$

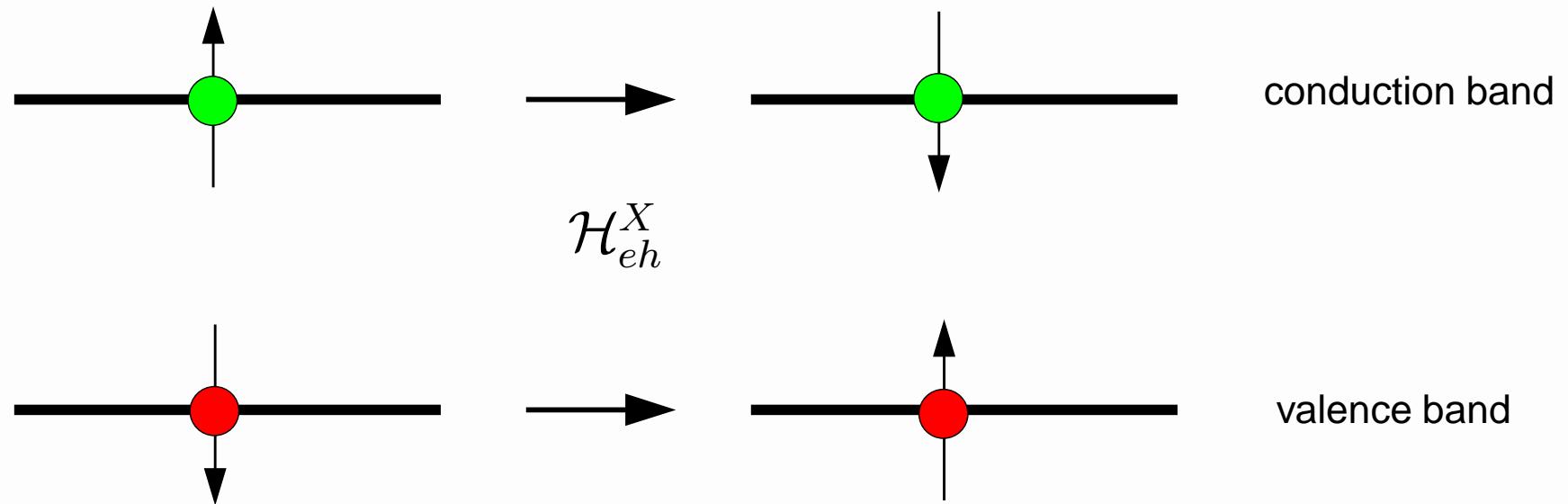
structure inversion-asymmetry (SIA/Rashba)

$$B(k) \sim k$$

Spin relaxation BAP

Bir Aronov Pikus (BAP) mechanism

- Scattering of electrons and holes due to **Coulomb-exchange interaction** possible
 - simultaneous spin-flip of electrons and holes
 - ⇒ restriction on electron system: spin relaxation



Spin relaxation EY

Elliott Yafet (EY) mechanism

- SO interaction leads to admixture of hole states in the valence band to electron states in the conduction band with opposite spin
 - no pure states
 - ⇒ direct spin flip scattering possible
- Characteristics:
spin relaxation time \leftrightarrow scattering time

$$\tau_s \sim \tau_p$$



- What is one of the best methods to describe dynamics in optically excited semiconductors?

Bloch equations I

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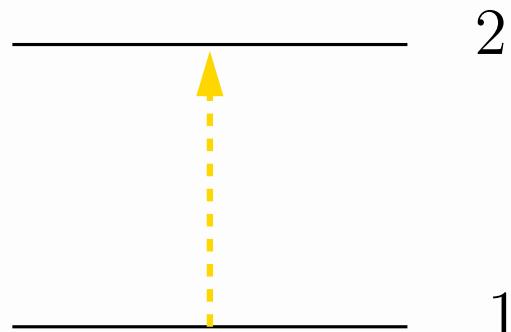
Bloch equations

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Bloch equations

- Example: optically driven two-level system

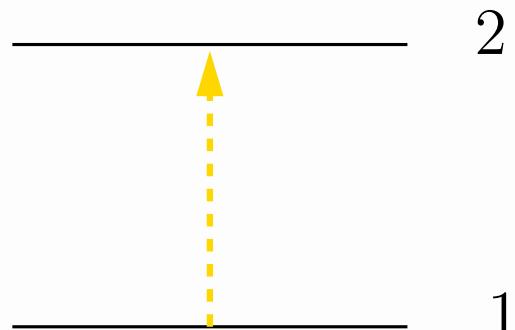


Bloch equations I

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Bloch equations

- Example: optically driven two-level system



Dynamical variables of the system:
occupation difference
coherence

Bloch equations II

- Description by 2×2 density matrix:

$$\varrho_{ij} := \langle c_i^\dagger c_j \rangle = \begin{cases} i = j & \text{occupation number} \\ i \neq j & \text{coherence} \end{cases}$$

