

# Disorder effects on spin dependent tunneling

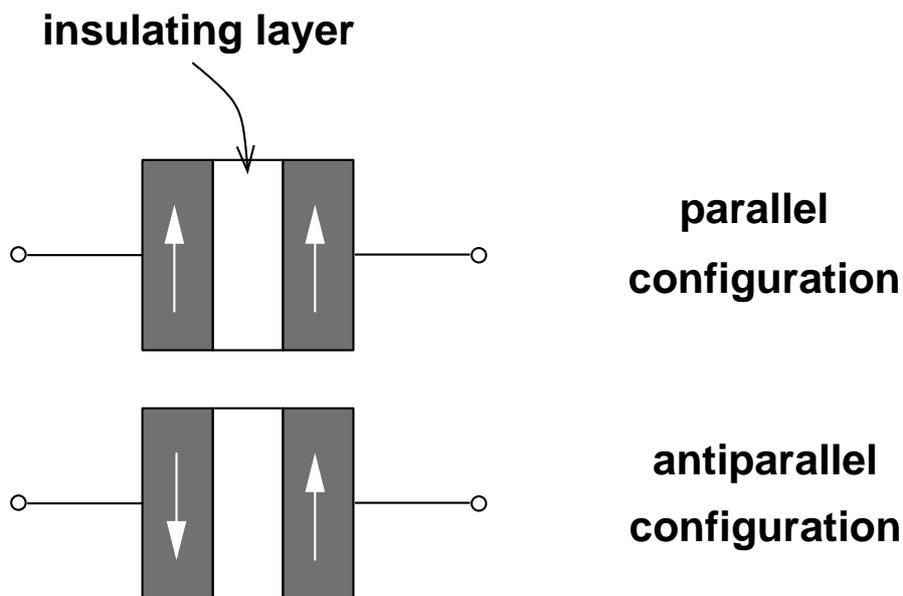
Michael Wimmer and Klaus Richter

## Outline of the talk

- Motivation and Definitions
- Overview of theoretical models
  - Juillièrè's model
  - *ab initio* calculations
  - Bratkovsky's model
  - Extension of Bratkovsky's model
- Results
  - Magnetic field dependence
  - Effect of disorder on the TMR
  - Connection to Juillièrè's model
- Conclusion

## Tunneling magnetoresistance

The resistance of an insulating layer sandwiched between two ferromagnetic contacts depends on the alignment of the magnetization in the ferromagnets:



The resistance is *higher* in the antiparallel configuration.

The TMR ratio is defined as

$$TMR = \frac{R_{AP} - R_P}{R_P}$$

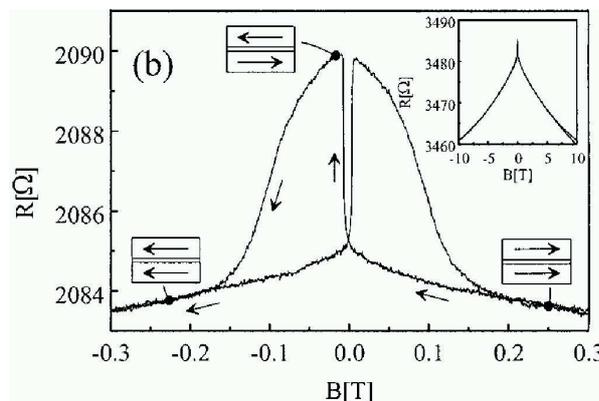
- Juillère 1975: TMR 14% at 4.2 K and small bias voltages (Ge)
- today: TMR > 10% at room temperature and higher voltages ( $\text{Al}_2\text{O}_3$ )

The TMR effect has promising applications in spin-electronics: magnetic sensors, hard disks, MRAMs

# Experiments

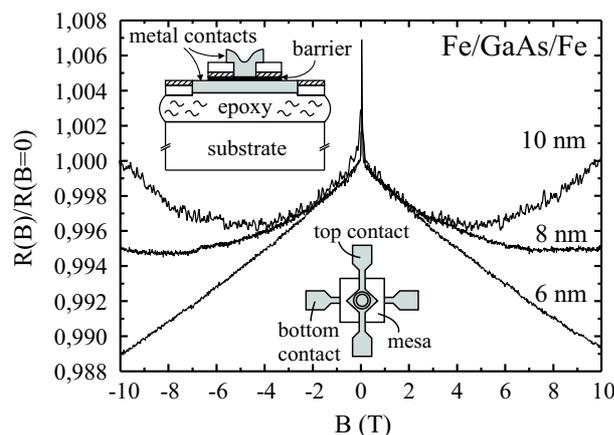
Experiments in the group of Prof. Weiss in Regensburg on Fe/GaAs/Fe tunnel junctions

- small TMR effect: 0.2–1.7% (band structure considerations predicted  $\approx 100\%$ !)



