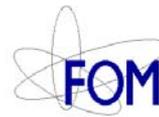


Spin pumping : control of electrons and nuclei in nanostructures

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Outline

- **Introduction :** - quantum pumping and its history
- charge pumping
- spin pumping
- **Pumping of electrons in the quantum Hall regime :**
transport of **electrons** and control of **nuclei**
- **Discussion**

Introduction

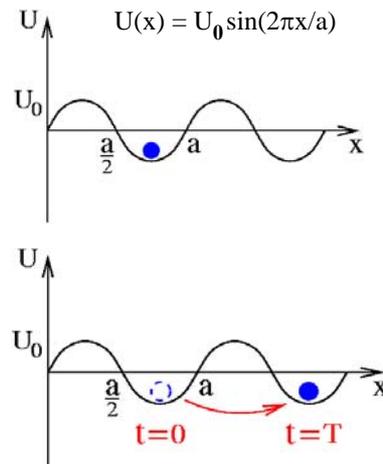
Idea behind pumping : to generate motion of particles by slow **periodic modulations** of their environment, e.g. their confining potential or a magnetic field.

Thouless pump, 1983 : adiabatic transport of electrons in 1D periodic potential

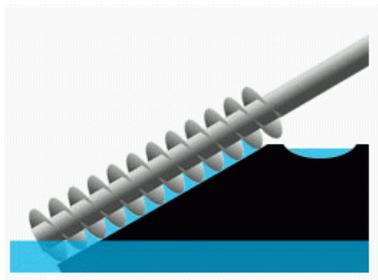
For **moving** potential, **every minimum is shifted by a** after each period T :

$$U(x+vt) = U_0 \sin(2\pi x/a) \cos(2\pi t/T) + U_0 \cos(2\pi x/a) \sin(2\pi t/T)$$

Superposition of two standing waves with a phase difference can produce pumping



Archimedean screw

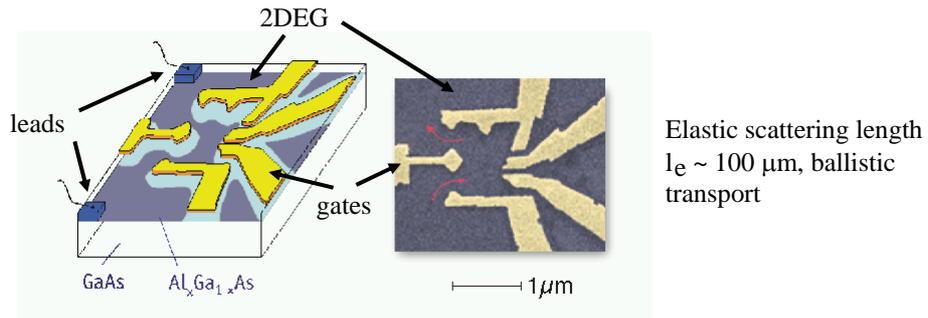


- over 2000 years old
- used for irrigation

's Hertogenbosch, NL

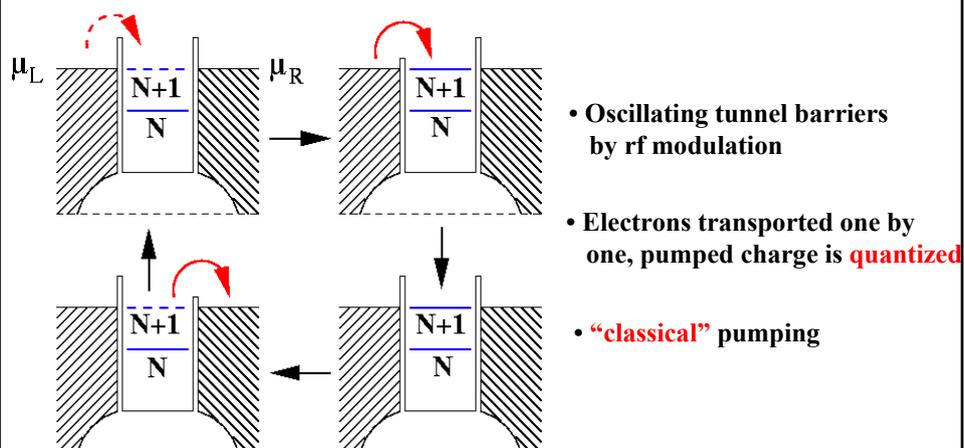
Charge pumping in condensed matter systems

Quantum dot = small island in a metal or semiconductor material (two-dimensional electron gas, 2DEG), confined by **gates** and connected to leads via **quantum point contacts (QPCs)**.