- Equations of motion (EOM) given by *Liouville equation*

$$i \hbar \partial_t \varrho = [\mathcal{H}, \varrho]_-$$

- Decay of the components:
 - ▶ occupation number T_1 (\rightarrow diagonal entries)
 - ▶ coherence T_2 (\rightarrow offdiagonal entries)

Spindynamics I

- Possibility 1: classification of the spin states with respect to a **fixed quantization axis** (e.g. growth direction of a QW)

Spindynamics I

- Possibility 1: classification of the spin states with respect to a **fixed quantization axis** (e.g. growth direction of a QW)
- spin-up and spin-down electrons in the conduction band define two-level system (coupling via **SO interaction**)

$$\varrho(\mathbf{k}) := \begin{pmatrix} \varrho_{\uparrow\uparrow}(\mathbf{k}) & \varrho_{\uparrow\downarrow}(\mathbf{k}) \\ \varrho_{\downarrow\uparrow}(\mathbf{k}) & \varrho_{\downarrow\downarrow}(\mathbf{k}) \end{pmatrix}$$

Hamiltonian:

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{light} + \mathcal{H}_{scatt}$$

Spindynamics II

- Hamiltonian for a QW system with SO interaction

$$\mathcal{H}_0 = \sum_{\substack{\sigma \sigma' \\ \mathbf{k}'}} \left\{ \epsilon(\mathbf{k}') + \mathbf{h}(\mathbf{k}') \frac{\sigma_{\sigma \sigma'}}{2} \right\} c_{\sigma}^{\dagger}(\mathbf{k}') c_{\sigma'}(\mathbf{k}')$$

SO interaction: $\mathbf{h}(\mathbf{k}) = (h_x(\mathbf{k}), h_y(\mathbf{k}), 0)$

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- EOM:

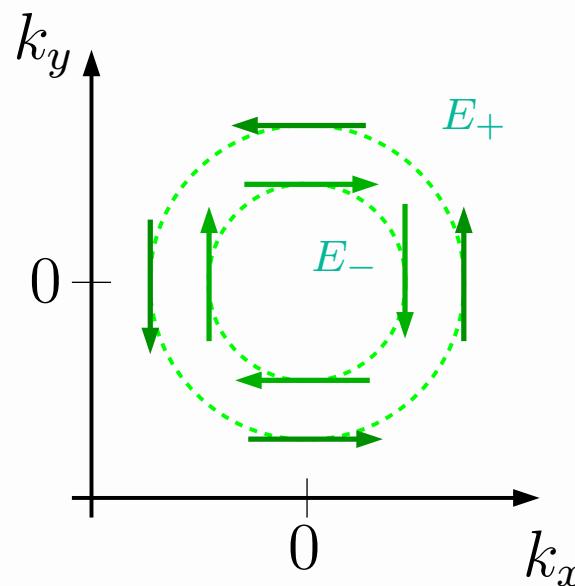
$$\partial_t \varrho_{\uparrow\uparrow}(\mathbf{k}) = -\frac{1}{\hbar} \left(h_x(\mathbf{k}) \Im\{\varrho_{\uparrow\downarrow}(\mathbf{k})\} - h_y(\mathbf{k}) \Re\{\varrho_{\uparrow\downarrow}(\mathbf{k})\} \right)$$

$$\partial_t \varrho_{\downarrow\downarrow}(\mathbf{k}) = \frac{1}{\hbar} \left(h_x(\mathbf{k}) \Im\{\varrho_{\uparrow\downarrow}(\mathbf{k})\} - h_y(\mathbf{k}) \Re\{\varrho_{\uparrow\downarrow}(\mathbf{k})\} \right)$$

$$\partial_t \varrho_{\uparrow\downarrow}(\mathbf{k}) = \frac{1}{2\hbar} \left(i h_x(\mathbf{k}) - h_y(\mathbf{k}) \right) \left(\varrho_{\uparrow\uparrow}(\mathbf{k}) - \varrho_{\downarrow\downarrow}(\mathbf{k}) \right)$$

Bloch equations with spin

- Aim: microscopic theory of spin relaxation based on the **Bloch equations**
- Formulation with **diagonal** kinetic part of Hamiltonian
 - Eigenstates
 - ⇒ Spin ($\pm \mathbf{m}_c$) depends on wavevector \mathbf{k}