S. Kreuzer *et al.*, Appl. Phys. Lett., **80**, 4582 (2002)

- anomalous magnetoresistance in high magnetic fields

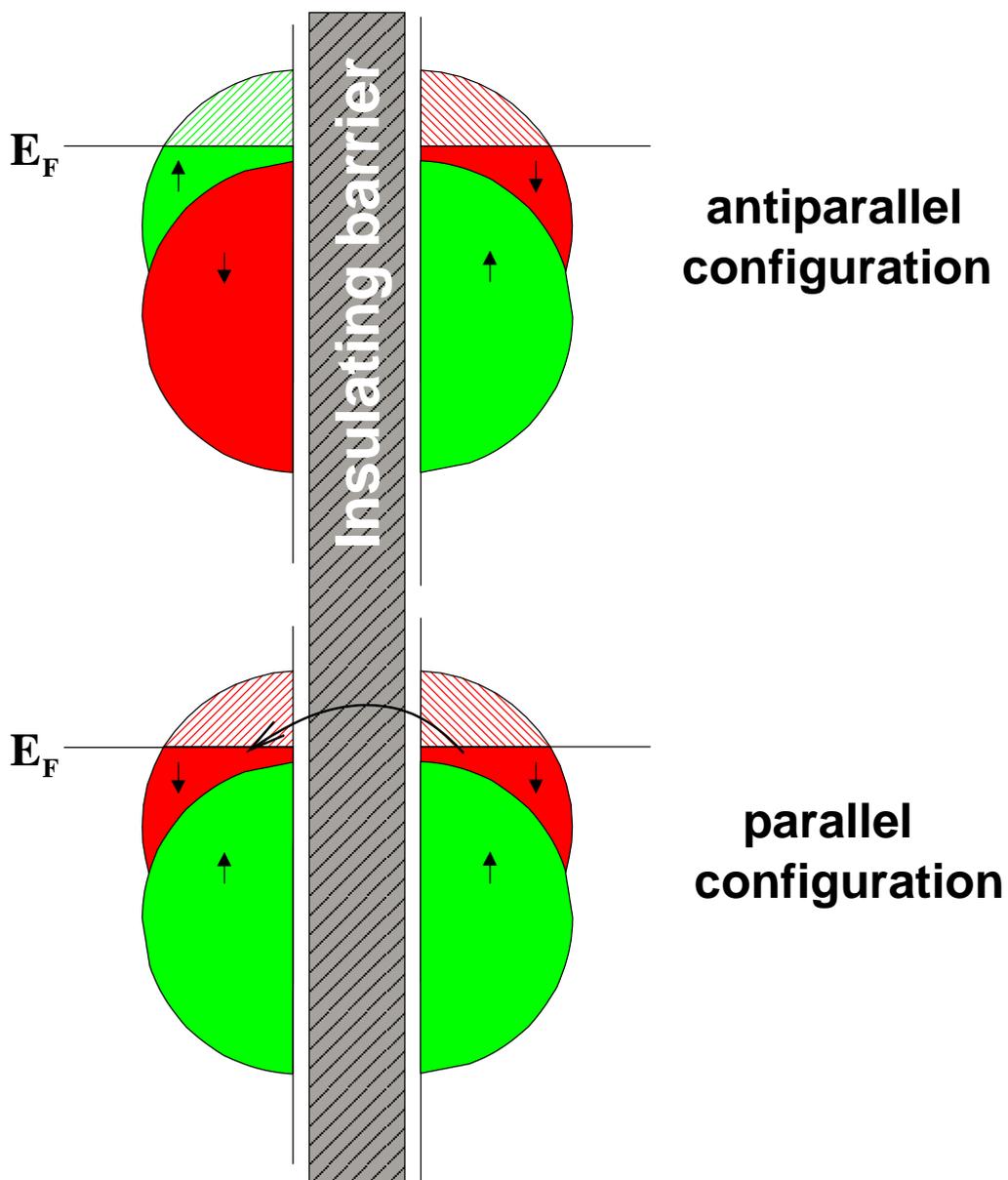


M. Zenger *et al.*, to be published in Appl. Phys. Lett.

- ➔ Interdiffusion of iron atoms in GaAs barrier?
- ➔ Importance of spin flip scattering?