Quantum dots can be **open** (wide QPCs) or **closed** (QPCs pinched off).

First electron pump : turnstile

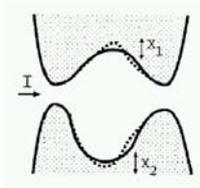


Kouwenhoven *et al.*, PRL **67**, 1626 (1992)
 Pothier *et al.*, Europhys. Lett. **17**, 249 (1992)

Quantum pumping in quantum dots : idea

Spivak *et al.*, PRL 51, 13226 (1995)

Open quantum dot



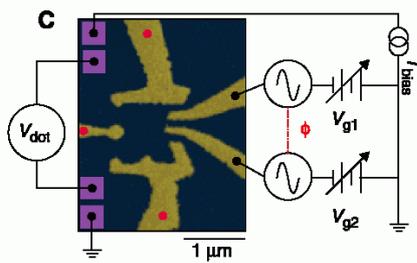
Current generated by **adiabatic periodic variation** of parameters X_1 and X_2 (gate voltage, magnetic field) with a **phase difference**

Physical picture : infinitesimal change of system parameters δX_i during a time δt leads to a **redistribution of charge** δQ_i within the system (due to changing electrostatic landscape). This redistribution produces electron flows $I_i = \delta Q_i / \delta t$

- pumped charge **depends on the interference of electron wavefunctions** in the system.
- current in general **not quantized** and its **direction** depends on microscopic properties of the (chaotic) system
- reversing phase difference reverses the direction of the current

Quantum pumping experiment

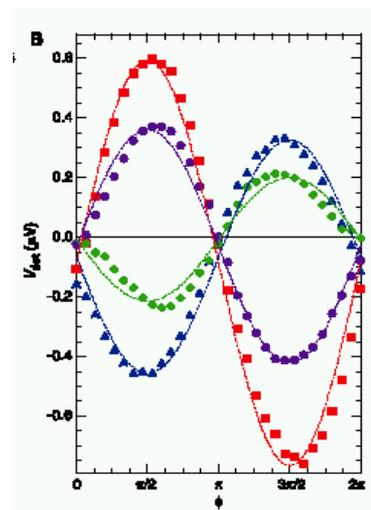
Switkes *et al.*, Science 283, 1905 (1999)



Experimental set-up, open quantum dot

Red gates control the conductance of the point contacts

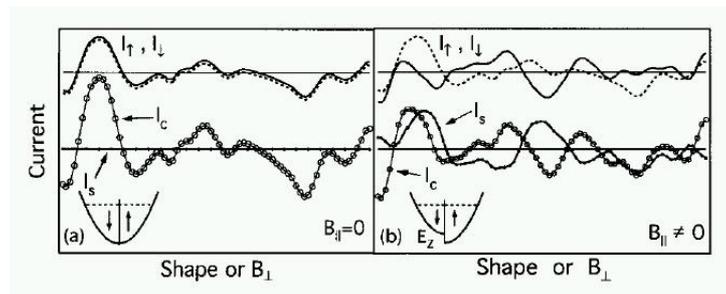
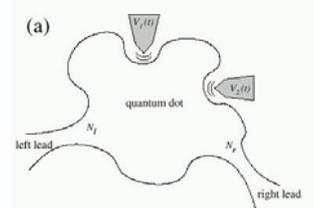
Black gates are used for pumping



Pumped current vs. phase difference ϕ

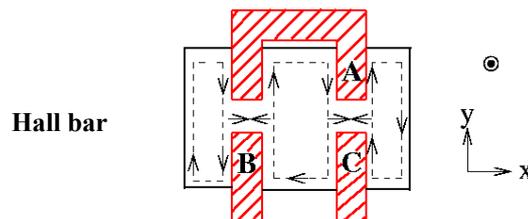
Spin pumping in quantum dots

Quantum dot in parallel magnetic field



Watson *et al.*, PRL **91**, 258301 (2003)
Mucciolo *et al.*, PRL **89**, 146802 (2002)

Spin pumping in the quantum Hall regime



Characteristics :