Bloch equations with spin II

- scattering described in the density matrix formalism
 - restriction on electron-phonon scattering

⇒ Extension of the *optical* Bloch equations

- Starting point: six-level system
- Spin polarization is controlled by excitation with circularly polarized light

Bloch equations with spin III

- Hamiltonian:

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{light} + \mathcal{H}_{phonon}$$

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$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_{light} + \mathcal{H}_{phonon}$$

- Kinetic contribution:

$$\mathcal{H}_0 = \sum_{\mathbf{k}' m'_c} \epsilon_{m'_c}(\mathbf{k}') c_{m'_c}^\dagger(\mathbf{k}') c_{m'_c}(\mathbf{k}') + \sum_{\mathbf{k}' m'_v} \epsilon_{m'_v}(\mathbf{k}') v_{m'_v}(\mathbf{k}') v_{m'_v}^\dagger(\mathbf{k}')$$

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- **Hamiltonian is diagonal**
→ spin precession contained in **eigenenergies** $\epsilon_{m_i}(\mathbf{k})$
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→ spin precession contained in **eigenenergies** $\epsilon_{m_i}(\mathbf{k})$
[]
- Interaction with the light field:

$$\mathcal{H}_{light} = - \sum_{\substack{m'_c m'_v \\ \mathbf{k}'}} \left\{ \mathbf{E}(t) \cdot \mathbf{d}_{m'_c m'_v}^{cv}(\mathbf{k}') c_{m'_c}^\dagger(\mathbf{k}') v_{m'_v}^\dagger(\mathbf{k}') + \text{h.c.} \right\}$$

Bloch equations with spin VI

- Electron-phonon interaction \mathcal{H}_{phonon} :

$$\mathcal{H}_{phonon} =$$

Bloch equations with spin VI

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$$\mathcal{H}_{phonon} = \sum_{\mathbf{q}} \hbar \omega(\mathbf{q}) b^\dagger(\mathbf{q}) b(\mathbf{q})$$

Bloch equations with spin VI

- Electron-phonon interaction \mathcal{H}_{phonon} :

$$\mathcal{H}_{phonon} = \sum_{\mathbf{q}} \hbar \omega(\mathbf{q}) b^\dagger(\mathbf{q}) b(\mathbf{q})$$

$$+ \sum_{\mathbf{k}' \mathbf{q}} \left\{ \sum_{m'_c m''_c} \left(g_{m'_c m''_c}^e(\mathbf{q}) c_{m''_c}^\dagger(\mathbf{k}' + \mathbf{q}) b(\mathbf{q}) c_{m'_c}(\mathbf{k}') \right. \right.$$

$$\left. \left. + \text{h.c.} \right) \right\}$$

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Bloch equations with spin V

- Restriction to conduction band
→ 2×2 density matrix:

$$\varrho^{(m_c \bar{m}_c)}(\mathbf{k}) = \begin{pmatrix} \varrho_{m_c m_c}(\mathbf{k}) & \varrho_{m_c -m_c}(\mathbf{k}) \\ \varrho_{-m_c m_c}(\mathbf{k}) & \varrho_{-m_c -m_c}(\mathbf{k}) \end{pmatrix}$$

- Scattering treated in 2nd order Born approximation

Bloch equations with spin VI

- EOM of $\varrho_{m_c m_c}(\mathbf{k})$:

$$\begin{aligned} i\hbar \partial_t \varrho_{m_c m_c}(\mathbf{k}) = & \sum_{m_v} \left\{ \mathbf{E}(t) \cdot \mathbf{d}_{m_c m_v}^{cv}(\mathbf{k}) P_{m_c m_v}(\mathbf{k}) - \text{h.c.} \right\} \\ & + \sum_{\mathbf{q} m'_c} \left\{ g_{m'_c m_c}^e(\mathbf{q}) \langle c_{m'_c}^\dagger(\mathbf{k} + \mathbf{q}) b(\mathbf{q}) c_{m_c}(\mathbf{k}) \rangle \right. \\ & \quad - g_{m_c m'_c}^e(\mathbf{q}) \langle c_{m_c}^\dagger(\mathbf{k}) b(\mathbf{q}) c_{m'_c}(\mathbf{k} - \mathbf{q}) \rangle \\ & \quad + g_{m_c m'_c}^{e*}(\mathbf{q}) \langle c_{m'_c}^\dagger(\mathbf{k} - \mathbf{q}) b^\dagger(\mathbf{q}) c_{m_c}(\mathbf{k}) \rangle \\ & \quad \left. - g_{m'_c m_c}^{e*}(\mathbf{q}) \langle c_{m_c}^\dagger(\mathbf{k}) b^\dagger(\mathbf{q}) c_{m'_c}(\mathbf{k} + \mathbf{q}) \rangle \right\} \end{aligned}$$