## Physics behind TMR

The density of states of a magnet is different for spin up and spin down. Tunneling depends on the density of states:



## Juillièrè's model

Physics Letters **54A**, 225(1975)

Assuming that the conductance is proportional to the DOS, the TMR ratio reads:

$$TMR = \frac{2P^2}{1 - P^2}$$

where  $P$  is the (spin) polarization of the ferromagnets:

$$P = \frac{D_{\uparrow}(E_F) - D_{\downarrow}(E_F)}{D_{\uparrow}(E_F) + D_{\downarrow}(E_F)}$$

- widely used to interpret experiment
- TMR ratio intrinsic property to the ferromagnetic leads
- rather useful for e.g.  $\text{Al}_2\text{O}_3$  barriers
- however: overestimates TMR value for GaAs barrier

From a theoretical point of view:

Model is valid for the case of a very **high** and **disordered** barrier!

D. Ryndyk, unpublished

## *ab initio* calculations

Try to model the system as detailed as possible:

- structure
- electronic properties
- relativistic effects (spin-orbit, ...)

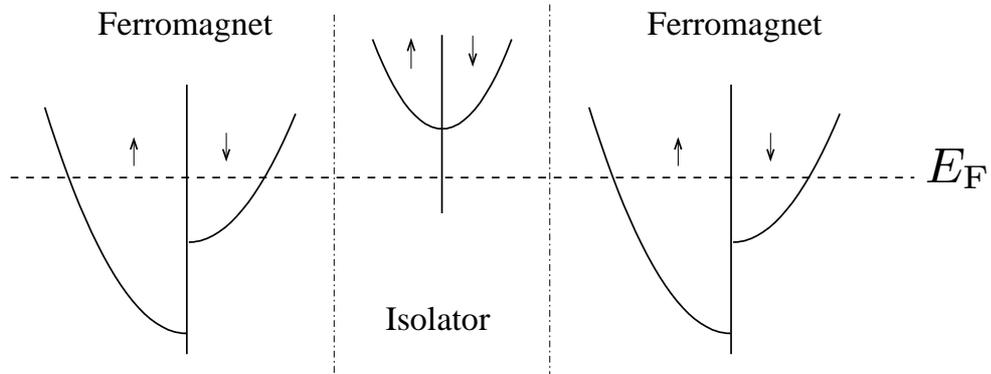
but:

- usually limited to epitaxial systems
- numerics can be difficult → various problems
- in my opinion: results can be difficult to interpret
- Prediction for GaAs barrier:  $TMR \approx 100\%$
- large TMR values arise because of *symmetries*

# Bratkovsky's model

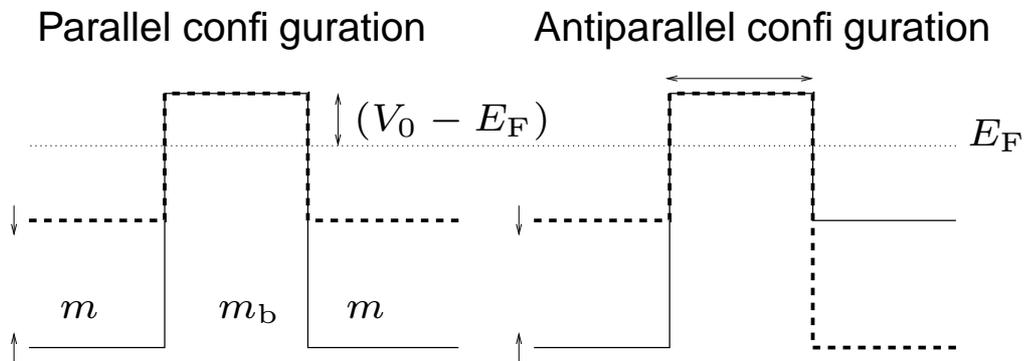
PRB **39**, 6995 (1989), PRB **56**, 2344 (1997)

Model the system using a free electron gas description:



- ferromagnet: exchange splitting.
- different materials: different effective mass  $m^*$ .

⇒ “Tunneling through a step barrier”



*Symmetry in the system*

We consider a **clean** system

⇒ translational symmetry parallel to the barrier

⇒ conservation of parallel momentum  $k_{||}$ .