- electrons travel along the edges of the sample (edge channels)
- quantized energy levels (Landau levels)
- # of edge channels corresponds to the # of (partially) filled Landau levels ν
- separation of “left-movers” and “right-movers”
- electrons can be **scattered** from one side to another

Idea : investigate pumping of electrons across a Hall bar and the effect on the nuclei via hyperfine interaction

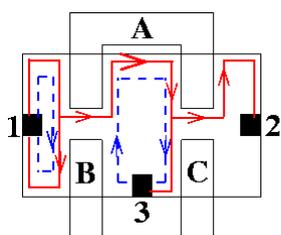
Motivation : era of quantum computing and quantum information processing. **Spins**, electronic but also nuclear, are promising candidates for qubits because of their long coherence times.

Drawback : difficult to measure spin effects directly, easier to measure charge

Ideally : manipulate and read-out spin processes via charge

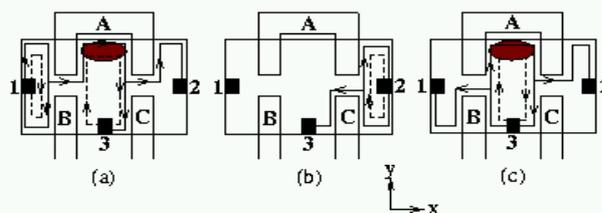
Here : contribution towards manipulation and read-out of nuclear spins via pumped current

Charge pumping in a Hall bar



- AB and AC form 2 quantum point contacts (QPC's)
- $\nu = 2$: spin-split Landau levels, one for **spin-up** and one for **spin-down**
- the QPC's transmit at most one edge channel
- time-varying voltages applied to B and C form pumping parameters

Current flow :



The pumped current

Dynamics of electrons in absence of gates is described by Hamiltonian :

$$\mathcal{H} = \frac{1}{2m^*} (i\hbar\vec{\nabla} + e\vec{A})^2 + V(y) + \frac{1}{2}g^* \mu_B B \sigma + \frac{1}{2}A(I_z)\sigma$$

For harmonic potential $V(y) = \frac{1}{2} m^* \omega_0^2 y^2$ the Schrödinger equation is exactly solvable → Landau levels

$$\begin{aligned} \psi_{\lambda,\sigma}(x, y, t) &= C_\lambda \chi_\lambda(y) e^{i(\hbar x - \frac{E_{\lambda,\sigma} t}{\hbar})}, \\ \chi_\lambda(y) &= e^{-\frac{1}{2i\hbar}(y + \frac{\omega_c^2}{\omega_0^2 + \omega_c^2} y_k)^2} \left(\frac{\partial}{\partial y} \right)^\lambda e^{-\frac{1}{2i\hbar}(y + \frac{\omega_c^2}{\omega_0^2 + \omega_c^2} y_k)^2} \\ E_{\lambda,\sigma} &= \left(\lambda + \frac{1}{2}\right) \hbar \sqrt{\omega_0^2 + \omega_c^2} + \frac{1}{2} m^* \frac{\omega_0^2 \omega_c^2}{\omega_0^2 + \omega_c^2} y_k^2 \\ &\quad + \frac{1}{2} g^* \mu_B B \sigma + \frac{1}{2} A(I_z) \sigma, \quad \lambda = 0, 1, 2, \dots \end{aligned}$$

Model QPC's as δ -function barriers and use Floquet theory to find pumped current into contact 1, 2 and 3:

$$I_\alpha = \frac{e}{\hbar} \int dE f(E) \sum_{E_n > 0} (|t_{\alpha\beta}(E_n, E)|^2 - |t_{\beta\alpha}(E_n, E)|^2)$$

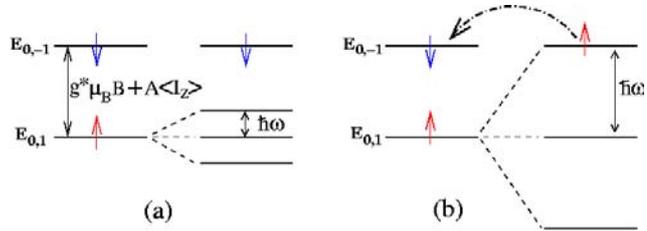
Floquet theory describes pumping in terms of **gain or loss of energy quanta $\hbar\omega$** at the two oscillating barriers