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- **Hierarchy problem** due to *phonon-assisted* density matrices

Bloch equations with spin VII

Solution: truncation of the hierarchy

1. Derive EOM of the phonon-assisted density matrices
 2. Factorize the expectation values into their macroscopic parts
 3. Take only those which lead to a absolute squared value of the interaction matrix element
 4. Integrate and apply the *Markov* and *adiabatic* approximation
 5. Insert result into initial EOM
- Boltzmann limit

Results

- Diagonal entry:

$$\begin{aligned}\partial_t \varrho_{m_c m_c}(\mathbf{k})|_{phonon} &= -\Gamma_{m_c m_c}^{out}(\mathbf{k}) \varrho_{m_c m_c}(\mathbf{k}) \\ &\quad + \Gamma_{m_c m_c}^{in}(\mathbf{k})(1 - \varrho_{m_c m_c}(\mathbf{k}))\end{aligned}$$

- with:

$$\begin{aligned}\Gamma_{m_c m_c}^{out}(\mathbf{k}) &= \frac{\pi}{\hbar} \sum_{\mathbf{q}, m'_c} |g_{m'_c m_c}(\mathbf{q})|^2 \times \\ &\left\{ \delta \left(\epsilon_{m'_c}(\mathbf{k} + \mathbf{q}) - \epsilon_{m_c}(\mathbf{k}) - \hbar\omega(\mathbf{q}) \right) \left(1 - \varrho_{m'_c m'_c}(\mathbf{k} + \mathbf{q}) \right) \beta(\mathbf{q}) + \right. \\ &\delta \left(\epsilon_{m'_c}(\mathbf{k} - \mathbf{q}) - \epsilon_{m_c}(\mathbf{k}) + \hbar\omega(\mathbf{q}) \right) \left(1 - \varrho_{m'_c m'_c}(\mathbf{k} - \mathbf{q}) \right) \times \\ &\left. (1 + \beta(\mathbf{q})) \right\}\end{aligned}$$

Results II

- Offdiagonal entry:

$$\partial_t \varrho_{m_c - m_c}(\mathbf{k})|_{phonon} = \frac{1}{i\hbar} \Sigma_{m_c - m_c}^{e-p}(\mathbf{k}) \varrho_{m_c - m_c}(\mathbf{k})$$

- Self-energy

$$\Sigma_{m_c - m_c}^{e-p}(\mathbf{k}) = \hbar \left(\Omega_{m_c - m_c}^{e-p}(\mathbf{k}) - i \Gamma_{m_c - m_c}^{e-p}(\mathbf{k}) \right)$$

- real and imaginary part are connected via
Kramers-Kronig relation

Results III

Imaginary part of the self-energy

$$\begin{aligned}
 \Gamma_{m_c - m_c}^{e-p}(\mathbf{k}) = & \\
 \frac{\pi}{\hbar} \sum_{\mathbf{q} m'_c} \Big\{ & |g_{m'_c m_c}^e(\mathbf{q})|^2 \delta(\epsilon_{m'_c}(\mathbf{k} + \mathbf{q}) - \epsilon_{-m_c}(\mathbf{k}) - \hbar\omega(\mathbf{q})) \times \\
 & [(1 - \varrho_{m'_c m'_c}(\mathbf{k} + \mathbf{q})) \beta(\mathbf{q}) + \varrho_{m'_c m'_c}(\mathbf{k} + \mathbf{q})(1 + \beta(\mathbf{q}))] \\
 & + |g_{m'_c m_c}^e(\mathbf{q})|^2 \delta(\epsilon_{m'_c}(\mathbf{k} - \mathbf{q}) - \epsilon_{-m_c}(\mathbf{k}) + \hbar\omega(\mathbf{q})) \times \\
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 & [(1 - \varrho_{m'_c m'_c}(\mathbf{k} + \mathbf{q})) \beta(\mathbf{q}) + \varrho_{m'_c m'_c}(\mathbf{k} + \mathbf{q})(1 + \beta(\mathbf{q}))] \Big\}
 \end{aligned}$$