⇒ independent transport channels

## Bratkovsky's model - part 2

### *Bratkovsky's approximations*

This model can be solved exactly (numerically). But there is some useful approximation:

In the case of a **low** barrier,

- transport is essentially **one-dimensional**,
- only perpendicular incidence is transmitted.

In this limit the Juillièrè model holds with a **modified** Polarization  $P_{\text{eff}}$ :

$$P_{\text{eff}} = P \frac{\kappa_0 - (m_b/m)^2 k_{F,\uparrow} k_{F,\downarrow}}{\kappa_0 + (m_b/m)^2 k_{F,\uparrow} k_{F,\downarrow}}$$

- IF the effective mass in the barrier is small compared to the electron mass  $m_b \ll m_e$   
 $\Rightarrow$  The same result as Juillièrè's model  
 BUT: this is just a coincidence, the physics is totally different!
- Again: no quantitative agreement with experiment.

## Comparison of models

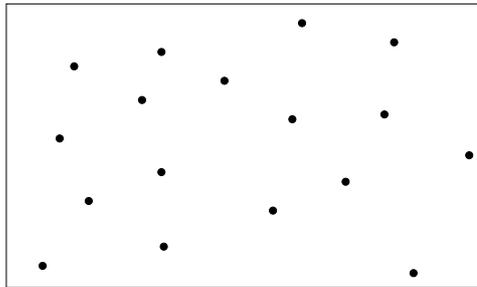
Juillièrè's model	Bratkovsky's model	<i>ab initio</i> calculations
high barrier	low barrier	any system
disordered system	clean system	epitaxial systems

- Juillièrè's and Bratkovsky's model describe contrary situations
- Juillièrè's model more appropriate for oxide barriers
- Bratkovsky's model maybe appropriate for semiconductor barriers?

## Model and technique

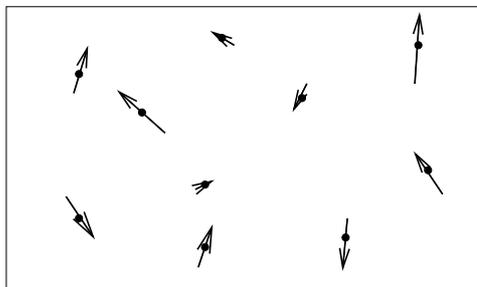
Extend Bratkovsky's model to include disorder:

- elastic disorder:  $\delta$ -peaked impurities with random position and strength



⇒ isotropic momentum scattering

- spin-flip disorder:  $\delta$ -peaked impurities with random position and a small random magnetization