Incoming particle with energy E leaves with energy $E_n \equiv E + n\hbar\omega$

The Floquet scattering matrix is obtained by matching wave functions

$$\psi(x, t) = \sum_{n=-\infty}^{\infty} (a_n e^{ik_n x} + b_n e^{-ik_n x}) e^{-i(E_{0,1} + n\hbar\omega)t/\hbar}$$

Energy level diagrams



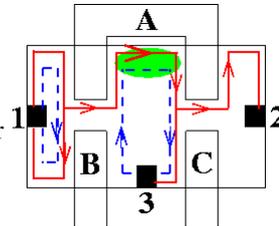
$$\hbar\omega \ll g^*\mu_B B + A\langle I_z \rangle$$

effective Zeeman gap

$$\hbar\omega \sim g^*\mu_B B + A\langle I_z \rangle$$

For $\hbar\omega \sim g^*\mu_B B + A\langle I_z \rangle$:

- **transitions** between the two Landau levels may occur
- Simultaneously, nuclear spins are flipped



Control of nuclear polarization via quantum pumping

Pumped current :

$$I_1 = 2\frac{e}{h}\mu\frac{q^2}{k_0^2}\left(-2 + \beta - \beta^2 + O\left(\frac{P}{k_0}\right)\right)$$

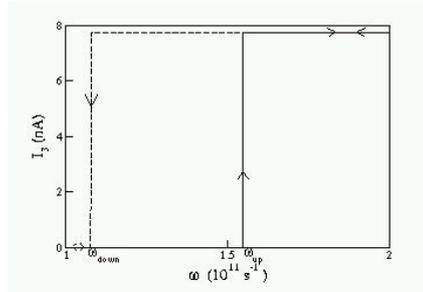
$$I_2 = 2\frac{e}{h}\mu\frac{q^2}{k_0^2}\left(2 - 2\beta + \beta^2 + O\left(\frac{P}{k_0}\right)\right)$$

$$I_3 = 2\beta\frac{e}{h}\mu\frac{q^2}{k_0^2}\left(1 + O\left(\frac{P}{k_0}\right)\right).$$

Measure I_3 as a function of ω :

$$\omega_{\text{up}} = g^*\mu_B B / \hbar$$

Sweep $\omega(t) = \omega(0) + \alpha t$



- $I_3 \sim 1-10$ nA, and 20 % shift of Zeeman gap for typical parameters
- Difference $\Delta\omega = \omega_{\text{up}} - \omega_{\text{down}}$ direct measure of local nuclear polarization

$$\Delta\omega = \frac{M}{\hbar(M - \hbar\alpha)} [2|g^*|\mu_B B - 2\hbar\omega(0) - \hbar\alpha(2t_{\text{sweep}} + t_{\text{dwell}})]$$

- Nuclear polarization set by the sweep time and sweep rate

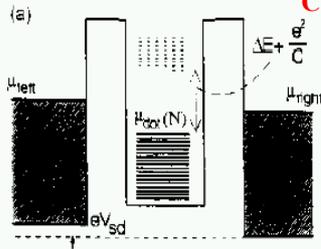
Perspectives

- Quantum pumping useful “tool” to study electron transport at the edge of a 2DEG in the quantum Hall regime
- Provides new technique to accurately **manipulate** and **monitor** local dynamic nuclear polarization
- Interesting as possibility for e.g. memory storage in solid-state systems

Reference: condmat/0307166

Transport through tunnel-coupled quantum dots: **Coulomb blockade**

Potential landscape of a dot



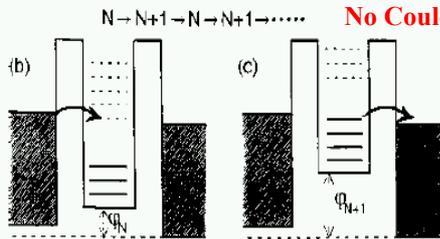
Coulomb blockade

ϕ_N = electrostatic potential of dot occupied by N electrons

$$V_{sd} = (\mu_{left} - \mu_{right})/e$$

Energy required to add an electron:

$$\mu_{dot}(N+1) - \mu_{dot}(N) = \Delta E + e^2/C$$



No Coulomb blockade

ΔE = energy level spacing, typically $10 \mu\text{eV}$.

In order to resolve the energy levels ΔE must be larger than the thermal energy, $\Delta E \gg k_B T$.

So temperature must be less than $\sim 10 \text{ mK}$