Result IV

- Offdiagonal-entry: scattering contributions *beyond* the Boltzmann limit
(different truncation rules, but still 2nd order Born approximation)

$$\partial_t \varrho_{m_c - m_c}(\mathbf{k}) = -\frac{1}{i\hbar} \sum_{\mathbf{q} m'_c} \bar{\Sigma}_{m'_c - m'_c}^{e-p}(\mathbf{q}) \varrho_{m'_c - m'_c}(\mathbf{k} + \mathbf{q})$$

- self-energy

$$\bar{\Sigma}_{m'_c - m'_c}^{e-p}(\mathbf{q}) = \hbar \left(\bar{\Omega}_{m'_c - m'_c}^{e-p}(\mathbf{q}) - i \bar{\Gamma}_{m'_c - m'_c}^{e-p}(\mathbf{q}) \right)$$

- contributions are **not** connected via *Kramers-Kronig relation*

Summary of results

- Typical form of EOM in 2nd order Born approximation
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⇒ **spin dependent optical Bloch equations**

⇒ Decay times

Decay times

- Formal definition of decay times:

$$\frac{1}{T_{1,\mathbf{k}}} = \sum_{m'_c} \left(\Gamma_{m'_c m'_c}^{in}(\mathbf{k}) + \Gamma_{m'_c m'_c}^{out}(\mathbf{k}) \right)$$

$$\frac{1}{T_{2,\mathbf{k}}} = \Gamma_{m_c - m_c}^{e-p}(\mathbf{k})$$

- Result for **small spin splitting**:

$$T_{1,\mathbf{k}} \simeq T_{2,\mathbf{k}}$$

- Result for **spin degenerate**:

$$T_{1,\mathbf{k}} = T_{2,\mathbf{k}}$$

⇒ Experimental observables

Observables

- Experimental observables:

Spin polarization S (\rightarrow spin relaxation):

$$S = \sum_{\mathbf{k}} (\varrho_{\uparrow\uparrow}(\mathbf{k}) - \varrho_{\downarrow\downarrow}(\mathbf{k}))$$

Spin coherence C (\rightarrow spin dephasing):

$$C = \sum_{\mathbf{k}} |\varrho_{\uparrow\downarrow}(\mathbf{k})|$$

Observables

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⇒ Unitary transformation

Transformation

- Transformed density matrix (*Rashba SO interaction*)

$$\varrho^{(\uparrow\downarrow)}(\mathbf{k})|_{\text{Rashba}} =$$

$$\frac{1}{2} \begin{pmatrix} d_+ + 2\Im \{\varrho_{m_c - m_c}(\mathbf{k}) e^{i\varphi}\} & d_- + 2i\Re \{\varrho_{m_c - m_c}(\mathbf{k}) e^{i\varphi}\} \\ d_- - 2i\Re \{\varrho_{m_c - m_c}(\mathbf{k}) e^{i\varphi}\} & d_+ - 2\Im \{\varrho_{m_c - m_c}(\mathbf{k}) e^{i\varphi}\} \end{pmatrix}$$

with

$$d_{\pm} = \varrho_{m_c m_c}(\mathbf{k}) \pm \varrho_{-m_c -m_c}(\mathbf{k})$$

and

$$\varphi = \triangleleft(k_x, k_y)$$

Transformation II

- Observables:

$$S = \sum_{\mathbf{k}} 4\Re \left\{ -i e^{-i\varphi} \varrho_{m_c - m_c}(\mathbf{k}) \right\}$$

$$C = \sum_{\mathbf{k}} \sqrt{d_-^2 + 4\Im \left\{ -i e^{-i\varphi} \varrho_{m_c - m_c}(\mathbf{k}) \right\}}$$

- Spin relaxation is ruled by $T_{2,\mathbf{k}}$ of the Bloch equations
- Spin dephasing is ruled by a combination of $T_{1,\mathbf{k}}$ and $T_{2,\mathbf{k}}$ of the Bloch equations
- Connection discussed by M.E. Flatté et al. in
Semiconductor Spintronics and Quantum Computation
but here: microscopic theory

- Concept of Bloch equations:

Extension towards spin dynamics

Conclusion

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Extension towards spin dynamics
- Microscopic description of spin dynamics:
optical Bloch equations with spin
→ electron-phonon scattering

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→ electron-phonon scattering
- Formal definition of T_1 and T_2 times
- Connection between decay times of Bloch equations and spin relaxation/dephasing times

Outlook

- Extension of semiconductor Bloch equations
→ inclusion of many-particle effects (**already done**)
- Numerical evaluation of equations (**work in progress**)
- More information: **cond-mat/0412370**

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THANK YOU FOR YOUR
ATTENTION!