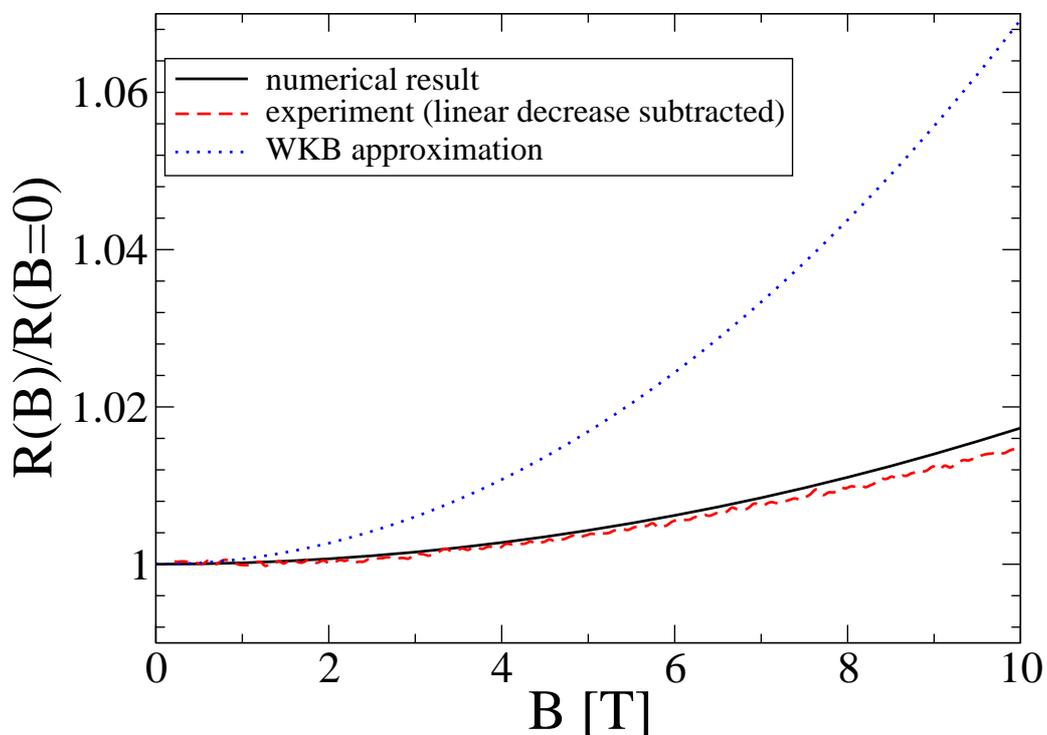
⇒ spin-flip **and** momentum scattering

- model is useful to describe scattering on **magnetic** impurities (e.g. iron atoms in GaAs)
- not suited for magnon scattering
- low-bias and  $T = 0$  limit
- conductance is now calculated numerically

# Magnetic field dependence of tunnel resistance

We consider a magnetic field parallel to the tunnel barrier

- WKB approximation: quadratic increase of resistance  
(L. Eaves, in *The physics and fabrication of microstructures and microdevices*)
- our numerical studies show **qualitative** agreement with WKB approximation, but better **quantitative** agreement with experiment



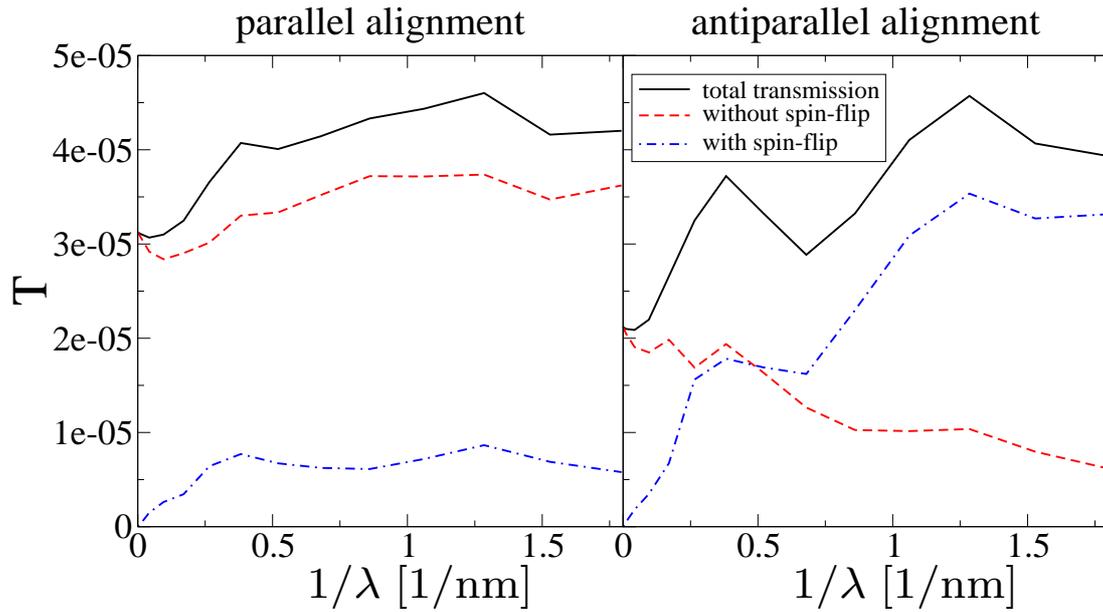
→ simple model can capture a lot of the relevant physics.

# Disorder at interface – transmission

Consider disorder only close to interface

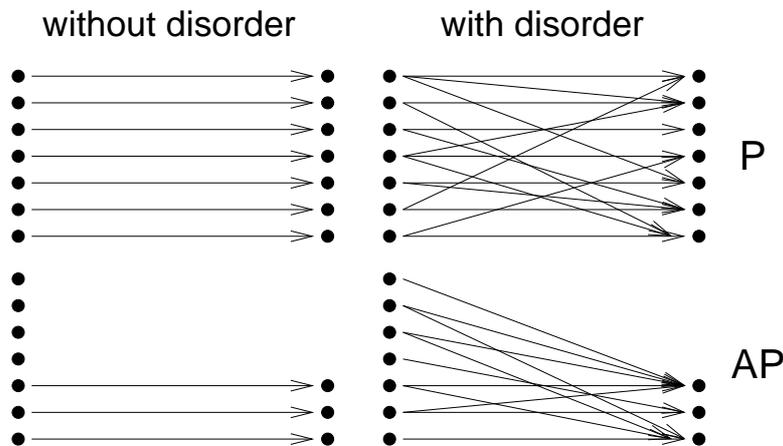


Transmission with spin-flips:



→ overall transmission is increased

→ disorder lifts  $k_{||}$ -conservation



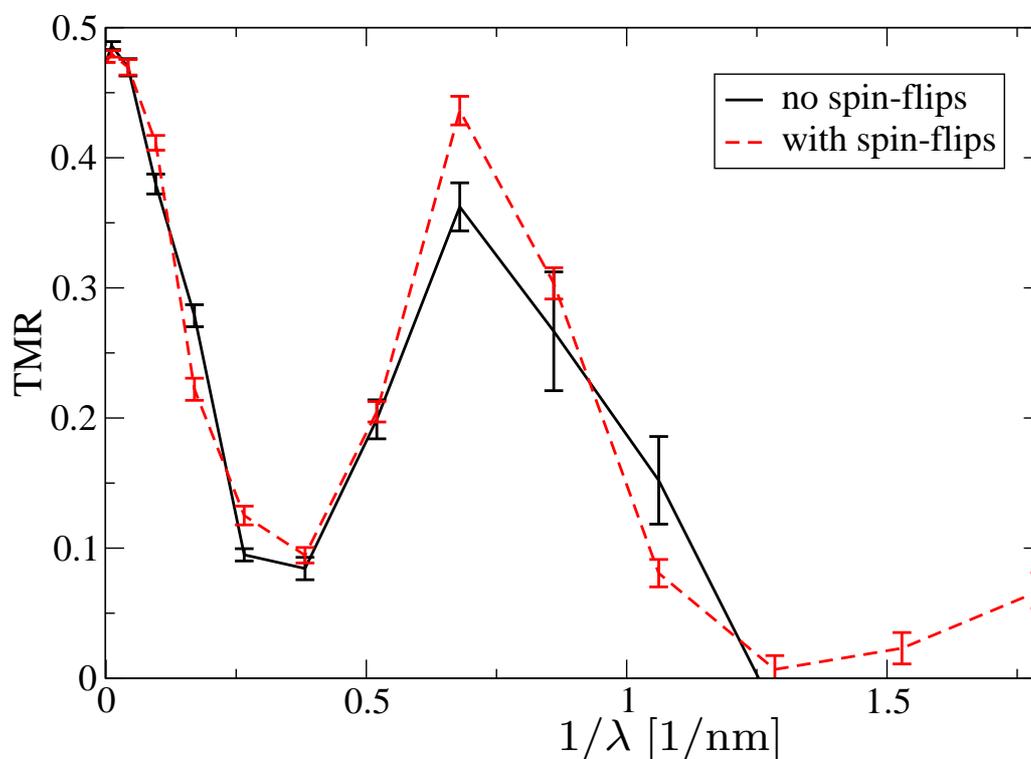
→ increase in antiparallel case is stronger than in parallel case

⇒ decrease in TMR ratio

## Disorder at interface – TMR ratio

Definition:  $TMR = \frac{R_{AP} - R_P}{R_P}$ . (“optimistic” TMR ratio)

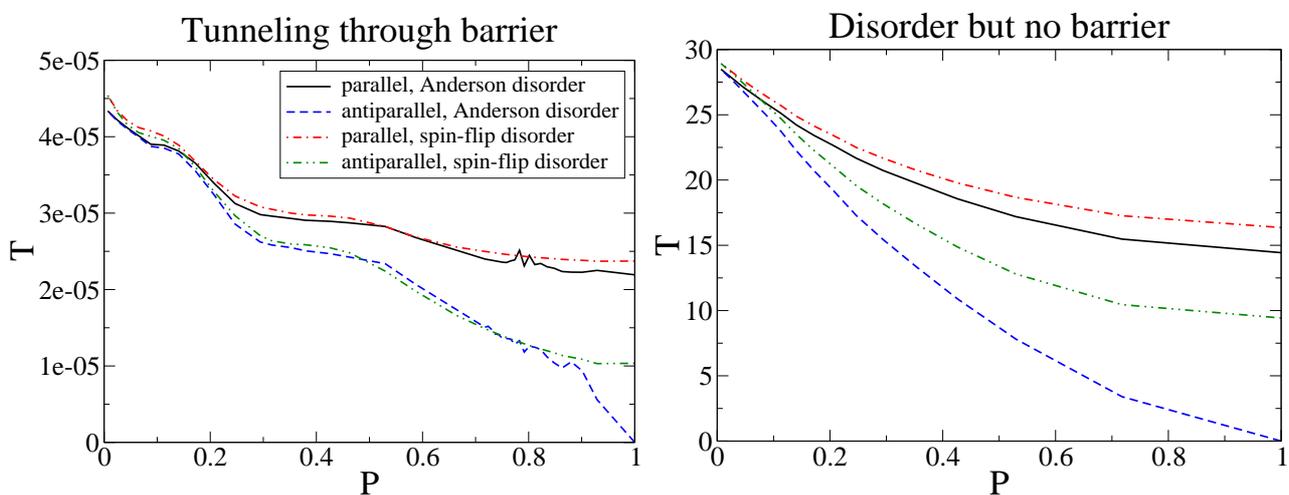
Effect of disorder on the TMR ratio:



- disorder can decrease the TMR effect significantly
- almost **identical** decrease of TMR ratio for spin conserving and spin-flip scattering!

## Disorder at interface – polarization dependence

Transmission in the presence of disorder depending on the spin-polarization  $P$  of the ferromagnets:



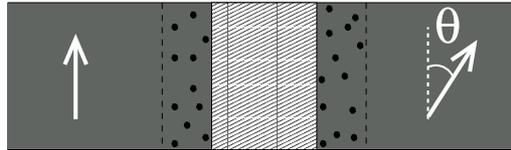
→ similar behaviour of tunneling probability for spin-conserving and spin-flip scattering except for  $P \approx 1$

→ **but:** significant effect of spin-flips without barrier!

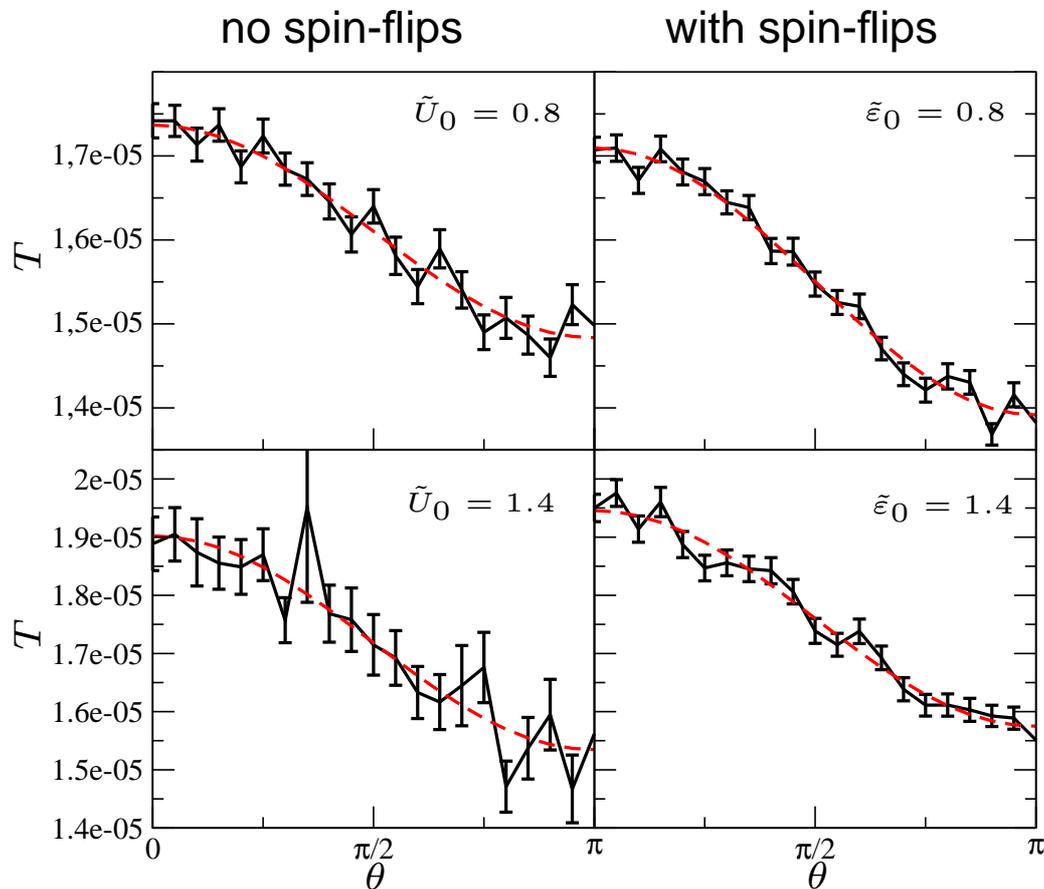
⇒ spin-flips less important because barrier acts as a quasi one-dimensional channel?

## Disorder at interface – angular dependence

Dependence of transmission probability on the angle between the magnetizations in the ferromagnet with disorder:



Transmission probabilities:

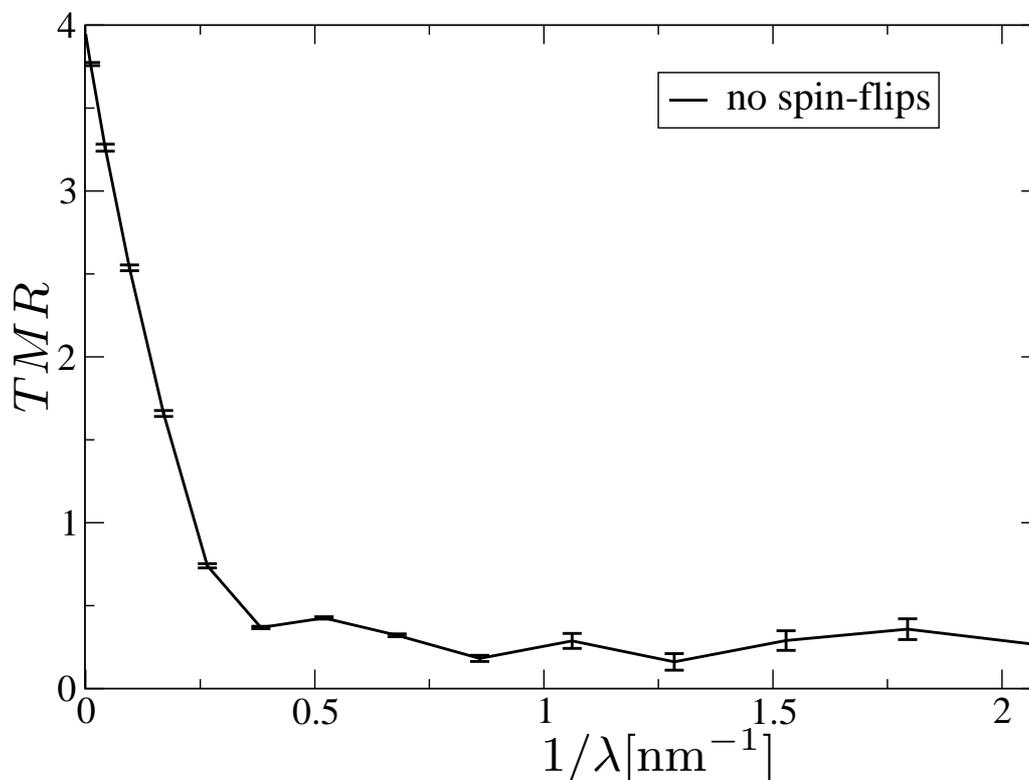


- angular dependence shows  $\cos$ -behaviour just as in clean case, regardless of scattering
- “effective” (spin) polarization is decreased

## What about Juillièrè's model?

- Juillièrè's model rather successful for  $\text{Al}_2\text{O}_3$  barriers
- oxide barriers are usually amorphous  $\rightarrow$  a lot of disorder
- we just showed that disorder decreases the TMR ratio ...

Consider the case of a **very high** barrier (15 eV) and disorder at the barrier interface



- $\rightarrow$  disorder again **reduces** TMR value drastically
- $\rightarrow$  BUT: TMR ratio saturates at a value above 0
- $\rightarrow$  this is consistent with Juillièrè's model: a finite TMR ratio for a high, disordered barrier.

## Conclusions

We have shown that:

- Disorder can decrease the TMR effect significantly.
- Spin-flips have little influence on the TMR ratio if there is also momentum scattering.
- The TMR of high tunnel barriers (e.g. oxide barriers) is more robust against disorder than low barriers (e.g. semiconducting barriers)

Have we explained the experimental findings?

Maybe. Maybe not.

- The model of the system may be too simple.
- The strength of the impurities is a *parameter* in our simulations, it should be calculated from first principles.
- However: the simulations can show us *trends*:
  - ➔ Although the semiconducting barrier itself is one-crystalline, having a clean interface might be crucial for such a low barrier, in contrast to the rather high oxide barriers  $\Rightarrow$  contradicts our intuition!

## Suggestions to the experimentalists

Unfortunately I don't have any. But open for discussion ...